## Appendix 1

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

This Appendix has two parts. Part 1 is composed of 17 tables from the aspect of algebra, 15 figures from the aspect of geometry, as well as some Notations. While part 1 deals with the essence of Phillips unemployment, Part 2 clarifies the underlying background of Phillips unemployment by geometrical measurements, in the form of hyperbolas.

## Part 1: The essence of Phillips unemployment

## 1. Tables

## Algebraic measurements clarifying the essence of Phillips unemployment

These 17 tables are indicated as algebraic measurements to clarify the essence of Phillips unemployment. These tables are for 68 countries, 1990-2013, using the KEWT database series, 8.14 and 9.15. New discoveries soon after the EES (18 June 2014) clarify that Deficit=0 is most sustainable; effectively, efficiently, and robustly, resulting in the Rate of Inflation=0 and Technological Progress>0 (hereunder simply, the inflation rate).

Here is the list of these 17 tables at a glance.
Table A1 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A2 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A3 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A4 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A5 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)

## Appendix 1, HEU

Table A6 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A7 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A8 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A9 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A10 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)

Table A11 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A12 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)

Table A13 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A14 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A15 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A16 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)
Table A17 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. (by country, 1990-2013)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

Table A1 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$.
by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-\mathrm{i}} \mathrm{PRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{spRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 17 Asian counries |  |  | E0. Euro Area using IMF data |  |  | 15 Europe except for Euro Area |  |  | 1. Argentina |  |  |
| 1990 | (0.0630) | 0.0754 | 0.0125 |  |  |  | (0.0055) | 0.0091 | 0.0036 | (0.0020) | 0.0497 | 0.0477 |
| 1991 | (0.0591) | 0.0845 | 0.0255 |  |  |  | (0.0264) | 0.0220 | (0.0044) | (0.0058) | 0.0099 | 0.0041 |
| 1992 | (0.0589) | 0.0927 | 0.0338 |  |  |  | (0.0403) | 0.0390 | (0.0013) | (0.0004) | (0.0277) | (0.0281) |
| 1993 | (0.0591) | 0.0905 | 0.0314 |  |  |  | (0.0689) | 0.0332 | (0.0357) | (0.0074) | (0.0334) | (0.0408) |
| 1994 | (0.0577) | 0.0843 | 0.0266 |  |  |  | (0.0568) | 0.0445 | (0.0123) | (0.0081) | (0.0420) | (0.0501) |
| 1995 | (0.0565) | 0.0755 | 0.0190 |  |  |  | (0.0372) | 0.0136 | (0.0236) | (0.0061) | (0.0187) | (0.0248) |
| 1996 | (0.0552) | 0.0691 | 0.0139 |  |  |  | (0.0311) | (0.0131) | (0.0442) | (0.0214) | (0.0085) | (0.0299) |
| 1997 | (0.0442) | 0.0713 | 0.0271 |  |  |  | (0.0288) | (0.0104) | (0.0392) | (0.0165) | (0.0320) | (0.0485) |
| 1998 | (0.1305) | 0.1643 | 0.0338 |  |  |  | (0.0267) | 0.0048 | (0.0219) | (0.0154) | (0.0404) | (0.0558) |
| 1999 | (0.0883) | 0.1171 | 0.0288 | (0.0091) | 0.0202 | 0.0111 | (0.0366) | 0.0158 | (0.0209) | (0.0318) | (0.0168) | (0.0487) |
| 2000 | (0.0892) | 0.1149 | 0.0257 | (0.0051) | 0.0084 | 0.0034 | (0.0214) | (0.0176) | (0.0390) | (0.0267) | (0.0096) | (0.0362) |
| 2001 | (0.0681) | 0.0917 | 0.0236 | (0.0145) | 0.0236 | 0.0091 | (0.0316) | 0.0281 | (0.0035) | (0.8432) | 0.8257 | (0.0174) |
| 2002 | (0.0868) | 0.1181 | 0.0313 | (0.0223) | 0.0401 | 0.0179 | (0.0284) | 0.0201 | (0.0083) | (0.8044) | 0.8910 | 0.0866 |
| 2003 | (0.0854) | 0.1195 | 0.0341 | (0.0283) | 0.0447 | 0.0164 | (0.0637) | 0.0297 | (0.0340) | (0.3704) | 0.4268 | 0.0564 |
| 2004 | (0.0654) | 0.1038 | 0.0384 | (0.0267) | 0.0510 | 0.0244 | (0.0350) | (0.0153) | (0.0503) | (0.1615) | 0.1782 | 0.0168 |
| 2005 | (0.0529) | 0.0879 | 0.0350 | (0.0224) | 0.0406 | 0.0182 | (0.0233) | (0.0368) | (0.0601) | (0.8836) | 0.9112 | 0.0277 |
| 2006 | (0.0397) | 0.0784 | 0.0387 | (0.0091) | 0.0281 | 0.0190 | (0.0122) | (0.0673) | (0.0795) | (0.3644) | 0.3989 | 0.0345 |
| 2007 | (0.0234) | 0.0710 | 0.0477 | 0.0001 | 0.0188 | 0.0189 | (0.0053) | (0.0844) | (0.0898) | (0.2741) | 0.2993 | 0.0253 |
| 2008 | (0.0459) | 0.0744 | 0.0285 | (0.0165) | 0.0226 | 0.0061 | (0.0200) | (0.0644) | (0.0844) | (0.2365) | 0.2680 | 0.0315 |
| 2009 | (0.1023) | 0.1260 | 0.0237 | (0.0629) | 0.0773 | 0.0143 | (0.0506) | 0.0212 | (0.0294) | (0.3476) | 0.4412 | 0.0936 |
| 2010 | (0.0890) | 0.1171 | 0.0282 | (0.0651) | 0.0815 | 0.0164 | (0.0418) | (0.0112) | (0.0530) | (0.0327) | 0.0999 | 0.0672 |
| 2011 | (0.0973) | 0.1066 | 0.0092 | (0.0651) | 0.0815 | 0.0164 | (0.0361) | 0.0214 | (0.0147) | (0.0992) | 0.1516 | 0.0524 |
| 2012 | (0.0973) | 0.1066 | 0.0092 | (0.0651) | 0.0815 | 0.0164 | (0.0342) | 0.0210 | (0.0132) | (0.0513) | 0.1006 | 0.0493 |
| 2013 | (0.0973) | 0.1066 | 0.0092 | (0.0447) | 0.0617 | 0.0169 | (0.1044) | 0.0643 | (0.0401) | (0.0513) | 0.1006 | 0.0493 |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | gy * | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 17 Asian counries |  |  | E0. Euro Area using IMF data |  |  | 15 Europe except for Euro Area |  |  | 1. Argentina |  |  |
| 1990 | 0.0714 | 0.0671 | 0.0385 |  |  |  | 0.0331 | 0.0430 | 0.0299 | 0.5257 | (0.0571) | (0.0506) |
| 1991 | 0.0707 | 0.0631 | 0.0353 |  |  |  | 0.0675 | 0.0574 | 0.0438 | 2.6261 | (0.1099) | (0.0768) |
| 1992 | 0.0445 | 0.0483 | 0.0269 |  |  |  | (0.0556) | 0.1711 | (0.0805) | 7.8699 | (0.0928) | (0.0648) |
| 1993 | 0.0306 | 0.0408 | 0.0219 |  |  |  | 0.0911 | 0.0585 | 0.0458 | 0.5155 | 0.1258 | 0.0996 |
| 1994 | 0.0248 | 0.0378 | 0.0196 |  |  |  | (0.1416) | 0.1715 | (0.3154) | 0.3217 | 0.1181 | 0.0927 |
| 1995 | 0.0219 | 0.0365 | 0.0189 |  |  |  | 0.0887 | 0.0687 | 0.0609 | 0.2041 | 0.0990 | 0.0749 |
| 1996 | 0.0168 | 0.0358 | 0.0155 |  |  |  | 0.0975 | 0.0807 | 0.0727 | 0.1597 | 0.1002 | 0.0784 |
| 1997 | 0.0183 | 0.0350 | 0.0151 |  |  |  | 0.1807 | 0.0776 | 0.0705 | 0.1356 | 0.1019 | 0.0811 |
| 1998 | 0.0090 | 0.0236 | 0.0065 |  |  |  | 0.2000 | 0.0871 | 0.0799 | 0.1097 | 0.0974 | 0.0761 |
| 1999 | 0.0095 | 0.0195 | 0.0058 | 0.0235 | 0.0206 | 0.0154 | 0.2294 | 0.0751 | 0.0672 | 0.1013 | 0.0710 | 0.0519 |
| 2000 | 0.0092 | 0.0236 | 0.0068 | 0.0237 | 0.0227 | 0.0166 | 0.2434 | 0.0887 | 0.0794 | 0.0846 | 0.0641 | 0.0471 |
| 2001 | 0.0103 | 0.0177 | 0.0055 | 0.0242 | 0.0280 | 0.0208 | 0.2754 | 0.0636 | 0.0642 | 0.0703 | 0.0502 | 0.0354 |
| 2002 | 0.0011 | 0.0115 | 0.0004 | 0.0418 | 0.0420 | 0.0304 | 0.2446 | 0.0774 | 0.0701 | 0.1094 | 0.0503 | 0.0342 |
| 2003 | 0.0035 | 0.0121 | 0.0012 | 0.0213 | 0.0249 | 0.0167 | 0.2682 | 0.0795 | 0.0707 | 0.1172 | 0.0648 | 0.0475 |
| 2004 | 0.0086 | 0.0151 | 0.0040 | 0.0212 | 0.0243 | 0.0160 | 0.2405 | 0.0891 | 0.0787 | 0.1327 | 0.0903 | 0.0682 |
| 2005 | 0.0085 | 0.0141 | 0.0036 | 0.0235 | 0.0250 | 0.0182 | 0.2175 | 0.0902 | 0.0790 | 0.1458 | 0.0899 | 0.0665 |
| 2006 | 0.0094 | 0.0149 | 0.0043 | 0.0234 | 0.0271 | 0.0189 | 0.1707 | 0.1065 | 0.0938 | 0.1861 | 0.1003 | 0.0711 |
| 2007 | 0.1386 | (0.0251) | (0.0242) | 0.0287 | 0.0328 | 0.0239 | 0.1477 | 0.1067 | 0.0935 | 0.1882 | 0.1057 | 0.0756 |
| 2008 | 0.0173 | 0.0227 | 0.0117 | 0.0261 | 0.0309 | 0.0236 | 0.1203 | 0.1079 | 0.0951 | 0.2160 | 0.1052 | 0.0784 |
| 2009 | 0.0182 | 0.0245 | 0.0135 | 0.0245 | 0.0203 | 0.0158 | 0.1153 | 0.0594 | 0.0505 | 0.1437 | 0.0546 | 0.0382 |
| 2010 | 0.0226 | 0.0293 | 0.0177 | 0.0265 | 0.0204 | 0.0173 | 0.1050 | 0.0746 | 0.0647 | 0.2133 | 0.0999 | 0.0616 |
| 2011 | 0.0233 | 0.0311 | 0.0210 | 0.0264 | 0.0217 | 0.0185 | 0.0952 | 0.0612 | 0.0532 | 0.2302 | 0.1182 | 0.0712 |
| 2012 | (0.0187) | (0.7909) | 1.3388 | 0.0261 | 0.0191 | 0.0162 | 0.0882 | 0.0663 | 0.0582 | 0.1849 | 0.1056 | 0.0647 |
| 2013 | (0.8881) | 0.0159 | (0.8068) | 0.0271 | 0.0185 | 0.0168 | (0.2563) | (0.1554) | 0.4232 | 0.2199 | 0.1031 | 0.0706 |

## Appendix 1, HEU

Table A2 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of Y, $g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{sprI}^{-\mathrm{i}_{\mathrm{PRI}}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1. The US |  |  | E1. Austria |  |  | 1. Denmark |  |  | 2. Bolivia |  |  |
| 1990 | (0.0422) | 0.0305 | (0.0117) | (0.0528) | 0.0633 | 0.0105 | (0.0078) | 0.0203 | 0.0125 | (0.0582) | 0.0453 | (0.0130) |
| 1991 | (0.0512) | 0.0500 | (0.0012) | (0.0560) | 0.0582 | 0.0022 | (0.0131) | 0.0352 | 0.0221 | (0.0529) | (0.0088) | (0.0617) |
| 1992 | (0.0515) | 0.0482 | (0.0033) | (0.0458) | 0.0513 | 0.0056 | (0.0176) | 0.0516 | 0.0340 | (0.0510) | (0.0503) | (0.1013) |
| 1993 | (0.0434) | 0.0345 | (0.0089) | (0.0594) | 0.0619 | 0.0025 | (0.0253) | 0.0681 | 0.0428 | (0.0533) | (0.0512) | (0.1046) |
| 1994 | (0.0325) | 0.0179 | (0.0146) | (0.0659) | 0.0586 | (0.0072) | (0.0264) | 0.0588 | 0.0324 | (0.0367) | (0.0255) | (0.0622) |
| 1995 | (0.0227) | 0.0140 | (0.0087) | (0.0584) | 0.0513 | (0.0071) | (0.0261) | 0.0601 | 0.0339 | (0.0243) | (0.0278) | (0.0521) |
| 1996 | (0.0162) | 0.0079 | (0.0083) | (0.0469) | 0.0339 | (0.0129) | (0.0032) | 0.0440 | 0.0408 | (0.0260) | (0.0267) | (0.0527) |
| 1997 | (0.0003) | (0.0079) | (0.0082) | (0.0203) | 0.0214 | 0.0011 | 0.0126 | 0.0127 | 0.0254 | (0.0481) | (0.0446) | (0.0927) |
| 1998 | 0.0070 | (0.0214) | (0.0143) | (0.0267) | 0.0425 | 0.0158 | 0.0188 | (0.0077) | 0.0111 | (0.0460) | (0.0988) | (0.1448) |
| 1999 | 0.0146 | (0.0425) | (0.0279) | (0.0260) | 0.0295 | 0.0035 | 0.0104 | 0.0369 | 0.0472 | (0.0459) | (0.0710) | (0.1169) |
| 2000 | 0.0262 | (0.0644) | (0.0382) | (0.0263) | 0.0376 | 0.0112 | 0.0210 | 0.0231 | 0.0440 | (0.0501) | (0.0515) | (0.1017) |
| 2001 | 0.0138 | (0.0484) | (0.0346) | (0.0053) | 0.0064 | 0.0011 | 0.0113 | 0.0474 | 0.0587 | (0.0818) | 0.0224 | (0.0594) |
| 2002 | (0.0170) | (0.0233) | (0.0403) | (0.0112) | 0.0523 | 0.0411 | 0.0009 | 0.0515 | 0.0524 | (0.1056) | 0.0372 | (0.0683) |
| 2003 | (0.0382) | (0.0063) | (0.0445) | (0.0213) | 0.0502 | 0.0289 | (0.0044) | 0.0681 | 0.0638 | (0.0789) | 0.0703 | (0.0086) |
| 2004 | (0.0397) | (0.0111) | (0.0508) | (0.0557) | 0.0909 | 0.0352 | 0.0205 | 0.0398 | 0.0603 | (0.0669) | 0.0745 | 0.0076 |
| 2005 | (0.0289) | (0.0282) | (0.0571) | (0.0231) | 0.0577 | 0.0346 | 0.0542 | 0.0166 | 0.0707 | 0.0045 | 0.0343 | 0.0388 |
| 2006 | (0.0210) | (0.0379) | (0.0589) | (0.0233) | 0.0695 | 0.0462 | 0.0572 | (0.0006) | 0.0567 | 0.0484 | 0.0528 | 0.1012 |
| 2007 | (0.0128) | (0.0334) | (0.0462) | (0.0126) | 0.0652 | 0.0526 | 0.0541 | (0.0163) | 0.0378 | 0.0270 | 0.0576 | 0.0846 |
| 2008 | (0.0335) | (0.0080) | (0.0416) | (0.0129) | 0.0771 | 0.0642 | 0.0381 | 0.0155 | 0.0536 | 0.0463 | 0.0317 | 0.0780 |
| 2009 | (0.1172) | 0.0975 | (0.0197) | (0.0488) | 0.0901 | 0.0413 | (0.0294) | 0.0909 | 0.0616 | (0.0259) | 0.0576 | 0.0317 |
| 2010 | (0.1008) | 0.0753 | (0.0255) | (0.0543) | 0.1006 | 0.0463 | (0.0277) | 0.1043 | 0.0766 | (0.0169) | 0.0941 | 0.0771 |
| 2011 | (0.1008) | 0.0753 | (0.0255) | (0.0316) | 0.0664 | 0.0348 | (0.0193) | 0.1051 | 0.0858 | (0.0299) | 0.0940 | 0.0641 |
| 2012 | (0.1008) | 0.0753 | (0.0255) | (0.0316) | 0.0664 | 0.0348 | (0.0405) | 0.1282 | 0.0877 | 0.0364 | 0.0692 | 0.1056 |
| 2013 | (0.1008) | 0.0753 | (0.0255) | (0.0316) | 0.0664 | 0.0348 | (0.0405) | 0.1282 | 0.0877 | 0.0364 | 0.0692 | 0.1056 |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla .rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1. the U S |  |  | E1. Austria |  |  | 1. Denmark |  |  | 2. Bolivia |  |  |
| 1990 | 0.0459 | 0.0212 | 0.0082 | 0.0332 | 0.0411 | 0.0284 | 0.1077 | 0.0675 | 0.0590 | (0.0026) | 0.0214 | (0.0003) |
| 1991 | 0.0346 | 0.0220 | 0.0072 | 0.0340 | 0.0437 | 0.0308 | 0.0976 | 0.0584 | 0.0508 | 0.0963 | 0.0464 | 0.0184 |
| 1992 | 0.0349 | 0.0210 | 0.0064 | 0.0389 | 0.0394 | 0.0330 | 0.0859 | 0.0493 | 0.0409 | 0.1192 | 0.0562 | 0.0257 |
| 1993 | 0.0464 | 0.0281 | 0.0129 | 0.0361 | 0.0365 | 0.0307 | 0.0772 | 0.0377 | 0.0306 | 0.1213 | 0.0551 | 0.0253 |
| 1994 | 0.0523 | 0.0326 | 0.0175 | 0.0380 | 0.0420 | 0.0355 | 0.0804 | 0.0375 | 0.0322 | 0.0891 | 0.0394 | 0.0128 |
| 1995 | 0.0505 | 0.0301 | 0.0157 | 0.0371 | 0.0311 | 0.0258 | 0.0865 | 0.0567 | 0.0453 | 0.1212 | 0.0471 | 0.0197 |
| 1996 | 0.0510 | 0.0332 | 0.0187 | 0.0351 | 0.0307 | 0.0229 | 0.0881 | 0.0530 | 0.0436 | 0.1428 | 0.0563 | 0.0268 |
| 1997 | 0.0500 | 0.0383 | 0.0234 | 0.0306 | 0.0303 | 0.0216 | 0.0887 | 0.0616 | 0.0509 | 0.1656 | 0.0808 | 0.0478 |
| 1998 | 0.0496 | 0.0438 | 0.0283 | 0.0363 | 0.0287 | 0.0249 | 0.0761 | 0.0610 | 0.0510 | 0.1574 | 0.1082 | 0.0677 |
| 1999 | 0.0513 | 0.0518 | 0.0359 | 0.0280 | 0.0271 | 0.0234 | 0.0875 | 0.0486 | 0.0424 | 0.1322 | 0.0662 | 0.0375 |
| 2000 | 0.0519 | 0.0551 | 0.0389 | 0.0273 | 0.0275 | 0.0226 | 0.1055 | 0.0626 | 0.0493 | 0.1225 | 0.0605 | 0.0332 |
| 2001 | 0.0565 | 0.0424 | 0.0275 | 0.0253 | 0.0312 | 0.0236 | 0.0999 | 0.0524 | 0.0426 | 0.0119 | 0.0437 | 0.0023 |
| 2002 | 0.0655 | 0.0330 | 0.0190 | 0.0249 | 0.0236 | 0.0167 | 0.0830 | 0.0502 | 0.0398 | 0.0991 | 0.0467 | 0.0218 |
| 2003 | 0.0705 | 0.0311 | 0.0176 | 0.0223 | 0.0244 | 0.0164 | 0.0785 | 0.0419 | 0.0345 | 0.0469 | 0.0257 | 0.0054 |
| 2004 | 0.0746 | 0.0340 | 0.0202 | 0.0282 | 0.0295 | 0.0206 | 0.0680 | 0.0404 | 0.0320 | 0.1040 | 0.0400 | 0.0177 |
| 2005 | 0.0808 | 0.0335 | 0.0196 | 0.0278 | 0.0291 | 0.0204 | 0.0714 | 0.0385 | 0.0301 | 0.0955 | 0.0340 | 0.0130 |
| 2006 | 0.0738 | 0.0427 | 0.0283 | 0.0332 | 0.0293 | 0.0213 | 0.0729 | 0.0444 | 0.0350 | 0.1154 | 0.0328 | 0.0121 |
| 2007 | 0.0611 | 0.0471 | 0.0332 | 0.0431 | 0.0323 | 0.0244 | 0.0642 | 0.0489 | 0.0376 | 0.1623 | 0.0429 | 0.0216 |
| 2008 | 0.0644 | 0.0381 | 0.0250 | 0.0394 | 0.0277 | 0.0207 | 0.0526 | 0.0369 | 0.0278 | 0.2138 | 0.0616 | 0.0379 |
| 2009 | (0.0533) | 0.0063 | (0.0020) | 0.0262 | 0.0231 | 0.0175 | 0.0381 | 0.0183 | 0.0133 | 0.1044 | 0.0459 | 0.0248 |
| 2010 | 0.0524 | 0.0161 | 0.0059 | 0.0274 | 0.0233 | 0.0176 | 0.0374 | 0.0200 | 0.0131 | 0.1190 | 0.0478 | 0.0253 |
| 2011 | 0.0174 | 0.0207 | 0.0025 | 0.0313 | 0.0290 | 0.0225 | 0.0371 | 0.0185 | 0.0118 | 0.1559 | 0.0663 | 0.0413 |
| 2012 | 0.0568 | 0.0175 | 0.0070 | 0.0313 | 0.0283 | 0.0218 | 0.0372 | 0.0141 | 0.0095 | 0.1505 | 0.0550 | 0.0303 |
| 2013 | 0.1133 | 0.0145 | 0.0118 | 0.0346 | 0.0267 | 0.0237 | 0.0490 | 0.0128 | 0.0116 | 0.1998 | 0.0404 | 0.0333 |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A3 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PrI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2. Canada |  |  | E2. Belgium |  |  | 2. Iceland |  |  | 3. Brazil |  |  |
| 1990 | (0.0527) | 0.0095 | (0.0433) | (0.0662) | 0.0848 | 0.0185 | (0.0276) | 0.0037 | (0.0239) | (0.0647) | 0.0781 | 0.0135 |
| 1991 | (0.0611) | 0.0178 | (0.0433) | (0.0722) | 0.0988 | 0.0265 | (0.0491) | (0.0020) | (0.0511) | (0.0474) | 0.0557 | 0.0083 |
| 1992 | (0.0652) | 0.0219 | (0.0433) | (0.0773) | 0.1115 | 0.0342 | (0.0353) | 0.0014 | (0.0339) | (0.0422) | 0.0696 | 0.0274 |
| 1993 | (0.0649) | 0.0266 | (0.0383) | (0.0716) | 0.1282 | 0.0566 | (0.0460) | 0.0467 | 0.0007 | (0.1036) | 0.1166 | 0.0130 |
| 1994 | (0.0527) | 0.0255 | (0.0271) | (0.0537) | 0.1167 | 0.0630 | (0.0568) | 0.0801 | 0.0233 | (0.0677) | 0.0662 | (0.0015) |
| 1995 | (0.0431) | 0.0391 | (0.0040) | (0.0617) | 0.1343 | 0.0725 | (0.0512) | 0.0608 | 0.0096 | (0.0394) | 0.0065 | (0.0329) |
| 1996 | (0.0222) | 0.0299 | 0.0077 | (0.0428) | 0.1095 | 0.0667 | (0.0103) | (0.0088) | (0.0191) | (0.0527) | 0.0166 | (0.0361) |
| 1997 | 0.0072 | (0.0212) | (0.0140) | (0.0326) | 0.1034 | 0.0708 | 0.0040 | (0.0237) | (0.0197) | (0.0753) | 0.0303 | (0.0451) |
| 1998 | 0.0169 | (0.0338) | (0.0169) | (0.0260) | 0.0978 | 0.0718 | 0.0312 | (0.1055) | (0.0743) | (0.0804) | 0.0486 | (0.0318) |
| 1999 | 0.0276 | (0.0239) | 0.0037 | (0.0033) | 0.0229 | 0.0197 | 0.0364 | (0.1113) | (0.0749) | (0.0417) | (0.0095) | (0.0512) |
| 2000 | 0.0386 | (0.0022) | 0.0364 | 0.0027 | 0.0213 | 0.0240 | 0.0157 | (0.1285) | (0.1129) | (0.0094) | (0.0409) | (0.0503) |
| 2001 | 0.0085 | 0.0276 | 0.0361 | 0.0039 | 0.0544 | 0.0583 | 0.0213 | (0.0684) | (0.0472) | (0.0233) | 0.0125 | (0.0107) |
| 2002 | 0.0090 | 0.0146 | 0.0235 | (0.0017) | 0.0816 | 0.0798 | (0.0027) | 0.0184 | 0.0156 | (0.0131) | 0.0338 | 0.0208 |
| 2003 | 0.0083 | 0.0156 | 0.0239 | (0.0022) | 0.0857 | 0.0835 | (0.0121) | (0.0399) | (0.0520) | (0.0484) | 0.0772 | 0.0288 |
| 2004 | 0.0235 | 0.0055 | 0.0290 | (0.0027) | 0.0710 | 0.0683 | 0.0231 | (0.1326) | (0.1095) | (0.0207) | 0.0604 | 0.0397 |
| 2005 | 0.0285 | (0.0030) | 0.0256 | (0.0305) | 0.0838 | 0.0533 | 0.1079 | (0.2860) | (0.1781) | (0.0400) | 0.0769 | 0.0369 |
| 2006 | 0.0335 | (0.0165) | 0.0171 | 0.0036 | 0.0501 | 0.0537 | 0.0948 | (0.3602) | (0.2654) | (0.0240) | 0.0535 | 0.0295 |
| 2007 | 0.0241 | (0.0154) | 0.0087 | (0.0012) | 0.0576 | 0.0564 | 0.0883 | (0.2697) | (0.1815) | (0.0117) | 0.0267 | 0.0150 |
| 2008 | (0.0015) | 0.0094 | 0.0079 | (0.0123) | 0.0391 | 0.0269 | 0.0165 | (0.2901) | (0.2736) | (0.0314) | 0.0309 | (0.0006) |
| 2009 | (0.0374) | 0.0021 | (0.0353) | (0.0656) | 0.0901 | 0.0246 | (0.0835) | (0.0263) | (0.1098) | (0.0267) | 0.0226 | (0.0040) |
| 2010 | (0.0473) | 0.0045 | (0.0428) | (0.0453) | 0.0943 | 0.0490 | (0.0665) | (0.0208) | (0.0873) | (0.0046) | (0.0089) | (0.0135) |
| 2011 | (0.0332) | (0.0028) | (0.0360) | (0.0451) | 0.0722 | 0.0270 | (0.0485) | (0.0218) | (0.0703) | (0.0146) | 0.0043 | (0.0103) |
| 2012 | (0.0332) | (0.0028) | (0.0360) | (0.0451) | 0.0722 | 0.0270 | (0.0493) | (0.0508) | (0.1001) | (0.0068) | (0.0108) | (0.0176) |
| 2013 | (0.0332) | (0.0028) | (0.0360) | (0.0451) | 0.0722 | 0.0270 | (0.0493) | (0.0508) | (0.1001) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2. Canada |  |  | E2. Belgium |  |  | 2. Iceland |  |  | 3. Brazil |  |  |
| 1990 | 0.0572 | 0.0797 | 0.0577 | 0.0670 | 0.0300 | 0.0242 | 0.0587 | 0.0585 | 0.0416 | 0.0544 | 0.1013 | 0.0749 |
| 1991 | 0.0541 | 0.0619 | 0.0446 | 0.0758 | 0.0221 | 0.0188 | 0.0660 | 0.0616 | 0.0439 | 0.1980 | 0.0960 | 0.0712 |
| 1992 | 0.0494 | 0.0638 | 0.0459 | 0.0579 | 0.0377 | 0.0277 | 0.0597 | 0.0498 | 0.0335 | 0.1688 | 0.0843 | 0.0611 |
| 1993 | 0.0484 | 0.0529 | 0.0371 | 0.0602 | 0.0206 | 0.0159 | 0.0486 | 0.0419 | 0.0271 | 0.0298 | 0.0434 | 0.0253 |
| 1994 | 0.0441 | 0.0574 | 0.0409 | 0.0683 | 0.0096 | 0.0077 | 0.0448 | 0.0384 | 0.0242 | 0.0810 | 0.0791 | 0.0573 |
| 1995 | 0.0447 | 0.0285 | 0.0171 | 0.0826 | 0.0266 | 0.0249 | 0.0451 | 0.0412 | 0.0267 | (0.0146) | 0.0280 | (0.0200) |
| 1996 | 0.0388 | 0.0256 | 0.0138 | 0.0770 | 0.0359 | 0.0294 | 0.0487 | 0.0519 | 0.0365 | 0.0086 | 0.0259 | 0.0095 |
| 1997 | 0.0445 | 0.0371 | 0.0248 | 0.0879 | 0.0396 | 0.0331 | 0.0494 | 0.0555 | 0.0399 | 0.0104 | 0.0293 | 0.0121 |
| 1998 | 0.0454 | 0.0351 | 0.0230 | 0.0844 | 0.0367 | 0.0315 | 0.0527 | 0.0755 | 0.0579 | 0.0098 | 0.0260 | 0.0097 |
| 1999 | 0.0407 | 0.0357 | 0.0239 | 0.0786 | 0.0536 | 0.0361 | 0.0587 | 0.0630 | 0.0459 | 0.0127 | 0.0310 | 0.0143 |
| 2000 | 0.0450 | 0.0394 | 0.0273 | 0.0667 | 0.0469 | 0.0339 | 0.0657 | 0.0719 | 0.0531 | 0.0133 | 0.0296 | 0.0119 |
| 2001 | 0.0370 | 0.0314 | 0.0194 | 0.0225 | 0.0266 | 0.0135 | 0.0493 | 0.0649 | 0.0487 | 0.0108 | 0.0226 | 0.0071 |
| 2002 | 0.0377 | 0.0332 | 0.0208 | 0.0236 | 0.0164 | 0.0110 | 0.0429 | 0.0373 | 0.0241 | 0.0091 | 0.0192 | 0.0049 |
| 2003 | 0.0372 | 0.0339 | 0.0209 | (0.0311) | 0.0017 | (0.0019) | 0.0511 | 0.0511 | 0.0325 | 0.0126 | 0.0208 | 0.0069 |
| 2004 | 0.0393 | 0.0368 | 0.0237 | 0.0247 | 0.0210 | 0.0133 | 0.0516 | 0.0775 | 0.0564 | 0.0206 | 0.0275 | 0.0134 |
| 2005 | 0.0406 | 0.0398 | 0.0261 | 0.0192 | 0.0202 | 0.0120 | 0.0603 | 0.0943 | 0.0700 | 0.0216 | 0.0256 | 0.0125 |
| 2006 | 0.0425 | 0.0447 | 0.0303 | 0.0230 | 0.0242 | 0.0146 | 0.0520 | 0.1266 | 0.1004 | 0.0261 | 0.0282 | 0.0158 |
| 2007 | 0.0439 | 0.0487 | 0.0340 | 0.0208 | 0.0232 | 0.0129 | 0.0453 | 0.0974 | 0.0755 | 0.0322 | 0.0350 | 0.0225 |
| 2008 | 0.0429 | 0.0482 | 0.0336 | 0.0185 | 0.0248 | 0.0146 | 0.0414 | 0.1346 | 0.1114 | 0.0390 | 0.0460 | 0.0329 |
| 2009 | 0.0463 | 0.0329 | 0.0192 | 0.0144 | 0.0185 | 0.0091 | 0.0369 | 0.0741 | 0.0603 | 0.0389 | 0.0349 | 0.0232 |
| 2010 | 0.0480 | 0.0368 | 0.0231 | 0.0125 | 0.0138 | 0.0058 | 0.0289 | 0.0700 | 0.0450 | 0.0432 | 0.0469 | 0.0342 |
| 2011 | 0.0438 | 0.0398 | 0.0264 | 0.0182 | 0.0193 | 0.0117 | 0.0277 | 0.0640 | 0.0400 | 0.0317 | 0.0558 | 0.0254 |
| 2012 | 0.0550 | 0.0353 | 0.0314 | 0.0206 | 0.0186 | 0.0126 | 0.0283 | 0.0630 | 0.0455 | 0.0321 | 0.0468 | 0.0174 |
| 2013 | 0.0524 | 0.0341 | 0.0303 | 0.0267 | 0.0173 | 0.0157 | 0.0326 | 0.0563 | 0.0511 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A4 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{s}_{\text {PRI }}-\mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{sprI}^{-\mathrm{i}} \mathrm{PRI}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3. Australia |  |  | 3. Finland |  |  | 3. Norway |  |  | 4. Chile |  |  |
| 1990 | 0.0250 | (0.0917) | (0.0667) | 0.0021 | (0.0190) | (0.0169) | 0.0060 | 0.0342 | 0.0402 | 0.0089 | (0.0370) | (0.0281) |
| 1991 | 0.0062 | (0.0519) | (0.0457) | (0.0797) | 0.0724 | (0.0073) | (0.0326) | 0.0861 | 0.0535 | 0.0171 | (0.0302) | (0.0131) |
| 1992 | (0.0287) | (0.0165) | (0.0452) | (0.1658) | 0.1808 | 0.0151 | (0.0743) | 0.1270 | 0.0527 | 0.0245 | (0.0591) | (0.0346) |
| 1993 | (0.0413) | 0.0016 | (0.0396) | (0.1504) | 0.2109 | 0.0605 | (0.0619) | 0.1090 | 0.0471 | 0.0206 | (0.0857) | (0.0651) |
| 1994 | (0.0369) | (0.0245) | (0.0613) | (0.1295) | 0.2011 | 0.0716 | (0.0213) | 0.0713 | 0.0500 | 0.0170 | (0.0540) | (0.0370) |
| 1995 | (0.0289) | 0.0142 | (0.0148) | (0.1056) | 0.1503 | 0.0447 | 0.0173 | 0.0384 | 0.0556 | 0.0262 | (0.0452) | (0.0190) |
| 1996 | (0.0112) | 0.0091 | (0.0021) | (0.0696) | 0.1216 | 0.0519 | 0.0071 | 0.0807 | 0.0878 | 0.0234 | (0.0789) | (0.0555) |
| 1997 | 0.0045 | (0.0010) | 0.0036 | (0.0040) | 0.0721 | 0.0682 | 0.0089 | 0.0716 | 0.0805 | 0.0199 | (0.0788) | (0.0589) |
| 1998 | 0.0330 | (0.0907) | (0.0576) | (0.0006) | 0.0731 | 0.0725 | (0.0320) | 0.0398 | 0.0079 | 0.0040 | (0.0667) | (0.0627) |
| 1999 | (0.0065) | (0.0593) | (0.0658) | 0.0145 | 0.0843 | 0.0988 | (0.0428) | 0.1159 | 0.0731 | (0.0150) | 0.0064 | (0.0086) |
| 2000 | 0.0121 | (0.0590) | (0.0470) | 0.0333 | 0.0667 | 0.1000 | 0.0001 | 0.1770 | 0.1771 | 0.0015 | (0.0234) | (0.0218) |
| 2001 | 0.0134 | (0.0385) | (0.0251) | 0.0618 | 0.0442 | 0.1060 | 0.0002 | 0.1912 | 0.1914 | 0.0158 | (0.0365) | (0.0207) |
| 2002 | 0.0156 | (0.0606) | (0.0450) | 0.0531 | 0.0556 | 0.1088 | 0.0001 | 0.1537 | 0.1538 | 0.0074 | (0.0248) | (0.0174) |
| 2003 | 0.0183 | (0.0825) | (0.0642) | 0.0349 | 0.0373 | 0.0722 | (0.0004) | 0.1530 | 0.1526 | 0.0123 | (0.0323) | (0.0200) |
| 2004 | 0.0213 | (0.0953) | (0.0740) | 0.0337 | 0.0524 | 0.0861 | 0.0041 | 0.1501 | 0.1542 | 0.0367 | (0.0267) | 0.0100 |
| 2005 | 0.0259 | (0.0955) | (0.0696) | 0.0340 | 0.0217 | 0.0557 | 0.0054 | 0.1873 | 0.1927 | 0.0617 | (0.0636) | (0.0019) |
| 2006 | 0.0348 | (0.1002) | (0.0654) | 0.0473 | 0.0164 | 0.0637 | 0.0103 | 0.1933 | 0.2036 | 0.0909 | (0.0640) | 0.0269 |
| 2007 | 0.0328 | (0.1098) | (0.0771) | 0.0636 | (0.0055) | 0.0581 | 0.0022 | 0.1501 | 0.1523 | 0.1057 | (0.0791) | 0.0266 |
| 2008 | 0.0296 | (0.0844) | (0.0548) | 0.0532 | (0.0062) | 0.0470 | 0.0024 | 0.1864 | 0.1888 | 0.0630 | (0.1047) | (0.0416) |
| 2009 | (0.0186) | (0.0331) | (0.0518) | (0.0237) | 0.0599 | 0.0363 | 0.0152 | 0.1295 | 0.1448 | (0.0284) | 0.0407 | 0.0122 |
| 2010 | (0.0329) | 0.0022 | (0.0308) | (0.0278) | 0.0588 | 0.0310 | 0.0081 | 0.1392 | 0.1473 | 0.0124 | (0.0171) | (0.0047) |
| 2011 | (0.0329) | 0.0022 | (0.0308) | (0.0083) | 0.0053 | (0.0030) | 0.0055 | (0.6566) | (0.6511) | 0.0229 | (0.0490) | (0.0262) |
| 2012 | (0.0329) | 0.0022 | (0.0308) | (0.0083) | 0.0053 | (0.0030) | 0.0093 | (0.6530) | (0.6437) | 0.0255 | (0.0740) | (0.0484) |
| 2013 | (0.0329) | 0.0022 | (0.0308) | (0.0083) | 0.0053 | (0.0030) | 0.0093 | (0.6530) | (0.6437) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla. .ate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3. Australia |  |  | 3. Finland |  |  | 3. Norway |  |  | 4. Chile |  |  |
| 1990 | 0.0427 | 0.0516 | 0.0320 | 0.0612 | 0.0650 | 0.0500 | 0.1566 | 0.0811 | 0.0612 | 0.0870 | 0.0853 | 0.0588 |
| 1991 | 0.0321 | 0.0182 | 0.0041 | 0.0357 | 0.0275 | 0.0210 | 0.1367 | 0.0711 | 0.0520 | 0.0784 | 0.0840 | 0.0547 |
| 1992 | 0.0439 | 0.0205 | 0.0066 | 0.0287 | 0.0205 | 0.0129 | 0.0958 | 0.0591 | 0.0430 | 0.0970 | 0.1017 | 0.0684 |
| 1993 | 0.0553 | 0.0249 | 0.0119 | 0.0193 | 0.0124 | 0.0058 | 0.1031 | 0.0617 | 0.0465 | 0.1226 | 0.1249 | 0.0825 |
| 1994 | 0.0612 | 0.0379 | 0.0232 | 0.0293 | 0.0162 | 0.0110 | 0.1095 | 0.0606 | 0.0470 | 0.1797 | 0.1343 | 0.0793 |
| 1995 | 0.0383 | 0.0216 | 0.0077 | 0.0492 | 0.0377 | 0.0294 | 0.0931 | 0.0594 | 0.0404 | 0.0996 | 0.1075 | 0.0607 |
| 1996 | 0.0384 | 0.0235 | 0.0097 | 0.0425 | 0.0314 | 0.0243 | 0.1217 | 0.0528 | 0.0373 | 0.0756 | 0.0988 | 0.0696 |
| 1997 | 0.0398 | 0.0235 | 0.0104 | 0.0622 | 0.0352 | 0.0283 | 0.1399 | 0.0642 | 0.0419 | 0.0727 | 0.0964 | 0.0692 |
| 1998 | 0.0526 | 0.0552 | 0.0386 | 0.0815 | 0.0420 | 0.0325 | 0.0946 | 0.0723 | 0.0549 | 0.0532 | 0.0839 | 0.0614 |
| 1999 | 0.0562 | 0.0526 | 0.0360 | 0.0651 | 0.0290 | 0.0213 | 0.1101 | 0.0570 | 0.0384 | 0.0444 | 0.0588 | 0.0406 |
| 2000 | 0.0502 | 0.0499 | 0.0337 | 0.0778 | 0.0334 | 0.0238 | 0.1443 | 0.0516 | 0.0345 | 0.0482 | 0.0654 | 0.0462 |
| 2001 | 0.0476 | 0.0399 | 0.0245 | 0.0742 | 0.0327 | 0.0217 | 0.1208 | 0.0385 | 0.0237 | 0.0699 | 0.0772 | 0.0537 |
| 2002 | 0.0506 | 0.0481 | 0.0318 | 0.0643 | 0.0261 | 0.0193 | 0.0979 | 0.0354 | 0.0224 | 0.0730 | 0.0762 | 0.0527 |
| 2003 | 0.0499 | 0.0567 | 0.0392 | 0.0459 | 0.0272 | 0.0215 | 0.0982 | 0.0299 | 0.0201 | 0.0735 | 0.0763 | 0.0532 |
| 2004 | 0.0506 | 0.0585 | 0.0407 | 0.0412 | 0.0238 | 0.0170 | 0.1092 | 0.0414 | 0.0268 | 0.1261 | 0.0874 | 0.0536 |
| 2005 | 0.0422 | 0.0624 | 0.0412 | 0.0423 | 0.0293 | 0.0237 | 0.1371 | 0.0466 | 0.0292 | 0.1461 | 0.0992 | 0.0575 |
| 2006 | 0.0552 | 0.0552 | 0.0496 | 0.0408 | 0.0286 | 0.0214 | 0.1452 | 0.0562 | 0.0318 | 0.2177 | 0.1162 | 0.0541 |
| 2007 | 0.0445 | 0.0647 | 0.0482 | 0.0559 | 0.0374 | 0.0276 | 0.1364 | 0.0682 | 0.0413 | 0.1995 | 0.1088 | 0.0521 |
| 2008 | 0.0438 | 0.0686 | 0.0520 | 0.0378 | 0.0347 | 0.0232 | 0.1641 | 0.0692 | 0.0415 | 0.1292 | 0.1020 | 0.0610 |
| 2009 | 0.0392 | 0.0520 | 0.0371 | 0.0233 | 0.0175 | 0.0124 | 0.0818 | 0.0500 | 0.0250 | 0.0628 | 0.0599 | 0.0389 |
| 2010 | 0.0377 | 0.0529 | 0.0383 | 0.0210 | 0.0183 | 0.0114 | 0.0999 | 0.0498 | 0.0297 | 0.0773 | 0.0701 | 0.0475 |
| 2011 | 0.0437 | 0.0472 | 0.0428 | 0.0267 | 0.0281 | 0.0220 | 0.0930 | 0.2772 | 0.1951 | 0.0611 | 0.0691 | 0.0493 |
| 2012 | 0.0409 | 0.0451 | 0.0409 | 0.0274 | 0.0252 | 0.0194 | 0.0737 | 0.2259 | 0.1556 | 0.0507 | 0.0692 | 0.0516 |
| 2013 | 0.0385 | 0.0431 | 0.0391 | 0.0311 | 0.0238 | 0.0215 | 0.0608 | 0.1829 | 0.1332 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A5 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ * |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4. New Zealand |  |  | 4. France |  |  | 4. Sweden |  |  | 5. Colombia |  |  |
| 1990 | 0.0477 | 0.0424 | 0.0294 | 0.0342 | 0.0426 | 0.0333 | 0.0694 | 0.0747 | 0.0597 | 0.1165 | 0.0810 | 0.0563 |
| 1991 | 0.0117 | 0.0435 | 0.0066 | 0.0322 | 0.0381 | 0.0292 | 0.0658 | 0.0589 | 0.0467 | 0.1114 | 0.0529 | 0.0337 |
| 1992 | 0.0449 | 0.0338 | 0.0220 | 0.0303 | 0.0325 | 0.0243 | 0.0631 | 0.0525 | 0.0419 | 0.1121 | 0.0611 | 0.0433 |
| 1993 | 0.0361 | 0.0471 | 0.0320 | 0.0293 | 0.0237 | 0.0169 | 0.0592 | 0.0411 | 0.0316 | 0.1289 | 0.0854 | 0.0652 |
| 1994 | 0.0351 | 0.0581 | 0.0394 | 0.0303 | 0.0261 | 0.0197 | 0.0529 | 0.0460 | 0.0342 | 0.1433 | 0.1351 | 0.1120 |
| 1995 | 0.0363 | 0.0449 | 0.0216 | 0.0321 | 0.0277 | 0.0214 | 0.0840 | 0.0531 | 0.0423 | 0.1564 | 0.1316 | 0.1063 |
| 1996 | 0.0555 | 0.0410 | 0.0249 | 0.0311 | 0.0232 | 0.0170 | 0.0758 | 0.0468 | 0.0394 | 0.1313 | 0.1061 | 0.0820 |
| 1997 | 0.0538 | 0.0364 | 0.0211 | 0.0308 | 0.0213 | 0.0160 | 0.0712 | 0.0339 | 0.0304 | 0.1434 | 0.0984 | 0.0730 |
| 1998 | 0.0572 | 0.0275 | 0.0160 | 0.0332 | 0.0249 | 0.0199 | 0.0715 | 0.0350 | 0.0313 | 0.1545 | 0.0856 | 0.0620 |
| 1999 | 0.0584 | 0.0372 | 0.0217 | 0.0299 | 0.0218 | 0.0172 | 0.0754 | 0.0369 | 0.0327 | 0.1157 | 0.0411 | 0.0210 |
| 2000 | 0.0550 | 0.0333 | 0.0213 | 0.0316 | 0.0300 | 0.0248 | 0.0789 | 0.0411 | 0.0351 | 0.1068 | 0.0535 | 0.0319 |
| 2001 | 0.0373 | 0.0396 | 0.0233 | 0.0275 | 0.0255 | 0.0183 | 0.0716 | 0.0382 | 0.0305 | 0.1242 | 0.0618 | 0.0354 |
| 2002 | 0.0389 | 0.0398 | 0.0234 | 0.0249 | 0.0255 | 0.0166 | 0.0644 | 0.0327 | 0.0260 | 0.1301 | 0.0673 | 0.0432 |
| 2003 | 0.0418 | 0.0464 | 0.0294 | 0.0206 | 0.0245 | 0.0130 | 0.0549 | 0.0252 | 0.0173 | 0.1011 | 0.0822 | 0.0585 |
| 2004 | 0.0454 | 0.0521 | 0.0344 | 0.0211 | 0.0246 | 0.0132 | 0.0655 | 0.0305 | 0.0217 | 0.1017 | 0.0451 | 0.0257 |
| 2005 | 0.0540 | 0.0516 | 0.0305 | 0.0259 | 0.0259 | 0.0168 | 0.0680 | 0.0299 | 0.0211 | 0.0921 | 0.0389 | 0.0209 |
| 2006 | 0.0677 | 0.0421 | 0.0260 | 0.0271 | 0.0276 | 0.0188 | 0.0850 | 0.0319 | 0.0232 | 0.1034 | 0.0617 | 0.0415 |
| 2007 | 0.0625 | 0.0455 | 0.0296 | 0.0289 | 0.0312 | 0.0229 | 0.0945 | 0.0355 | 0.0248 | 0.1041 | 0.0696 | 0.0488 |
| 2008 | 0.0725 | 0.0358 | 0.0204 | 0.0290 | 0.0304 | 0.0225 | 0.0704 | 0.0300 | 0.0178 | 0.1023 | 0.0700 | 0.0495 |
| 2009 | 0.0401 | 0.0183 | 0.0072 | 0.0291 | 0.0201 | 0.0129 | 0.0362 | 0.0185 | 0.0098 | 0.0930 | 0.0711 | 0.0507 |
| 2010 | 0.0405 | 0.0212 | 0.0123 | 0.0297 | 0.0207 | 0.0135 | 0.0550 | 0.0276 | 0.0175 | 0.0862 | 0.0616 | 0.0426 |
| 2011 | 0.0590 | 0.0187 | 0.0164 | 0.0228 | 0.0269 | 0.0141 | 0.0486 | 0.0337 | 0.0160 | 0.1033 | 0.0747 | 0.0537 |
| 2012 | 0.0575 | 0.0184 | 0.0161 | 0.0210 | 0.0245 | 0.0117 | 0.0424 | 0.0305 | 0.0144 | 0.0917 | 0.0713 | 0.0516 |
| 2013 | 0.0560 | 0.0181 | 0.0158 | 0.0290 | 0.0230 | 0.0154 | 0.0596 | 0.0277 | 0.0186 | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4. New Zealand |  |  | 4. France |  |  | 4. Sweden |  |  | 5. Colombia |  |  |
| 1990 | 0.0460 | (0.0871) | (0.0411) | (0.0236) | 0.0134 | (0.0102) | 0.0112 | (0.0407) | (0.0294) | (0.0090) | 0.0421 | 0.0331 |
| 1991 | 0.0229 | (0.0641) | (0.0412) | (0.0142) | 0.0118 | (0.0024) | (0.0169) | 0.0023 | (0.0146) | 0.0011 | 0.0750 | 0.0761 |
| 1992 | (0.0262) | (0.0051) | (0.0313) | (0.0440) | 0.0499 | 0.0059 | (0.0458) | 0.0234 | (0.0224) | (0.0370) | 0.0553 | 0.0182 |
| 1993 | 0.0012 | (0.0306) | (0.0294) | (0.0638) | 0.0790 | 0.0151 | (0.1635) | 0.1595 | (0.0040) | (0.0083) | (0.0114) | (0.0197) |
| 1994 | 0.0092 | (0.0640) | (0.0549) | (0.0626) | 0.0791 | 0.0164 | (0.1397) | 0.1411 | 0.0014 | (0.0169) | (0.0686) | (0.0855) |
| 1995 | 0.0053 | (0.0759) | (0.0706) | (0.0721) | 0.0790 | 0.0069 | (0.0941) | 0.1393 | 0.0451 | (0.0255) | (0.0649) | (0.0904) |
| 1996 | 0.0640 | (0.1506) | (0.0866) | (0.0577) | 0.0739 | 0.0163 | (0.0349) | 0.0786 | 0.0438 | (0.0417) | (0.0445) | (0.0862) |
| 1997 | 0.0483 | (0.1219) | (0.0736) | (0.0384) | 0.0736 | 0.0352 | (0.0097) | 0.0695 | 0.0598 | (0.0411) | (0.0493) | (0.0904) |
| 1998 | 0.0058 | (0.0616) | (0.0558) | (0.0278) | 0.0617 | 0.0339 | 0.0038 | 0.0551 | 0.0589 | (0.0549) | (0.0304) | (0.0853) |
| 1999 | 0.0234 | (0.1076) | (0.0842) | (0.0198) | 0.0605 | 0.0407 | 0.0160 | 0.0449 | 0.0609 | (0.0773) | 0.0628 | (0.0145) |
| 2000 | 0.0109 | (0.0723) | (0.0614) | (0.0058) | 0.0168 | 0.0109 | 0.0444 | 0.0159 | 0.0603 | (0.0563) | 0.0493 | (0.0069) |
| 2001 | 0.0068 | (0.0485) | (0.0416) | (0.0079) | 0.0360 | 0.0281 | 0.0233 | 0.0437 | 0.0670 | (0.0371) | (0.0032) | (0.0403) |
| 2002 | 0.0229 | (0.0681) | (0.0452) | (0.0267) | 0.0511 | 0.0244 | (0.0080) | 0.0792 | 0.0712 | (0.0577) | 0.0038 | (0.0539) |
| 2003 | 0.0321 | (0.0957) | (0.0636) | (0.0358) | 0.0569 | 0.0211 | (0.0074) | 0.0968 | 0.0894 | (0.0283) | (0.0251) | (0.0534) |
| 2004 | 0.0324 | (0.1152) | (0.0827) | (0.0301) | 0.0495 | 0.0194 | 0.0113 | 0.0788 | 0.0901 | (0.0919) | 0.1040 | 0.0121 |
| 2005 | 0.0562 | (0.1659) | (0.1097) | (0.0209) | 0.0315 | 0.0106 | 0.0286 | 0.0674 | 0.0960 | 0.1384 | (0.1060) | 0.0324 |
| 2006 | (0.0186) | (0.0863) | (0.1049) | (0.0158) | 0.0241 | 0.0082 | 0.0328 | 0.0726 | 0.1054 | (0.0726) | 0.0938 | 0.0212 |
| 2007 | (0.0113) | (0.0907) | (0.1020) | (0.0193) | 0.0214 | 0.0021 | 0.0488 | 0.0606 | 0.1094 | (0.0160) | 0.0290 | 0.0130 |
| 2008 | (0.0241) | (0.0801) | (0.1043) | (0.0276) | 0.0236 | (0.0040) | 0.0332 | 0.0819 | 0.1150 | 0.0104 | 0.0098 | 0.0201 |
| 2009 | (0.0954) | 0.0663 | (0.0292) | (0.0743) | 0.0746 | 0.0003 | (0.0003) | 0.0946 | 0.0943 | (0.0217) | 0.0301 | 0.0084 |
| 2010 | (0.0987) | 0.0982 | (0.0005) | (0.0733) | 0.0705 | (0.0028) | 0.0112 | 0.0836 | 0.0947 | (0.0060) | 0.0264 | 0.0205 |
| 2011 | (0.0987) | 0.0982 | (0.0005) | (0.0503) | 0.0466 | (0.0037) | 0.0114 | 0.0875 | 0.0989 | (0.0095) | 0.0357 | 0.0262 |
| 2012 | (0.0987) | 0.0982 | (0.0005) | (0.0503) | 0.0466 | (0.0037) | 0.0043 | 0.0902 | 0.0945 | (0.0167) | 0.0370 | 0.0203 |
| 2013 | (0.0987) | 0.0982 | (0.0005) | (0.0503) | 0.0466 | (0.0037) | 0.0043 | 0.0902 | 0.0945 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A6 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of Y, $g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{\text {- }}$ ipRI | bop | $\Delta \mathrm{d}$ | $\mathrm{spRI}^{-\mathrm{i}_{\text {PRI }}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{\text {-ipRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5. Mexico |  |  | 5. Germany |  |  | 5. Switzerland |  |  | 6. Paraguay |  |  |
| 1990 | (0.0275) | (0.0198) | (0.0472) | (0.0183) | 0.0419 | 0.0236 | 0.0046 | 0.0012 | 0.0057 | 0.0325 | (0.0773) | (0.0448) |
| 1991 | 0.0316 | (0.0923) | (0.0607) | (0.0245) | 0.0122 | (0.0123) | (0.0112) | 0.0269 | 0.0157 | (0.0017) | (0.0722) | (0.0740) |
| 1992 | 0.0451 | (0.1278) | (0.0827) | (0.0268) | 0.0190 | (0.0079) | (0.0080) | 0.0474 | 0.0394 | 0.0089 | (0.1232) | (0.1142) |
| 1993 | 0.0056 | (0.0790) | (0.0735) | (0.0281) | 0.0301 | 0.0020 | (0.0271) | 0.0830 | 0.0559 | 0.0129 | (0.1304) | (0.1176) |
| 1994 | (0.0003) | (0.0843) | (0.0846) | (0.0149) | 0.0181 | 0.0032 | (0.0140) | 0.0656 | 0.0516 | 0.0074 | (0.2079) | (0.2005) |
| 1995 | (0.0059) | (0.0152) | (0.0211) | (0.0192) | 0.0161 | (0.0031) | (0.0155) | 0.0732 | 0.0576 | 0.0050 | (0.1772) | (0.1722) |
| 1996 | (0.0024) | (0.0203) | (0.0227) | (0.0227) | 0.0269 | 0.0042 | (0.0132) | 0.0706 | 0.0574 | 0.0006 | (0.1726) | (0.1721) |
| 1997 | (0.0117) | (0.0233) | (0.0350) | (0.0147) | 0.0206 | 0.0059 | (0.0144) | 0.0741 | 0.0597 | (0.0016) | (0.1667) | (0.1683) |
| 1998 | (0.0157) | (0.0417) | (0.0574) | (0.0103) | 0.0140 | 0.0037 | 0.0010 | 0.0530 | 0.0540 | (0.0026) | (0.0871) | (0.0897) |
| 1999 | (0.0168) | (0.0286) | (0.0454) | (0.0156) | 0.0133 | (0.0023) | (0.0067) | 0.0689 | 0.0622 | (0.0309) | (0.0722) | (0.1031) |
| 2000 | (0.0136) | (0.0339) | (0.0475) | (0.0143) | (0.0185) | (0.0328) | (0.0102) | 0.0757 | 0.0655 | (0.0435) | (0.0583) | (0.1018) |
| 2001 | (0.0078) | (0.0390) | (0.0468) | (0.0336) | 0.0418 | 0.0082 | 0.0036 | 0.0520 | 0.0556 | (0.0095) | (0.0910) | (0.1005) |
| 2002 | (0.0191) | (0.0199) | (0.0390) | (0.0430) | 0.0770 | 0.0339 | (0.0103) | 0.0838 | 0.0735 | (0.0363) | 0.0060 | (0.0303) |
| 2003 | (0.0107) | (0.0228) | (0.0335) | (0.0479) | 0.0811 | 0.0332 | (0.0076) | 0.0815 | 0.0739 | (0.0073) | (0.0141) | (0.0214) |
| 2004 | (0.0094) | 0.0095 | 0.0001 | (0.0458) | 0.1149 | 0.0691 | (0.0068) | 0.0842 | 0.0774 | 0.0187 | (0.0403) | (0.0216) |
| 2005 | (0.0073) | (0.0269) | (0.0342) | (0.0412) | 0.1139 | 0.0726 | (0.0010) | 0.0767 | 0.0757 | 0.0080 | (0.0605) | (0.0526) |
| 2006 | (0.0157) | (0.0191) | (0.0347) | (0.0214) | 0.1073 | 0.0859 | 0.0054 | 0.0853 | 0.0907 | 0.0072 | (0.0656) | (0.0585) |
| 2007 | (0.0169) | (0.0199) | (0.0367) | (0.0000) | 0.0970 | 0.0970 | (0.0180) | 0.1335 | 0.1156 | 0.0127 | (0.0566) | (0.0440) |
| 2008 | (0.0143) | (0.0265) | (0.0408) | (0.0027) | 0.0882 | 0.0855 | (0.0180) | 0.1452 | 0.1272 | 0.0270 | (0.0775) | (0.0505) |
| 2009 | (0.0206) | (0.0126) | (0.0332) | (0.0357) | 0.1189 | 0.0833 | 0.0079 | 0.1159 | 0.1238 | 0.0013 | 0.0685 | 0.0698 |
| 2010 | (0.0255) | (0.0023) | (0.0278) | (0.0499) | 0.1365 | 0.0866 | 0.0041 | 0.1235 | 0.1275 | 0.0143 | 0.0202 | 0.0345 |
| 2011 | (0.0243) | 0.0238 | (0.0005) | (0.0015) | 0.0876 | 0.0861 | 0.0040 | 0.1249 | 0.1289 | 0.0107 | (0.0078) | 0.0030 |
| 2012 | (0.0243) | 0.0238 | (0.0005) | (0.0015) | 0.0876 | 0.0861 | 0.0040 | 0.1249 | 0.1289 | 0.0099 | (0.0133) | (0.0034) |
| 2013 | (0.0243) | 0.0238 | (0.0005) | (0.0015) | 0.0876 | 0.0861 | 0.0040 | 0.1249 | 0.1289 | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | $\begin{array}{\|l\|} \hline \text { Infla.rate, } \mathrm{HA} \quad \mathrm{~g}^{*} \\ \hline \text { 5. Switzerland } \\ \hline \end{array}$ |  | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5. Mexico |  |  | 5. Germany |  |  |  |  |  | 6. Paraguay |  |  |
| 1990 | 0.3745 | 0.1783 | 0.1291 | 0.0537 | 0.0501 | 0.0344 | 0.1102 | 0.0859 | 0.0629 | 0.0896 | 0.0801 | 0.0401 |
| 1991 | 0.2806 | 0.1630 | 0.1177 | 0.0381 | 0.0496 | 0.0372 | 0.0733 | 0.0696 | 0.0478 | 0.1168 | 0.0980 | 0.0599 |
| 1992 | 0.1267 | 0.1446 | 0.1089 | 0.0370 | 0.0467 | 0.0351 | 0.0641 | 0.0547 | 0.0370 | 0.1083 | 0.0933 | 0.0548 |
| 1993 | 0.1035 | 0.1198 | 0.0869 | 0.0324 | 0.0391 | 0.0282 | 0.0568 | 0.0420 | 0.0291 | 0.1149 | 0.0945 | 0.0564 |
| 1994 | 0.0943 | 0.1158 | 0.0865 | 0.0408 | 0.0420 | 0.0352 | 0.0643 | 0.0460 | 0.0335 | 0.1271 | 0.0991 | 0.0583 |
| 1995 | 0.1127 | 0.1059 | 0.0790 | 0.0399 | 0.0429 | 0.0358 | 0.0701 | 0.0602 | 0.0320 | 0.1220 | 0.0990 | 0.0592 |
| 1996 | 0.1654 | 0.1329 | 0.0953 | 0.0366 | 0.0372 | 0.0308 | 0.0782 | 0.0492 | 0.0360 | 0.1240 | 0.0904 | 0.0583 |
| 1997 | 0.1882 | 0.1450 | 0.1044 | 0.0360 | 0.0371 | 0.0305 | 0.1002 | 0.0421 | 0.0425 | 0.1112 | 0.0847 | 0.0539 |
| 1998 | 0.1119 | 0.1269 | 0.0953 | 0.0375 | 0.0388 | 0.0327 | 0.0841 | 0.0499 | 0.0383 | 0.0944 | 0.0735 | 0.0451 |
| 1999 | 0.1076 | 0.1173 | 0.0879 | 0.0253 | 0.0298 | 0.0248 | 0.0772 | 0.0444 | 0.0341 | 0.0833 | 0.0660 | 0.0374 |
| 2000 | 0.1005 | 0.1177 | 0.0851 | 0.0253 | 0.0366 | 0.0307 | 0.0827 | 0.0470 | 0.0341 | 0.0734 | 0.0497 | 0.0240 |
| 2001 | 0.0723 | 0.0911 | 0.0691 | 0.0183 | 0.0282 | 0.0173 | 0.0650 | 0.0454 | 0.0315 | 0.0767 | 0.0537 | 0.0278 |
| 2002 | 0.0688 | 0.0857 | 0.0649 | 0.0236 | 0.0216 | 0.0172 | 0.0590 | 0.0379 | 0.0254 | 0.0704 | 0.0455 | 0.0213 |
| 2003 | 0.0903 | 0.0984 | 0.0745 | 0.0236 | 0.0192 | 0.0163 | 0.0498 | 0.0351 | 0.0223 | 0.0939 | 0.0575 | 0.0317 |
| 2004 | 0.1458 | 0.1061 | 0.0740 | 0.0246 | 0.0131 | 0.0112 | 0.0561 | 0.0355 | 0.0236 | 0.1063 | 0.0657 | 0.0388 |
| 2005 | 0.0920 | 0.0982 | 0.0725 | 0.0262 | 0.0119 | 0.0109 | 0.0573 | 0.0365 | 0.0242 | 0.1054 | 0.0684 | 0.0415 |
| 2006 | 0.1048 | 0.1036 | 0.0740 | 0.0323 | 0.0125 | 0.0122 | 0.0787 | 0.0395 | 0.0260 | 0.1031 | 0.0685 | 0.0405 |
| 2007 | 0.1005 | 0.1012 | 0.0716 | 0.0449 | 0.0167 | 0.0160 | 0.1007 | 0.0388 | 0.0249 | 0.1078 | 0.0596 | 0.0348 |
| 2008 | 0.0922 | 0.0978 | 0.0688 | 0.0415 | 0.0171 | 0.0170 | 0.0903 | 0.0371 | 0.0205 | 0.1154 | 0.0577 | 0.0335 |
| 2009 | 0.0681 | 0.0812 | 0.0573 | 0.0335 | 0.0069 | 0.0084 | 0.0665 | 0.0286 | 0.0168 | 0.0888 | 0.0341 | 0.0138 |
| 2010 | 0.0709 | 0.0802 | 0.0560 | 0.0329 | 0.0101 | 0.0108 | 0.0724 | 0.0281 | 0.0173 | 0.0805 | 0.0512 | 0.0302 |
| 2011 | 0.0777 | 0.0738 | 0.0499 | 0.0370 | 0.0126 | 0.0144 | 0.0774 | 0.0295 | 0.0180 | 0.0991 | 0.0521 | 0.0308 |
| 2012 | 0.0846 | 0.0655 | 0.0535 | 0.0359 | 0.0106 | 0.0120 | 0.0908 | 0.0276 | 0.0206 | 0.2882 | 0.1622 | 0.0971 |
| 2013 | 0.0776 | 0.0615 | 0.0502 | 0.0312 | 0.0108 | 0.0107 | 0.0877 | 0.0269 | 0.0200 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A7 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 6. Bangradesh |  |  | 6. Greece |  |  | 6. the U K |  |  | 7. Peru |  |  |
| 1990 | (0.0084) | (0.0502) | (0.0586) | (0.1517) | 0.0368 | (0.1149) | 0.0082 | (0.0368) | (0.0286) | (0.0245) | 0.0214 | (0.0031) |
| 1991 | (0.0047) | (0.0326) | (0.0373) | (0.1202) | 0.0142 | (0.1060) | (0.0112) | (0.0017) | (0.0130) | (0.0246) | (0.0326) | (0.0573) |
| 1992 | (0.0103) | (0.0148) | (0.0251) | (0.0799) | (0.0219) | (0.1018) | (0.0569) | 0.0473 | (0.0096) | (0.0411) | (0.0185) | (0.0595) |
| 1993 | (0.0089) | (0.0174) | (0.0262) | (0.1266) | 0.0369 | (0.0898) | (0.0731) | 0.0628 | (0.0103) | (0.0331) | (0.0408) | (0.0739) |
| 1994 | 0.0012 | (0.0201) | (0.0189) | (0.2336) | 0.1523 | (0.0813) | (0.0586) | 0.0631 | 0.0044 | 0.0240 | (0.0784) | (0.0545) |
| 1995 | (0.0047) | (0.0326) | (0.0374) | (0.1312) | 0.0856 | (0.0456) | (0.0612) | 0.0520 | (0.0092) | (0.0377) | (0.0393) | (0.0770) |
| 1996 | (0.0013) | (0.0501) | (0.0514) | (0.1066) | 0.0496 | (0.0570) | (0.0406) | 0.0334 | (0.0071) | (0.0161) | (0.0511) | (0.0672) |
| 1997 | (0.0084) | (0.0219) | (0.0303) | (0.0742) | 0.0287 | (0.0455) | (0.0221) | 0.0249 | 0.0028 | (0.0089) | (0.0508) | (0.0597) |
| 1998 | (0.0042) | (0.0143) | (0.0185) | (0.0579) | 0.0025 | (0.0553) | 0.0063 | (0.0042) | 0.0020 | (0.0126) | (0.0573) | (0.0699) |
| 1999 | (0.0051) | (0.0169) | (0.0220) | (0.0493) | (0.0214) | (0.0708) | 0.0131 | (0.0347) | (0.0216) | (0.0350) | (0.0004) | (0.0355) |
| 2000 | (0.0066) | (0.0112) | (0.0178) | (0.0636) | (0.0695) | (0.1331) | 0.0167 | (0.0446) | (0.0279) | (0.0311) | 0.0008 | (0.0304) |
| 2001 | (0.0079) | (0.0239) | (0.0318) | (0.0349) | (0.1032) | (0.1381) | 0.0123 | (0.0362) | (0.0239) | (0.0312) | 0.0036 | (0.0276) |
| 2002 | (0.0021) | (0.0001) | (0.0022) | (0.0360) | (0.1100) | (0.1460) | (0.0173) | 0.0015 | (0.0157) | (0.0238) | 0.0057 | (0.0182) |
| 2003 | (0.0013) | (0.0020) | (0.0034) | (0.0413) | (0.0996) | (0.1409) | (0.0318) | 0.0200 | (0.0118) | (0.0195) | 0.0116 | (0.0079) |
| 2004 | (0.0080) | 0.0071 | (0.0009) | (0.0602) | (0.0575) | (0.1177) | (0.0303) | 0.0157 | (0.0147) | (0.0139) | 0.0473 | 0.0334 |
| 2005 | (0.0123) | (0.0026) | (0.0149) | (0.0378) | (0.0800) | (0.1179) | (0.0422) | 0.0221 | (0.0201) | (0.0078) | 0.0672 | 0.0594 |
| 2006 | (0.0158) | 0.0188 | 0.0030 | (0.0483) | (0.0948) | (0.1431) | (0.0216) | (0.0077) | (0.0293) | 0.0158 | 0.0751 | 0.0909 |
| 2007 | (0.0147) | 0.0206 | 0.0060 | (0.0565) | (0.1225) | (0.1790) | (0.0217) | 0.0011 | (0.0205) | 0.0204 | 0.0465 | 0.0669 |
| 2008 | (0.0105) | 0.0155 | 0.0050 | (0.0887) | (0.1057) | (0.1944) | (0.0427) | 0.0359 | (0.0068) | 0.0245 | (0.0216) | 0.0029 |
| 2009 | (0.0045) | 0.0261 | 0.0216 | (0.1592) | 0.0065 | (0.1526) | (0.1118) | 0.1049 | (0.0069) | 0.0217 | 0.0135 | 0.0351 |
| 2010 | (0.0127) | (0.0024) | (0.0151) | (0.1199) | (0.0127) | (0.1325) | (0.0998) | 0.0850 | (0.0147) | 0.0077 | 0.0210 | 0.0287 |
| 2011 | (0.0127) | (0.0024) | (0.0151) | (0.1210) | 0.0003 | (0.1207) | (0.0770) | 0.0768 | (0.0002) | 0.0069 | (0.0308) | (0.0240) |
| 2012 | (0.0127) | (0.0024) | (0.0151) | (0.1210) | 0.0003 | (0.1207) | (0.0608) | 0.0335 | (0.0273) | 0.0063 | 0.0140 | 0.0203 |
| 2013 | (0.0127) | (0.0024) | (0.0151) | (0.1210) | 0.0003 | (0.1207) | (0.0608) | 0.0335 | (0.0273) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 6. Bangradesh |  |  | 6. Greece |  |  | 6. the U K |  |  | 7. Peru |  |  |
| 1990 | 0.1125 | 0.0764 | 0.0407 | 0.1048 | 0.0668 | 0.0498 | 0.1247 | 0.0478 | 0.0405 | 0.6217 | 0.4999 | 0.0199 |
| 1991 | 0.0858 | 0.0787 | 0.0443 | 0.1001 | 0.0724 | 0.0539 | 0.1422 | 0.0294 | 0.0236 | 0.0693 | 0.0628 | 0.0368 |
| 1992 | 0.0798 | 0.0706 | 0.0390 | 0.1118 | 0.0677 | 0.0512 | 0.1561 | 0.0189 | 0.0137 | 0.1157 | 0.0746 | 0.0460 |
| 1993 | 0.0754 | 0.0424 | 0.0141 | 0.1223 | 0.0591 | 0.0443 | 0.1570 | 0.0184 | 0.0129 | 0.1521 | 0.0944 | 0.0709 |
| 1994 | 0.0734 | 0.0563 | 0.0249 | 0.1259 | 0.0555 | 0.0423 | 0.1402 | 0.0184 | 0.0133 | 0.1264 | 0.1109 | 0.0835 |
| 1995 | 0.0948 | 0.0545 | 0.0247 | 0.0781 | 0.0479 | 0.0213 | 0.1255 | 0.0381 | 0.0309 | 0.1025 | 0.1316 | 0.0879 |
| 1996 | 0.0898 | 0.0728 | 0.0401 | 0.1210 | 0.0488 | 0.0346 | 0.1255 | 0.0360 | 0.0290 | 0.1080 | 0.1024 | 0.0768 |
| 1997 | 0.0683 | 0.0778 | 0.0439 | 0.0941 | 0.0996 | 0.0825 | 0.1109 | 0.0369 | 0.0289 | 0.0879 | 0.1092 | 0.0768 |
| 1998 | 0.0626 | 0.0789 | 0.0451 | 0.0883 | 0.0991 | 0.0837 | 0.1156 | 0.0354 | 0.0288 | 0.0833 | 0.0959 | 0.0706 |
| 1999 | 0.0636 | 0.0791 | 0.0483 | 0.0858 | 0.1041 | 0.0871 | 0.1245 | 0.0423 | 0.0342 | 0.0710 | 0.0766 | 0.0538 |
| 2000 | 0.0678 | 0.0554 | 0.0324 | 0.1247 | 0.0674 | 0.0490 | 0.1324 | 0.0403 | 0.0321 | 0.0677 | 0.0685 | 0.0475 |
| 2001 | 0.0680 | 0.0296 | 0.0093 | 0.0119 | 0.0315 | 0.0257 | 0.1341 | 0.0341 | 0.0255 | 0.0651 | 0.0575 | 0.0383 |
| 2002 | 0.0478 | 0.0256 | 0.0067 | 0.0122 | 0.0325 | 0.0275 | 0.1375 | 0.0259 | 0.0183 | 0.0598 | 0.0557 | 0.0374 |
| 2003 | 0.0703 | 0.0665 | 0.0441 | 0.0170 | 0.0368 | 0.0317 | 0.1357 | 0.0240 | 0.0164 | 0.0568 | 0.0543 | 0.0372 |
| 2004 | 0.0708 | 0.0694 | 0.0472 | 0.0200 | 0.0203 | 0.0171 | 0.1368 | 0.0254 | 0.0171 | 0.0606 | 0.0503 | 0.0340 |
| 2005 | 0.0726 | 0.0779 | 0.0553 | 0.0215 | 0.0198 | 0.0164 | 0.1434 | 0.0242 | 0.0156 | 0.0751 | 0.0502 | 0.0336 |
| 2006 | 0.0711 | 0.0694 | 0.0482 | 0.0201 | 0.0258 | 0.0219 | 0.1397 | 0.0344 | 0.0240 | 0.1508 | 0.0649 | 0.0419 |
| 2007 | 0.0724 | 0.0684 | 0.0479 | 0.0222 | 0.0300 | 0.0239 | 0.1266 | 0.0344 | 0.0241 | 0.1657 | 0.0802 | 0.0531 |
| 2008 | 0.0745 | 0.0692 | 0.0490 | 0.0306 | 0.0282 | 0.0219 | 0.1183 | 0.0207 | 0.0122 | 0.1248 | 0.0951 | 0.0689 |
| 2009 | 0.0725 | 0.0598 | 0.0410 | 0.0340 | 0.0185 | 0.0126 | 0.0581 | 0.0088 | 0.0021 | 0.0742 | 0.0591 | 0.0422 |
| 2010 | 0.0737 | 0.0717 | 0.0520 | 0.0304 | 0.0165 | 0.0121 | 0.1142 | 0.0173 | 0.0084 | 0.1216 | 0.0831 | 0.0573 |
| 2011 | 0.0810 | 0.0610 | 0.0553 | 0.0284 | 0.0135 | 0.0098 | 0.0332 | 0.0154 | 0.0022 | 0.1557 | 0.1147 | 0.0794 |
| 2012 | 0.0730 | 0.0575 | 0.0522 | 0.0255 | 0.0052 | 0.0039 | 0.0978 | 0.0216 | 0.0080 | 0.1278 | 0.0925 | 0.0570 |
| 2013 | 0.0664 | 0.0543 | 0.0493 | 0.0267 | 0.0052 | 0.0041 | 0.1480 | 0.0190 | 0.0106 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A8 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of Y, $g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{spRI}^{-1 \mathrm{ipRI}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 7. China |  |  | 7. Ireland |  |  | 1. Bulgaria |  |  | 8. Iran |  |  |
| 1990 | (0.0080) | 0.0357 | 0.0278 | (0.0195) | (0.0481) | (0.0676) | 0.0000 | 0.0000 | 0.0000 | (0.0200) | (0.1070) | (0.1270) |
| 1991 | (0.0111) | 0.0401 | 0.0290 | (0.0094) | (0.0463) | (0.0557) | 0.0000 | 0.0000 | 0.0000 | (0.0248) | (0.1086) | (0.1335) |
| 1992 | (0.0100) | 0.0207 | 0.0107 | (0.0263) | (0.0085) | (0.0347) | 0.0000 | 0.0000 | 0.0000 | (0.0125) | 0.0092 | (0.0033) |
| 1993 | (0.0085) | (0.0112) | (0.0198) | (0.0091) | 0.0070 | (0.0021) | 0.0000 | 0.0000 | 0.0000 | (0.0077) | 0.0359 | 0.0282 |
| 1994 | (0.0123) | 0.0259 | 0.0136 | (0.0104) | 0.0053 | (0.0051) | 0.0000 | 0.0000 | 0.0000 | 0.0027 | 0.1989 | 0.2016 |
| 1995 | (0.0100) | 0.0271 | 0.0171 | (0.0070) | 0.0086 | 0.0016 | (0.0505) | 0.0035 | (0.0470) | 0.0015 | 0.0860 | 0.0874 |
| 1996 | (0.0076) | 0.0252 | 0.0176 | 0.0025 | 0.0015 | 0.0040 | (0.0179) | 0.0321 | 0.0142 | 0.0022 | 0.0557 | 0.0579 |
| 1997 | (0.0074) | 0.0587 | 0.0513 | 0.0062 | 0.0012 | 0.0074 | 0.0225 | (0.0093) | 0.0133 | (0.0116) | 0.0336 | 0.0220 |
| 1998 | (0.0110) | 0.0627 | 0.0517 | 0.0227 | (0.0317) | (0.0089) | 0.0297 | (0.0524) | (0.0227) | (0.0586) | 0.0372 | (0.0214) |
| 1999 | (0.0196) | 0.0522 | 0.0326 | 0.0536 | (0.0530) | 0.0006 | 0.0163 | (0.0957) | (0.0794) | (0.0024) | 0.0737 | 0.0714 |
| 2000 | (0.0254) | 0.0498 | 0.0244 | 0.0461 | (0.0498) | (0.0037) | 0.0064 | (0.0938) | (0.0873) | (0.0076) | 0.0668 | 0.0591 |
| 2001 | (0.0233) | 0.0448 | 0.0215 | 0.0423 | (0.0406) | 0.0017 | 0.0208 | (0.1298) | (0.1090) | 0.0505 | (0.0291) | 0.0215 |
| 2002 | (0.0265) | 0.0524 | 0.0259 | 0.0264 | (0.0245) | 0.0018 | (0.0003) | (0.0673) | (0.0676) | 0.0472 | (0.0214) | 0.0258 |
| 2003 | (0.0218) | 0.0439 | 0.0221 | 0.0296 | (0.0148) | 0.0148 | 0.0082 | (0.1119) | (0.1037) | 0.0445 | (0.0453) | (0.0008) |
| 2004 | (0.0132) | 0.0389 | 0.0257 | 0.0383 | (0.0315) | 0.0067 | 0.0372 | (0.1488) | (0.1116) | 0.0137 | (0.0095) | 0.0042 |
| 2005 | (0.0124) | 0.0680 | 0.0556 | 0.0420 | (0.0652) | (0.0233) | 0.0696 | (0.2356) | (0.1660) | (0.0107) | 0.0978 | 0.0871 |
| 2006 | (0.0078) | 0.0855 | 0.0778 | 0.0590 | (0.0976) | (0.0386) | 0.0369 | (0.2656) | (0.2287) | (0.0351) | 0.1265 | 0.0914 |
| 2007 | 0.0059 | 0.0842 | 0.0902 | 0.0364 | (0.0927) | (0.0563) | 0.0390 | (0.2834) | (0.2445) | (0.0369) | 0.1573 | 0.1204 |
| 2008 | (0.0042) | 0.0848 | 0.0806 | (0.0381) | (0.0182) | (0.0563) | 0.0296 | (0.3160) | (0.2864) | (0.0545) | 0.1374 | 0.0829 |
| 2009 | (0.0226) | 0.0661 | 0.0436 | (0.1318) | 0.1169 | (0.0149) | (0.0022) | (0.1209) | (0.1231) | (0.0440) | 0.0852 | 0.0412 |
| 2010 | (0.0169) | 0.0560 | 0.0392 | (0.3226) | 0.3530 | 0.0304 | (0.0456) | (0.0042) | (0.0498) | (0.0140) | 0.0822 | 0.0682 |
| 2011 | (0.1140) | 0.1398 | 0.0259 | (0.1363) | 0.1659 | 0.0295 | (0.0456) | (0.0042) | (0.0498) | (0.0140) | 0.0822 | 0.0682 |
| 2012 | (0.1140) | 0.1398 | 0.0259 | (0.1363) | 0.1659 | 0.0295 | (0.0456) | (0.0042) | (0.0498) | (0.0140) | 0.0822 | 0.0682 |
| 2013 | (0.1140) | 0.1398 | 0.0259 | (0.1363) | 0.1659 | 0.0295 | (0.0456) | (0.0042) | (0.0498) | (0.0140) | 0.0822 | 0.0682 |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 7. China |  |  | 7. Ireland |  |  | 1. Bulgaria |  |  | 8. Iran |  |  |
| 1990 | 0.2116 | 0.1676 | 0.0986 | 0.0701 | 0.0802 | 0.0716 |  |  |  | 0.0837 | 0.1313 | 0.0846 |
| 1991 | 0.1946 | 0.1575 | 0.0923 | 0.0479 | 0.0687 | 0.0554 |  |  |  | 0.1226 | 0.1747 | 0.1106 |
| 1992 | 0.1876 | 0.1595 | 0.0945 | 0.0413 | 0.0595 | 0.0451 |  |  |  | 0.1895 | 0.1651 | 0.1021 |
| 1993 | 0.2093 | 0.1875 | 0.1063 | 0.0552 | 0.0541 | 0.0444 |  |  |  | 0.1273 | 0.1021 | 0.0671 |
| 1994 | 0.2222 | 0.1825 | 0.1011 | 0.0536 | 0.0541 | 0.0446 |  |  |  | 0.2094 | 0.0743 | 0.0417 |
| 1995 | 0.1842 | 0.1525 | 0.0929 | 0.0801 | 0.0725 | 0.0484 | 0.4228 | 0.1736 | 0.1579 | 0.1426 | 0.1496 | 0.0574 |
| 1996 | 0.1771 | 0.1482 | 0.0900 | 0.0961 | 0.0756 | 0.0514 | 0.4449 | 0.1199 | 0.1140 | 0.2614 | 0.1653 | 0.1042 |
| 1997 | 0.1717 | 0.1337 | 0.0786 | 0.1374 | 0.0901 | 0.0556 | 2.2194 | 0.0304 | 0.0340 | 0.2142 | 0.1639 | 0.1031 |
| 1998 | 0.1530 | 0.1217 | 0.0721 | 0.1446 | 0.1006 | 0.0588 | 0.7024 | 0.0882 | 0.0876 | 0.1400 | 0.1256 | 0.0863 |
| 1999 | 0.1367 | 0.1155 | 0.0706 | 0.0293 | 0.0325 | 0.0146 | 0.7194 | 0.0877 | 0.0809 | 0.1828 | 0.1145 | 0.0742 |
| 2000 | 0.1251 | 0.1130 | 0.0674 | 0.0442 | 0.0425 | 0.0166 | 0.4783 | 0.0948 | 0.0872 | 0.2203 | 0.1425 | 0.0919 |
| 2001 | 0.1254 | 0.1114 | 0.0675 | 0.0382 | 0.0437 | 0.0147 | 0.3516 | 0.1054 | 0.0954 | 0.2115 | 0.1434 | 0.1032 |
| 2002 | 0.1269 | 0.1112 | 0.0659 | 0.0437 | 0.0465 | 0.0163 | 0.4387 | 0.0539 | 0.0501 | 0.2365 | 0.1737 | 0.1089 |
| 2003 | 0.1350 | 0.1184 | 0.0670 | 0.0440 | 0.0452 | 0.0158 | 0.3630 | 0.0767 | 0.0675 | 0.2255 | 0.1842 | 0.1128 |
| 2004 | 0.1464 | 0.1258 | 0.0679 | 0.0439 | 0.0479 | 0.0158 | 0.2186 | 0.0995 | 0.0922 | 0.2150 | 0.1754 | 0.1080 |
| 2005 | 0.1512 | 0.1209 | 0.0633 | 0.0580 | 0.0561 | 0.0206 | 0.2194 | 0.1142 | 0.1015 | 0.2146 | 0.1387 | 0.0831 |
| 2006 | 0.1567 | 0.1187 | 0.0603 | 0.0576 | 0.0581 | 0.0228 | 0.1909 | 0.1380 | 0.1205 | 0.2138 | 0.1378 | 0.0816 |
| 2007 | (1.3208) | 7.0324 | 1.3443 | 0.0522 | 0.0563 | 0.0258 | 0.2086 | 0.1269 | 0.1059 | 0.2514 | 0.1491 | 0.0823 |
| 2008 | (4.2659) | 1.0553 | 0.5332 | 0.0273 | 0.0428 | 0.0216 | 0.1051 | 0.1579 | 0.1448 | 0.2220 | 0.1498 | 0.0856 |
| 2009 | 1.3797 | 0.5584 | 0.2644 | 0.0189 | 0.0317 | 0.0135 | 0.0668 | 0.0987 | 0.0948 | 0.1802 | 0.1438 | 0.0842 |
| 2010 | 0.6435 | 0.3766 | 0.1772 | 0.0161 | 0.0256 | 0.0089 | 0.0712 | 0.0735 | 0.0721 | 0.2001 | 0.1494 | 0.0810 |
| 2011 | 0.4430 | 0.3043 | 0.1400 | 0.0238 | 0.0292 | 0.0105 | 0.0584 | 0.0707 | 0.0632 | 0.1830 | 0.1274 | 0.0763 |
| 2012 | 0.3162 | 0.2323 | 0.1091 | 0.0302 | 0.0265 | 0.0095 | 0.0528 | 0.0660 | 0.0590 | 0.1575 | 0.1130 | 0.0677 |
| 2013 | 0.2437 | 0.1885 | 0.0885 | 0.0504 | 0.0250 | 0.0155 | 0.0482 | 0.0619 | 0.0554 | 0.1382 | 0.1015 | 0.0608 |

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

Table A9 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}^{\text {P }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8. India |  |  | 8. Italy |  |  | 2. Czech Republic |  |  | 9. Kazakhstan |  |  |
| 1990 | (0.0850) | 0.0544 | (0.0305) | (0.1231) | 0.1023 | (0.0209) |  |  |  |  |  |  |
| 1991 | (0.0609) | 0.0438 | (0.0171) | (0.1162) | 0.0901 | (0.0261) |  |  |  |  |  |  |
| 1992 | (0.0592) | 0.0335 | (0.0257) | (0.0961) | 0.0916 | (0.0045) |  |  |  |  |  |  |
| 1993 | (0.0776) | 0.0623 | (0.0153) | (0.0788) | 0.1080 | 0.0292 |  |  |  |  |  |  |
| 1994 | (0.0612) | 0.0438 | (0.0175) | (0.0746) | 0.1034 | 0.0288 |  |  |  |  |  |  |
| 1995 | (0.0623) | 0.0335 | (0.0288) | (0.0762) | 0.1056 | 0.0293 | 0.0050 | (0.0517) | (0.0466) | (0.0267) | (0.0321) | (0.0588) |
| 1996 | (0.0594) | 0.0334 | (0.0260) | (0.0813) | 0.1238 | 0.0425 | (0.0011) | (0.0741) | (0.0752) | (0.0489) | 0.0303 | (0.0186) |
| 1997 | (0.0345) | 0.0086 | (0.0259) | (0.0173) | 0.0538 | 0.0365 | (0.0094) | (0.0630) | (0.0724) | (0.0443) | (0.0011) | (0.0454) |
| 1998 | (0.0408) | 0.0098 | (0.0310) | (0.0260) | 0.0534 | 0.0274 | (0.0171) | (0.0174) | (0.0345) | (0.0485) | (0.0001) | (0.0485) |
| 1999 | (0.0359) | 0.0065 | (0.0294) | (0.0112) | 0.0291 | 0.0179 | (0.0153) | (0.0226) | (0.0379) | (0.0370) | 0.0717 | 0.0348 |
| 2000 | (0.0420) | 0.0203 | (0.0217) | (0.0176) | 0.0198 | 0.0023 | (0.0222) | (0.0335) | (0.0557) | (0.0014) | 0.1003 | 0.0989 |
| 2001 | (0.0478) | 0.0286 | (0.0192) | (0.0487) | 0.0567 | 0.0080 | (0.0308) | (0.0317) | (0.0625) | (0.0046) | (0.0664) | (0.0710) |
| 2002 | (0.0514) | 0.0332 | (0.0182) | (0.0310) | 0.0340 | 0.0031 | (0.0210) | (0.0545) | (0.0756) | (0.0041) | (0.0510) | (0.0551) |
| 2003 | (0.0396) | 0.0186 | (0.0210) | (0.0151) | 0.0132 | (0.0019) | (0.0461) | (0.0257) | (0.0718) | (0.0115) | 0.0082 | (0.0033) |
| 2004 | (0.0361) | 0.0085 | (0.0276) | (0.0377) | 0.0377 | 0.0000 | (0.0368) | (0.0230) | (0.0598) | (0.0035) | 0.0255 | 0.0220 |
| 2005 | (0.0391) | (0.0034) | (0.0425) | (0.0481) | 0.0373 | (0.0108) | (0.0207) | 0.0063 | (0.0144) | 0.0068 | (0.0131) | (0.0064) |
| 2006 | (0.0275) | (0.0207) | (0.0482) | (0.0285) | 0.0075 | (0.0210) | (0.0199) | 0.0025 | (0.0175) | 0.0088 | (0.0199) | (0.0110) |
| 2007 | (0.0314) | (0.0227) | (0.0541) | (0.0254) | 0.0107 | (0.0147) | (0.0023) | (0.0203) | (0.0226) | (0.0190) | (0.0486) | (0.0676) |
| 2008 | (0.0681) | 0.0007 | (0.0673) | (0.0348) | 0.0140 | (0.0208) | (0.0322) | 0.0327 | 0.0005 | 0.0527 | 0.0090 | 0.0616 |
| 2009 | (0.0794) | 0.0076 | (0.0718) | (0.0576) | 0.0396 | (0.0181) | (0.0684) | 0.0644 | (0.0040) | (0.0155) | (0.0180) | (0.0336) |
| 2010 | (0.0595) | 0.0048 | (0.0547) | (0.0501) | 0.0151 | (0.0350) | (0.0608) | 0.0407 | (0.0201) | (0.0082) | 0.0355 | 0.0273 |
| 2011 | (0.0544) | (0.0125) | (0.0669) | (0.0464) | 0.0161 | (0.0303) | (0.0608) | 0.0407 | (0.0201) | (0.0017) | 0.1338 | 0.1320 |
| 2012 | (0.0544) | (0.0125) | (0.0669) | (0.0464) | 0.0161 | (0.0303) | (0.0608) | 0.0407 | (0.0201) | 0.0108 | (0.0466) | (0.0358) |
| 2013 | (0.0544) | (0.0125) | (0.0669) | (0.0464) | 0.0161 | (0.0303) | (0.0608) | 0.0407 | (0.0201) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | gy * | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA gy* |  | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8. India |  |  | 8. Italy |  |  | 2. Czech R | ublic |  | 9. Kazakhstan |  |  |
| 1990 | 0.0507 | 0.0748 | 0.0473 | 0.0743 | 0.0663 | 0.0578 |  |  |  |  |  |  |
| 1991 | 0.0522 | 0.0695 | 0.0440 | 0.0945 | 0.0567 | 0.0666 |  |  |  |  |  |  |
| 1992 | 0.0592 | 0.0815 | 0.0544 | 0.0695 | 0.0488 | 0.0426 |  |  |  |  |  |  |
| 1993 | 0.0626 | 0.0806 | 0.0533 | 0.0631 | 0.0358 | 0.0293 |  |  |  |  |  |  |
| 1994 | 0.0866 | 0.0967 | 0.0651 | 0.0642 | 0.0369 | 0.0311 |  |  |  |  |  |  |
| 1995 | 0.0496 | 0.0548 | 0.0274 | 0.0812 | 0.0543 | 0.0466 | 0.8259 | 0.2901 | 0.1885 | 0.0573 | 0.0525 | 0.0522 |
| 1996 | 0.0413 | 0.0600 | 0.0228 | 0.0692 | 0.0397 | 0.0345 | 0.4447 | 0.2357 | 0.1613 | 0.1067 | 0.0307 | 0.0401 |
| 1997 | 0.0439 | 0.0638 | 0.0272 | 0.0788 | 0.0377 | 0.0387 | 0.1922 | 0.1581 | 0.1221 | 0.1518 | 0.0327 | 0.0411 |
| 1998 | 0.0571 | 0.0560 | 0.0244 | 0.0666 | 0.0364 | 0.0340 | 0.1063 | 0.0923 | 0.0836 | 0.1921 | 0.0255 | 0.0334 |
| 1999 | 0.1045 | 0.1114 | 0.0777 | 0.0685 | 0.0284 | 0.0257 | 0.1684 | 0.1191 | 0.0969 | 0.1131 | 0.0279 | 0.0364 |
| 2000 | 0.0947 | 0.1020 | 0.0699 | 0.0724 | 0.0323 | 0.0296 | 0.1803 | 0.1283 | 0.0989 | 0.1753 | 0.0368 | 0.0385 |
| 2001 | 0.0891 | 0.0951 | 0.0664 | 0.0600 | 0.0353 | 0.0284 | 0.1509 | 0.1193 | 0.0913 | 0.1817 | 0.1192 | 0.1249 |
| 2002 | 0.1011 | 0.0987 | 0.0674 | 0.0539 | 0.0372 | 0.0272 | 0.0708 | 0.0863 | 0.0769 | 0.1534 | 0.1326 | 0.1027 |
| 2003 | 0.1269 | 0.1091 | 0.0717 | 0.0593 | 0.0337 | 0.0258 | 0.0808 | 0.0895 | 0.0763 | 0.1657 | 0.1274 | 0.0917 |
| 2004 | 0.1251 | 0.1147 | 0.0755 | 0.1521 | 0.0215 | 0.0454 | 0.0917 | 0.0893 | 0.0720 | 0.1897 | 0.1351 | 0.0934 |
| 2005 | 0.0885 | 0.0814 | 0.0531 | 0.0074 | 0.0480 | 0.0044 | 0.1048 | 0.0793 | 0.0591 | 0.2195 | 0.1750 | 0.1151 |
| 2006 | 0.0963 | 0.0917 | 0.0612 | 0.0551 | 0.0397 | 0.0290 | 0.1113 | 0.0828 | 0.0586 | 0.2506 | 0.2036 | 0.1234 |
| 2007 | 0.1011 | 0.0990 | 0.0667 | 0.0517 | 0.0381 | 0.0276 | 0.1138 | 0.0853 | 0.0581 | 0.2070 | 0.2021 | 0.1264 |
| 2008 | 0.1019 | 0.1047 | 0.0714 | 0.0548 | 0.0347 | 0.0247 | 0.0841 | 0.0668 | 0.0477 | 0.2372 | 0.1674 | 0.0950 |
| 2009 | 0.0951 | 0.0982 | 0.0670 | 0.0614 | 0.0211 | 0.0132 | 0.0556 | 0.0546 | 0.0412 | 0.1162 | 0.1176 | 0.0812 |
| 2010 | 0.1006 | 0.0980 | 0.0666 | 0.0662 | 0.0279 | 0.0196 | 0.0538 | 0.0563 | 0.0434 | 0.1685 | 0.1382 | 0.0855 |
| 2011 | 0.1024 | 0.1052 | 0.0720 | 0.0575 | 0.0256 | 0.0144 | 0.0539 | 0.0524 | 0.0437 | 0.2025 | 0.1182 | 0.0676 |
| 2012 | 0.1027 | 0.0912 | 0.0729 | 0.0465 | 0.0159 | 0.0083 | 0.0505 | 0.0498 | 0.0415 | 0.2000 | 0.1870 | 0.1063 |
| 2013 | 0.0910 | 0.0836 | 0.0668 | 0.0465 | 0.0159 | 0.0083 | 0.0476 | 0.0475 | 0.0395 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A10 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{\text {-ipRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 9. Indonesia |  |  | 9. Luxemburg |  |  | 3. Hungary |  |  | 10. Kuwait |  |  |
| 1990 | 0.0042 | (0.0495) | (0.0453) |  |  |  | (0.0146) | 0.0453 | 0.0307 | (0.2063) | 0.5228 | 0.3166 |
| 1991 | 0.0044 | (0.0484) | (0.0440) |  |  |  | (0.0266) | 0.0156 | (0.0110) | (0.1792) | (0.4976) | (0.6768) |
| 1992 | (0.0042) | (0.0182) | (0.0225) |  |  |  | (0.0340) | 0.0311 | (0.0029) | 0.1886 | (0.0496) | 0.1390 |
| 1993 | 0.0068 | (0.0159) | (0.0091) |  |  |  | (0.0752) | (0.0183) | (0.0935) | (0.1520) | 0.3658 | 0.2138 |
| 1994 | 0.0104 | (0.0275) | (0.0171) |  |  |  | (0.0691) | (0.0044) | (0.0735) | (0.1455) | 0.3831 | 0.2376 |
| 1995 | 0.0241 | (0.0705) | (0.0464) | 0.0182 | 0.2760 | 0.2942 | (0.0736) | 0.0731 | (0.0006) | (0.0844) | 0.3959 | 0.3115 |
| 1996 | 0.0126 | (0.0483) | (0.0357) | 0.1168 | 0.1606 | 0.2774 | (0.0377) | 0.0433 | 0.0056 | 0.1189 | 0.2058 | 0.3247 |
| 1997 | (0.0073) | (0.0275) | (0.0348) | 0.0349 | 0.1810 | 0.2159 | (0.0548) | 0.0673 | 0.0125 | 0.1253 | 0.2477 | 0.3730 |
| 1998 | (0.0328) | 0.0785 | 0.0457 | 0.0319 | 0.1669 | 0.1988 | (0.0763) | 0.0588 | (0.0175) | (0.1857) | 0.3547 | 0.1690 |
| 1999 | (0.0125) | 0.0176 | 0.0051 | 0.0669 | 0.1341 | 0.2010 | (0.0890) | 0.0558 | (0.0332) | 0.0690 | 0.1887 | 0.2578 |
| 2000 | (0.0429) | 0.0847 | 0.0418 | 0.0901 | 0.1281 | 0.2182 | (0.0477) | 0.0034 | (0.0443) | 0.1853 | 0.3083 | 0.4936 |
| 2001 | (0.0243) | 0.0728 | 0.0485 | 0.0764 | (0.0026) | 0.0737 | (0.0519) | 0.0369 | (0.0151) | 0.3281 | (0.0004) | 0.3277 |
| 2002 | (0.0139) | 0.0494 | 0.0355 | 0.0588 | (0.0310) | 0.0278 | (0.0892) | 0.0661 | (0.0231) | 0.1251 | 0.0593 | 0.1844 |
| 2003 | (0.0193) | 0.0576 | 0.0384 | 0.0366 | (0.0237) | 0.0129 | (0.0878) | 0.0402 | (0.0476) | 0.0964 | 0.1747 | 0.2711 |
| 2004 | (0.0144) | 0.0610 | 0.0466 | 0.0148 | 0.1109 | 0.1257 | (0.0779) | 0.0374 | (0.0405) | 0.0790 | 0.2866 | 0.3655 |
| 2005 | (0.0039) | (0.0041) | (0.0080) | 0.0296 | 0.0951 | 0.1247 | (0.0868) | 0.0643 | (0.0225) | 0.1137 | 0.3764 | 0.4901 |
| 2006 | (0.0108) | 0.0235 | 0.0127 | 0.0408 | 0.0510 | 0.0918 | (0.0919) | 0.0794 | (0.0125) | 0.3881 | 0.1853 | 0.5734 |
| 2007 | (0.0087) | 0.0080 | (0.0008) | 0.0585 | 0.0956 | 0.1541 | (0.0519) | 0.0650 | 0.0131 | 0.2377 | 0.2668 | 0.5045 |
| 2008 | (0.0194) | (0.0080) | (0.0274) | 0.0540 | 0.0500 | 0.1040 | (0.0484) | 0.0545 | 0.0061 | 0.3521 | 0.1767 | 0.5288 |
| 2009 | (0.0171) | 0.0095 | (0.0076) | 0.0135 | (0.0321) | (0.0185) | (0.0516) | 0.1116 | 0.0599 | 0.1285 | 0.2736 | 0.4021 |
| 2010 | (0.0068) | (0.0057) | (0.0124) | 0.0157 | (0.0101) | 0.0056 | (0.0636) | 0.1478 | 0.0842 | 0.2999 | 0.1705 | 0.4705 |
| 2011 | (0.0142) | (0.0016) | (0.0158) | 0.0205 | 0.0160 | 0.0365 | (0.0636) | 0.1478 | 0.0842 | 0.2700 | 0.3166 | 0.5866 |
| 2012 | (0.0142) | (0.0016) | (0.0158) | 0.0205 | 0.0160 | 0.0365 | (0.0636) | 0.1478 | 0.0842 | 0.0825 | 0.4727 | 0.5552 |
| 2013 | (0.0142) | (0.0016) | (0.0158) | 0.0205 | 0.0160 | 0.0365 | (0.0636) | 0.1478 | 0.0842 | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 9. Indonesia |  |  | 9. Luxemburg |  |  | 3. Hungary |  |  | 10. Kuwait |  |  |
| 1990 | 0.3725 | 0.2086 | 0.1111 |  |  |  | 0.1002 | 0.0556 | 0.0527 | 0.2525 | (0.0449) | (0.0708) |
| 1991 | 0.3070 | 0.1831 | 0.1005 |  |  |  | 0.0974 | 0.0434 | 0.0397 | 0.0719 | 0.2858 | 0.2748 |
| 1992 | 0.3301 | 0.1855 | 0.0828 |  |  |  | 0.1031 | 0.0506 | 0.0486 | (0.1144) | (0.1132) | 0.2650 |
| 1993 | 0.1795 | 0.1223 | 0.0726 |  |  |  | 0.2484 | 0.0477 | 0.0395 | 0.1296 | (0.0244) | (0.0461) |
| 1994 | 0.1684 | 0.1213 | 0.0725 |  |  |  | 0.1815 | 0.0608 | 0.0542 | (0.9880) | 0.0099 | (0.0764) |
| 1995 | 0.1688 | 0.1332 | 0.0809 | 0.0388 | 0.0166 | 0.0065 | 0.1048 | 0.0626 | 0.0502 | 0.3309 | (0.0391) | (0.0850) |
| 1996 | 0.1623 | 0.1232 | 0.0774 | 0.0464 | 0.0229 | 0.0106 | 0.1265 | 0.0535 | 0.0503 | 0.2696 | (0.0603) | (0.0555) |
| 1997 | 0.1779 | 0.1273 | 0.0769 | 0.0526 | 0.0402 | 0.0235 | 0.1304 | 0.0635 | 0.0585 | 0.3686 | (0.0862) | (0.1064) |
| 1998 | 0.1030 | 0.0715 | 0.0475 | 0.0580 | 0.0464 | 0.0292 | 0.1289 | 0.0783 | 0.0739 | 0.1637 | (0.0101) | (0.0629) |
| 1999 | 0.0625 | 0.0631 | 0.0440 | 0.0949 | 0.0656 | 0.0396 | 0.1231 | 0.0753 | 0.0711 | 0.1827 | (0.0096) | (0.0596) |
| 2000 | 0.1941 | 0.1456 | 0.0561 | 0.1131 | 0.0665 | 0.0404 | 0.1152 | 0.0868 | 0.0807 | 0.1657 | (0.0258) | (0.0611) |
| 2001 | 0.2481 | 0.1175 | 0.0692 | 0.0857 | 0.0953 | 0.0657 | 0.1210 | 0.0596 | 0.0567 | 0.2362 | (0.0093) | (0.0442) |
| 2002 | 0.1260 | 0.0836 | 0.0568 | 0.0797 | 0.1031 | 0.0717 | 0.1165 | 0.0686 | 0.0650 | (0.2930) | 0.0045 | (0.0302) |
| 2003 | 0.0829 | 0.0634 | 0.0443 | 0.0902 | 0.1118 | 0.0716 | 0.1755 | 0.0486 | 0.0442 | (0.2662) | 0.0066 | (0.0220) |
| 2004 | 0.0884 | 0.0642 | 0.0432 | 0.0815 | 0.0757 | 0.0478 | 0.1381 | 0.0555 | 0.0518 | (0.4154) | 0.0069 | (0.0183) |
| 2005 | 0.1328 | 0.1046 | 0.0746 | 0.0898 | 0.0856 | 0.0467 | 0.1447 | 0.0409 | 0.0375 | (1.8123) | 0.0029 | (0.0140) |
| 2006 | 0.1645 | 0.1060 | 0.0724 | 0.1007 | 0.1045 | 0.0500 | 0.1116 | 0.0783 | 0.0734 | 0.9920 | (0.0107) | (0.0187) |
| 2007 | 0.1569 | 0.1091 | 0.0760 | 0.1091 | 0.0941 | 0.0407 | 0.1018 | 0.0619 | 0.0576 | (0.5734) | 0.0084 | (0.0080) |
| 2008 | 0.2142 | 0.1412 | 0.0915 | 0.0895 | 0.0925 | 0.0426 | 0.0930 | 0.0611 | 0.0570 | (0.3214) | 0.0132 | (0.0049) |
| 2009 | 0.2101 | 0.1292 | 0.0808 | 0.0712 | 0.0983 | 0.0553 | 0.0901 | 0.0353 | 0.0336 | (0.1047) | 0.0159 | (0.0047) |
| 2010 | 0.1983 | 0.1383 | 0.0863 | 0.0711 | 0.1010 | 0.0445 | 0.0982 | 0.0290 | 0.0277 | 0.0784 | 0.0274 | 0.0034 |
| 2011 | 0.1951 | 0.1436 | 0.0875 | 0.0762 | 0.0925 | 0.0423 | 0.0873 | 0.0290 | 0.0258 | (2.8397) | 0.0031 | (0.0077) |
| 2012 | 0.1754 | 0.1229 | 0.0815 | 0.0740 | 0.0895 | 0.0436 | 0.0832 | 0.0282 | 0.0251 | (0.5667) | 0.0184 | (0.0092) |
| 2013 | 0.1505 | 0.1095 | 0.0726 | 0.0813 | 0.0805 | 0.0481 | 0.0795 | 0.0274 | 0.0244 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

Table A11 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-\mathrm{i}_{\mathrm{PRI}}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{spRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-\mathrm{i}_{\mathrm{PRI}}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10. Japan |  |  | 10. Netherlands |  |  | 4. Latvia |  |  | 11. Pakistan |  |  |
| 1990 | (0.0643) | 0.0789 | 0.0147 | (0.0487) | 0.0967 | 0.0480 |  |  |  | (0.0602) | 0.0474 | (0.0128) |
| 1991 | (0.0605) | 0.0885 | 0.0280 | (0.0297) | 0.0790 | 0.0493 |  |  |  | (0.0843) | 0.0931 | 0.0088 |
| 1992 | (0.0606) | 0.0978 | 0.0372 | (0.0365) | 0.0813 | 0.0448 |  |  |  | (0.0880) | 0.0643 | (0.0236) |
| 1993 | (0.0606) | 0.0959 | 0.0352 | (0.0101) | 0.0702 | 0.0601 |  |  |  | (0.0992) | 0.0393 | (0.0599) |
| 1994 | (0.0600) | 0.0905 | 0.0305 | (0.0053) | 0.0647 | 0.0594 |  |  |  | (0.0808) | 0.0529 | (0.0279) |
| 1995 | (0.0593) | 0.0822 | 0.0230 | (0.0388) | 0.1095 | 0.0707 | (0.0085) | (0.0107) | (0.0192) | (0.0737) | 0.0519 | (0.0218) |
| 1996 | (0.0583) | 0.0758 | 0.0175 | (0.0156) | 0.0789 | 0.0633 | (0.0156) | (0.0570) | (0.0726) | (0.0888) | 0.0348 | (0.0540) |
| 1997 | (0.0472) | 0.0784 | 0.0311 | (0.0167) | 0.0821 | 0.0654 | 0.0071 | (0.0819) | (0.0748) | (0.0868) | 0.0259 | (0.0609) |
| 1998 | (0.1434) | 0.1806 | 0.0372 | (0.0046) | 0.0719 | 0.0673 | 0.0015 | (0.1276) | (0.1262) | (0.0713) | 0.0497 | (0.0217) |
| 1999 | (0.0974) | 0.1305 | 0.0330 | (0.0169) | 0.0766 | 0.0596 | (0.0883) | (0.0258) | (0.1141) | (0.0764) | 0.0488 | (0.0276) |
| 2000 | (0.0989) | 0.1289 | 0.0299 | (0.0010) | 0.0876 | 0.0866 | (0.0700) | (0.0111) | (0.0810) | (0.0504) | 0.0224 | (0.0280) |
| 2001 | (0.0747) | 0.1030 | 0.0283 | 0.0056 | 0.0680 | 0.0735 | (0.0571) | (0.0461) | (0.1032) | (0.0416) | 0.0156 | (0.0261) |
| 2002 | (0.0962) | 0.1335 | 0.0373 | (0.0122) | 0.0960 | 0.0838 | (0.0588) | (0.0463) | (0.1050) | (0.0317) | 0.0366 | 0.0049 |
| 2003 | (0.0966) | 0.1387 | 0.0421 | (0.0248) | 0.1082 | 0.0834 | (0.0310) | (0.1124) | (0.1434) | (0.0320) | 0.0732 | 0.0412 |
| 2004 | (0.0739) | 0.1219 | 0.0481 | (0.0160) | 0.1287 | 0.1128 | (0.0096) | (0.1877) | (0.1974) | (0.0217) | 0.0577 | 0.0360 |
| 2005 | (0.0598) | 0.1064 | 0.0467 | 0.0012 | 0.1001 | 0.1013 | (0.0048) | (0.1691) | (0.1739) | (0.0356) | 0.0155 | (0.0201) |
| 2006 | (0.0453) | 0.0963 | 0.0509 | 0.0085 | 0.1086 | 0.1171 | 0.0197 | (0.2910) | (0.2713) | (0.0470) | (0.0199) | (0.0669) |
| 2007 | (0.0258) | 0.0881 | 0.0624 | 0.0075 | 0.1023 | 0.1097 | 0.0363 | (0.2945) | (0.2583) | (0.0464) | (0.0129) | (0.0593) |
| 2008 | (0.0501) | 0.0932 | 0.0431 | 0.0136 | 0.0554 | 0.0690 | (0.0249) | (0.1377) | (0.1626) | (0.0826) | (0.0172) | (0.0999) |
| 2009 | (0.1216) | 0.1579 | 0.0363 | (0.0500) | 0.1007 | 0.0507 | (0.0979) | 0.1662 | 0.0684 | (0.0529) | (0.0008) | (0.0537) |
| 2010 | (0.1082) | 0.1521 | 0.0439 | (0.0476) | 0.1240 | 0.0764 | (0.0801) | 0.0942 | 0.0141 | (0.0557) | 0.0330 | (0.0226) |
| 2011 | (0.1132) | 0.1346 | 0.0215 | (0.0446) | 0.1553 | 0.1108 | (0.0801) | 0.0942 | 0.0141 | (0.0720) | 0.0662 | (0.0058) |
| 2012 | (0.1132) | 0.1346 | 0.0215 | (0.0446) | 0.1553 | 0.1108 | (0.0801) | 0.0942 | 0.0141 | (0.0672) | 0.0317 | (0.0355) |
| 2013 | (0.1132) | 0.1346 | 0.0215 | (0.0446) | 0.1553 | 0.1108 | (0.0801) | 0.0942 | 0.0141 | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10. Japan |  |  | 10. Netherlands |  |  | 4. Latvia |  |  | 11. Pakistan |  |  |
| 1990 | 0.0755 | 0.0629 | 0.0472 | 0.0560 | 0.0417 | 0.0272 |  |  |  | 0.0925 | 0.0516 | 0.0180 |
| 1991 | 0.0748 | 0.0588 | 0.0441 | 0.0495 | 0.0398 | 0.0252 |  |  |  | 0.0884 | 0.0665 | 0.0319 |
| 1992 | 0.0612 | 0.0440 | 0.0341 | 0.0439 | 0.0376 | 0.0247 |  |  |  | 0.1064 | 0.0855 | 0.0484 |
| 1993 | 0.0451 | 0.0358 | 0.0294 | 0.0408 | 0.0328 | 0.0210 |  |  |  | 0.1254 | 0.0898 | 0.0508 |
| 1994 | 0.0374 | 0.0320 | 0.0269 | 0.0525 | 0.0358 | 0.0250 |  |  |  | 0.1019 | 0.0816 | 0.0468 |
| 1995 | 0.0339 | 0.0311 | 0.0265 | 0.0533 | 0.0354 | 0.0226 | 0.1221 | 0.0100 | 0.0193 | 0.1073 | 0.0726 | 0.0387 |
| 1996 | 0.0306 | 0.0294 | 0.0252 | 0.0514 | 0.0362 | 0.0235 | 0.1071 | 0.0234 | 0.0295 | 0.1282 | 0.0829 | 0.0470 |
| 1997 | 0.0330 | 0.0285 | 0.0242 | 0.0570 | 0.0369 | 0.0248 | 0.0757 | 0.0347 | 0.0371 | 0.1347 | 0.0799 | 0.0414 |
| 1998 | 0.0251 | 0.0171 | 0.0144 | 0.0751 | 0.0445 | 0.0271 | 0.0813 | 0.0488 | 0.0528 | 0.0944 | 0.0745 | 0.0418 |
| 1999 | 0.0235 | 0.0122 | 0.0092 | 0.0451 | 0.0338 | 0.0235 | 0.0755 | 0.0459 | 0.0466 | 0.1059 | 0.0594 | 0.0280 |
| 2000 | 0.0242 | 0.0153 | 0.0123 | 0.0487 | 0.0291 | 0.0194 | 0.0580 | 0.0470 | 0.0498 | 0.1135 | 0.0769 | 0.0450 |
| 2001 | 0.0263 | 0.0099 | 0.0076 | 0.0562 | 0.0315 | 0.0248 | 0.0508 | 0.0579 | 0.0559 | 0.1906 | 0.0533 | 0.0554 |
| 2002 | 0.0190 | 0.0027 | 0.0012 | 0.0414 | 0.0261 | 0.0175 | 0.0555 | 0.0570 | 0.0592 | 0.0952 | 0.0527 | 0.0293 |
| 2003 | 0.0134 | 0.0016 | 0.0005 | 0.0372 | 0.0240 | 0.0159 | 0.0581 | 0.0670 | 0.0678 | 0.0711 | 0.0358 | 0.0155 |
| 2004 | 0.0226 | 0.0031 | 0.0019 | 0.0374 | 0.0184 | 0.0109 | 0.0488 | 0.0915 | 0.0867 | 0.0873 | 0.0419 | 0.0213 |
| 2005 | 0.0222 | 0.0020 | 0.0011 | 0.0479 | 0.0259 | 0.0163 | 0.0496 | 0.0939 | 0.0939 | 0.1337 | 0.0621 | 0.0379 |
| 2006 | 0.0333 | 0.0010 | 0.0008 | 0.0549 | 0.0218 | 0.0150 | 0.0494 | 0.1228 | 0.1155 | 0.1599 | 0.0853 | 0.0566 |
| 2007 | 0.0231 | 0.0015 | 0.0010 | 0.0659 | 0.0277 | 0.0194 | 0.0506 | 0.1312 | 0.1236 | 0.1337 | 0.0864 | 0.0584 |
| 2008 | 0.0304 | 0.0045 | 0.0037 | 0.0685 | 0.0397 | 0.0290 | 0.0504 | 0.0982 | 0.0930 | 0.2056 | 0.0840 | 0.0521 |
| 2009 | 0.0308 | 0.0062 | 0.0055 | 0.0419 | 0.0321 | 0.0246 | 0.0594 | 0.0074 | 0.0107 | 0.2011 | 0.0533 | 0.0276 |
| 2010 | 0.0273 | 0.0093 | 0.0085 | 0.0415 | 0.0257 | 0.0190 | 0.0403 | 0.0253 | 0.0271 | 0.1052 | 0.0249 | 0.0054 |
| 2011 | 0.0317 | 0.0089 | 0.0081 | 0.0497 | 0.0209 | 0.0149 | 0.0331 | 0.0257 | 0.0234 | 3.8861 | (0.0029) | (0.0151) |
| 2012 | 0.0303 | 0.0089 | 0.0078 | 0.0466 | 0.0197 | 0.0146 | 0.0320 | 0.0251 | 0.0228 | 1.8734 | (0.0153) | (0.0216) |
| 2013 | 0.0300 | 0.0088 | 0.0078 | 0.0518 | 0.0188 | 0.0159 | 0.0310 | 0.0245 | 0.0222 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A12 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of Y, $g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11. Korea |  |  | 11. Portugal |  |  | 5. Poland |  |  | 12. Saudi Arabia |  |  |
| 1990 | (0.0075) | (0.0065) | (0.0140) | (0.0527) | (0.0869) | (0.1396) | (0.0513) | 0.1325 | 0.0811 | (0.0283) | 0.1586 | 0.1303 |
| 1991 | (0.0179) | (0.0166) | (0.0345) | (0.0684) | (0.0784) | (0.1467) | (0.0816) | 0.0601 | (0.0216) | (0.0302) | 0.0542 | 0.0240 |
| 1992 | (0.0053) | (0.0123) | (0.0176) | (0.0262) | (0.1116) | (0.1378) | (0.0443) | 0.0612 | 0.0169 | (0.0241) | 0.0661 | 0.0420 |
| 1993 | 0.0068 | (0.0078) | (0.0010) | (0.0892) | (0.0513) | (0.1406) | (0.0354) | 0.0461 | 0.0107 | (0.0350) | 0.0533 | 0.0183 |
| 1994 | 0.0034 | (0.0181) | (0.0147) | (0.0567) | (0.0658) | (0.1225) | (0.0246) | 0.0358 | 0.0112 | (0.0321) | 0.1252 | 0.0931 |
| 1995 | 0.0030 | (0.3156) | (0.3127) | (0.0566) | (0.0522) | (0.1088) | (0.0194) | 0.0439 | 0.0245 | (0.0323) | 0.1571 | 0.1248 |
| 1996 | 0.0011 | (0.0455) | (0.0444) | (0.0254) | (0.0843) | (0.1097) | (0.0214) | 0.0049 | (0.0165) | (0.0348) | 0.1847 | 0.1499 |
| 1997 | (0.0002) | (0.0132) | (0.0134) | (0.0234) | (0.0965) | (0.1199) | (0.0186) | (0.0268) | (0.0454) | (0.0306) | 0.1769 | 0.1463 |
| 1998 | (0.0329) | 0.1684 | 0.1355 | (0.0145) | (0.1255) | (0.1399) | (0.0132) | (0.0427) | (0.0559) | (0.0366) | 0.0820 | 0.0454 |
| 1999 | (0.0349) | 0.1008 | 0.0659 | (0.0311) | (0.0833) | (0.1144) | (0.0031) | (0.0652) | (0.0683) | (0.0810) | 0.2239 | 0.1429 |
| 2000 | 0.0514 | (0.0238) | 0.0276 | (0.0153) | (0.1071) | (0.1223) | 0.0147 | (0.0889) | (0.0742) | (0.0357) | 0.2493 | 0.2136 |
| 2001 | 0.0318 | (0.0081) | 0.0237 | (0.0273) | (0.0853) | (0.1126) | (0.0446) | 0.0023 | (0.0424) | (0.0436) | 0.2299 | 0.1864 |
| 2002 | 0.0420 | (0.0243) | 0.0177 | (0.0208) | (0.0726) | (0.0934) | (0.0524) | 0.0124 | (0.0400) | (0.0322) | 0.2332 | 0.2010 |
| 2003 | 0.0197 | 0.0075 | 0.0272 | (0.0212) | (0.0525) | (0.0737) | (0.0515) | 0.0204 | (0.0311) | 0.0497 | 0.1986 | 0.2483 |
| 2004 | 0.0011 | 0.0502 | 0.0514 | (0.0250) | (0.0628) | (0.0878) | (0.0550) | 0.0278 | (0.0272) | 0.1169 | 0.1798 | 0.2967 |
| 2005 | 0.0106 | 0.0197 | 0.0303 | (0.0567) | (0.0398) | (0.0965) | (0.0400) | 0.0314 | (0.0086) | 0.1966 | 0.1580 | 0.3546 |
| 2006 | 0.0132 | 0.0046 | 0.0178 | (0.0430) | (0.0549) | (0.0980) | (0.0406) | 0.0198 | (0.0209) | 0.2207 | 0.1208 | 0.3415 |
| 2007 | 0.0261 | (0.0070) | 0.0190 | (0.0294) | (0.0605) | (0.0899) | (0.0173) | (0.0146) | (0.0319) | 0.1272 | 0.1678 | 0.2950 |
| 2008 | 0.0184 | (0.0265) | (0.0081) | (0.0425) | (0.0707) | (0.1132) | (0.0357) | (0.0084) | (0.0441) | (0.0091) | 0.3412 | 0.3320 |
| 2009 | 0.0002 | 0.0464 | 0.0466 | (0.1032) | 0.0200 | (0.0832) | (0.0638) | 0.0646 | 0.0008 | (0.0601) | 0.1857 | 0.1256 |
| 2010 | 0.0186 | 0.0118 | 0.0303 | (0.0930) | 0.0064 | (0.0866) | (0.0595) | 0.0508 | (0.0086) | (0.0591) | 0.2587 | 0.1997 |
| 2011 | 0.0193 | 0.0064 | 0.0258 | (0.0441) | (0.0051) | (0.0491) | (0.0595) | 0.0508 | (0.0086) | (0.0531) | 0.3660 | 0.3129 |
| 2012 | 0.0193 | 0.0064 | 0.0258 | (0.0441) | (0.0051) | (0.0491) | (0.0595) | 0.0508 | (0.0086) | (0.0570) | 0.3725 | 0.3154 |
| 2013 | 0.0193 | 0.0064 | 0.0258 | (0.0441) | (0.0051) | (0.0491) | (0.0595) | 0.0508 | (0.0086) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate,HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11. Korea |  |  | 11. Portugal |  |  | 5. Poland |  |  | 12. Saudi Arabia |  |  |
| 1990 | 0.1471 | 0.1343 | 0.0901 | 0.0630 | 0.0684 | 0.0641 | 0.1770 | 0.0719 | 0.0488 | 0.0584 | 0.0489 | 0.0137 |
| 1991 | 0.1437 | 0.1402 | 0.0944 | 0.0870 | 0.0627 | 0.0554 | 0.0873 | 0.0514 | 0.0431 | 0.0201 | 0.0824 | 0.0158 |
| 1992 | 0.1381 | 0.1311 | 0.0869 | 0.0784 | 0.0647 | 0.0563 | 0.1070 | 0.0440 | 0.0368 | 0.0889 | 0.0723 | 0.0424 |
| 1993 | 0.1202 | 0.1114 | 0.0747 | 0.0835 | 0.0546 | 0.0441 | 0.1375 | 0.0469 | 0.0397 | 0.0781 | 0.0728 | 0.0451 |
| 1994 | 0.1171 | 0.1126 | 0.0768 | 0.0816 | 0.0529 | 0.0393 | 0.1504 | 0.0647 | 0.0567 | 0.1100 | 0.0634 | 0.0304 |
| 1995 | 0.1056 | 0.1999 | 0.1444 | 0.0613 | 0.0590 | 0.0407 | 0.1943 | 0.0564 | 0.0499 | 0.0086 | 0.0519 | 0.0024 |
| 1996 | 0.0961 | 0.1011 | 0.0736 | 0.0707 | 0.0555 | 0.0449 | 0.2370 | 0.0631 | 0.0559 | 0.0210 | 0.0520 | 0.0043 |
| 1997 | 0.0892 | 0.0857 | 0.0623 | 0.0661 | 0.0596 | 0.0488 | 0.2234 | 0.0824 | 0.0739 | 0.0159 | 0.0536 | 0.0034 |
| 1998 | 0.0754 | 0.0352 | 0.0239 | 0.0711 | 0.0626 | 0.0496 | 0.1873 | 0.0911 | 0.0827 | 0.0346 | 0.0532 | 0.0213 |
| 1999 | 0.0989 | 0.0527 | 0.0349 | 0.0208 | 0.0364 | 0.0280 | 0.1770 | 0.0881 | 0.0795 | 0.0505 | 0.0484 | 0.0158 |
| 2000 | 0.0888 | 0.0611 | 0.0431 | 0.0186 | 0.0331 | 0.0145 | 0.1771 | 0.0820 | 0.0734 | 0.0621 | 0.0452 | 0.0129 |
| 2001 | 0.0739 | 0.0562 | 0.0416 | 0.0344 | 0.0295 | 0.0243 | 0.1911 | 0.0513 | 0.0452 | 0.0185 | 0.0443 | 0.0046 |
| 2002 | 0.0786 | 0.0604 | 0.0445 | 0.0221 | 0.0280 | 0.0147 | 0.2284 | 0.0360 | 0.0308 | 0.0140 | 0.0500 | 0.0035 |
| 2003 | 0.0898 | 0.0615 | 0.0437 | 0.0411 | 0.0206 | 0.0190 | 0.2005 | 0.0358 | 0.0313 | 0.0280 | 0.0555 | 0.0057 |
| 2004 | 0.1123 | 0.0620 | 0.0411 | 0.0354 | 0.0222 | 0.0151 | 0.1645 | 0.0444 | 0.0395 | 0.0736 | 0.0626 | 0.0114 |
| 2005 | 0.0846 | 0.0581 | 0.0413 | 0.0349 | 0.0272 | 0.0205 | 0.1485 | 0.0383 | 0.0346 | 0.1654 | 0.0707 | 0.0183 |
| 2006 | 0.0707 | 0.0562 | 0.0411 | 0.0345 | 0.0281 | 0.0214 | 0.1333 | 0.0493 | 0.0447 | 0.2167 | 0.0749 | 0.0252 |
| 2007 | 0.0921 | 0.0645 | 0.0446 | 0.0337 | 0.0285 | 0.0229 | 0.1079 | 0.0881 | 0.0803 | 0.2516 | 0.0932 | 0.0386 |
| 2008 | 0.0802 | 0.0672 | 0.0482 | 0.0411 | 0.0288 | 0.0232 | 0.0939 | 0.0834 | 0.0765 | 0.3317 | 0.1033 | 0.0419 |
| 2009 | 0.0753 | 0.0495 | 0.0346 | 0.0399 | 0.0211 | 0.0166 | 0.0885 | 0.0567 | 0.0522 | 0.1466 | 0.0948 | 0.0532 |
| 2010 | 0.1004 | 0.0634 | 0.0420 | 0.0412 | 0.0211 | 0.0165 | 0.0832 | 0.0572 | 0.0527 | 0.1975 | 0.1008 | 0.0501 |
| 2011 | 0.0926 | 0.0613 | 0.0415 | 0.0358 | 0.0151 | 0.0119 | 0.0743 | 0.0544 | 0.0494 | 0.2615 | 0.0918 | 0.0376 |
| 2012 | 0.0926 | 0.0569 | 0.0417 | 0.0353 | 0.0054 | 0.0041 | 0.0679 | 0.0516 | 0.0469 | 0.2502 | 0.0900 | 0.0360 |
| 2013 | 0.0864 | 0.0539 | 0.0394 | 0.0384 | 0.0053 | 0.0044 | 0.0625 | 0.0491 | 0.0446 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A13 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{P} R \mathrm{I}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 12. Malaysia |  |  | 12. Slovak |  |  | 6. Romania |  |  | 13. Algeria |  |  |
| 1990 | (0.0321) | 0.0075 | (0.0245) |  |  |  |  |  |  | (0.0401) | 0.0210 | (0.0190) |
| 1991 | (0.0217) | (0.0749) | (0.0966) |  |  |  |  |  |  | (0.0322) | 0.0942 | 0.0620 |
| 1992 | (0.0090) | (0.0340) | (0.0430) |  |  |  |  |  |  | (0.0414) | 0.0639 | 0.0225 |
| 1993 | 0.0023 | (0.0567) | (0.0544) |  |  |  |  |  |  | (0.0514) | 0.0357 | (0.0157) |
| 1994 | 0.0251 | (0.0964) | (0.0713) |  |  |  |  |  |  | (0.0451) | (0.0161) | (0.0612) |
| 1995 | 0.0088 | (0.0990) | (0.0902) | (0.0288) | 0.0529 | 0.0242 | (0.0343) | (0.0308) | (0.0651) | (0.0157) | (0.0304) | (0.0461) |
| 1996 | 0.0075 | (0.0418) | (0.0342) | (0.0146) | (0.1048) | (0.1195) | (0.0473) | (0.0518) | (0.0992) | (0.0111) | 0.0911 | 0.0800 |
| 1997 | 0.0248 | (0.0718) | (0.0469) | (0.0445) | (0.0635) | (0.1080) | (0.0438) | (0.0364) | (0.0802) | (0.0280) | 0.1249 | 0.0969 |
| 1998 | (0.0187) | 0.1940 | 0.1753 | (0.0409) | (0.0803) | (0.1211) | (0.0322) | (0.0555) | (0.0877) | (0.0397) | 0.0382 | (0.0015) |
| 1999 | (0.0339) | 0.2285 | 0.1946 | (0.0354) | (0.0141) | (0.0495) | (0.0272) | (0.0255) | (0.0526) | (0.0038) | 0.0635 | 0.0597 |
| 2000 | (0.0350) | 0.1609 | 0.1259 | (0.0329) | 0.0049 | (0.0279) | (0.0170) | (0.0459) | (0.0629) | 0.1078 | 0.1292 | 0.2370 |
| 2001 | (0.0336) | 0.1433 | 0.1097 | (0.0027) | (0.0882) | (0.0909) | (0.0179) | (0.0692) | (0.0871) | 0.0485 | 0.1145 | 0.1630 |
| 2002 | (0.0223) | 0.1370 | 0.1146 | (0.0034) | (0.0775) | (0.0809) | 0.0034 | (0.0664) | (0.0630) | 0.0129 | 0.0968 | 0.1097 |
| 2003 | (0.0278) | 0.1790 | 0.1512 | (0.0015) | (0.0192) | (0.0207) | (0.0338) | (0.0487) | (0.0825) | 0.0612 | 0.0985 | 0.1597 |
| 2004 | (0.0289) | 0.1894 | 0.1605 | (0.0013) | (0.0290) | (0.0303) | (0.0126) | (0.0892) | (0.1018) | 0.0590 | 0.1011 | 0.1601 |
| 2005 | (0.0301) | 0.2213 | 0.1913 | (0.0013) | (0.0502) | (0.0515) | 0.0013 | (0.1123) | (0.1109) | 0.1488 | 0.1082 | 0.2570 |
| 2006 | (0.0254) | 0.2299 | 0.2045 | (0.0015) | (0.0415) | (0.0430) | 0.0063 | (0.1384) | (0.1321) | 0.1530 | 0.1453 | 0.2983 |
| 2007 | (0.0239) | 0.2120 | 0.1882 | (0.0010) | (0.0106) | (0.0115) | 0.0112 | (0.1639) | (0.1527) | 0.0685 | 0.1778 | 0.2463 |
| 2008 | (0.0278) | 0.2345 | 0.2068 | (0.0011) | (0.0242) | (0.0253) | (0.0189) | (0.1244) | (0.1433) | 0.1037 | 0.1097 | 0.2134 |
| 2009 | (0.0455) | 0.2453 | 0.1998 | (0.0953) | 0.0899 | (0.0054) | (0.0637) | (0.0031) | (0.0668) | (0.0534) | 0.0470 | (0.0064) |
| 2010 | (0.0481) | 0.1991 | 0.1510 | (0.0874) | 0.0857 | (0.0017) | (0.0399) | (0.0194) | (0.0593) | (0.0508) | 0.1285 | 0.0777 |
| 2011 | (0.0481) | 0.1991 | 0.1510 | (0.0626) | 0.0691 | 0.0065 | (0.0399) | (0.0194) | (0.0593) | (0.0537) | 0.1700 | 0.1163 |
| 2012 | (0.0481) | 0.1991 | 0.1510 |  |  |  | (0.0399) | (0.0194) | (0.0593) | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2013 | (0.0481) | 0.1991 | 0.1510 |  |  |  | (0.0399) | (0.0194) | (0.0593) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 12. Malaysia |  |  | 12. Slovak |  |  | 6. Romania |  |  | 13. Algeria |  |  |
| 1990 | 0.1518 | 0.1522 | 0.0944 |  |  |  |  |  |  | 0.0531 | 0.0776 | 0.0390 |
| 1991 | 0.1323 | 0.1685 | 0.1069 |  |  |  |  |  |  | 0.1209 | 0.1057 | 0.0584 |
| 1992 | 0.1355 | 0.1556 | 0.0910 |  |  |  |  |  |  | 0.1072 | 0.1033 | 0.0601 |
| 1993 | 0.1248 | 0.1532 | 0.0872 |  |  |  |  |  |  | 0.0851 | 0.0926 | 0.0551 |
| 1994 | 0.1156 | 0.1521 | 0.0852 |  |  |  |  |  |  | 0.0930 | 0.1106 | 0.0707 |
| 1995 | 0.1321 | 0.1676 | 0.0933 | 0.0633 | 0.0486 | 0.0406 | 0.0288 | 0.0413 | 0.0433 | 0.1129 | 0.1184 | 0.0782 |
| 1996 | 0.1321 | 0.1528 | 0.0773 | 0.0444 | 0.0813 | 0.0720 | 0.0507 | 0.0532 | 0.0551 | 0.1437 | 0.0909 | 0.0556 |
| 1997 | 0.1222 | 0.1475 | 0.0736 | 0.0502 | 0.0822 | 0.0714 | 0.1135 | 0.0584 | 0.0592 | 0.1337 | 0.0782 | 0.0471 |
| 1998 | 0.1111 | 0.0871 | 0.0338 | 0.0414 | 0.0779 | 0.0691 | 0.1452 | 0.0661 | 0.0657 | 0.0985 | 0.0928 | 0.0576 |
| 1999 | 0.0926 | 0.0719 | 0.0272 | 0.0512 | 0.0654 | 0.0577 | 0.1447 | 0.0582 | 0.0596 | 0.1240 | 0.0860 | 0.0555 |
| 2000 | 0.1012 | 0.0884 | 0.0383 | 0.0523 | 0.0590 | 0.0519 | 0.2620 | 0.0731 | 0.0700 | 0.2278 | 0.0828 | 0.0432 |
| 2001 | 0.0784 | 0.0742 | 0.0340 | 0.0456 | 0.0715 | 0.0641 | 0.2580 | 0.0951 | 0.0903 | 0.1075 | 0.1059 | 0.0339 |
| 2002 | 0.0819 | 0.0747 | 0.0345 | 0.0456 | 0.0684 | 0.0616 | 0.2406 | 0.0966 | 0.0911 | 0.1684 | 0.1051 | 0.0632 |
| 2003 | 0.0862 | 0.0691 | 0.0311 | 0.0488 | 0.0523 | 0.0469 | 0.2213 | 0.0989 | 0.0933 | 0.1959 | 0.1054 | 0.0586 |
| 2004 | 0.0960 | 0.0722 | 0.0328 | 0.0531 | 0.0596 | 0.0531 | 0.1977 | 0.0968 | 0.0914 | 0.2162 | 0.1206 | 0.0637 |
| 2005 | 0.0940 | 0.0639 | 0.0281 | 0.0556 | 0.0689 | 0.0610 | 0.1774 | 0.0960 | 0.0903 | 0.2793 | 0.1209 | 0.0527 |
| 2006 | 0.0987 | 0.0633 | 0.0276 | 0.0547 | 0.0653 | 0.0580 | 0.1536 | 0.1178 | 0.1104 | 0.2822 | 0.1125 | 0.0446 |
| 2007 | 0.1088 | 0.0711 | 0.0324 | 0.0762 | 0.0668 | 0.0565 | 0.1332 | 0.1386 | 0.1283 | 0.2617 | 0.1277 | 0.0518 |
| 2008 | 0.1103 | 0.0648 | 0.0298 | 0.0660 | 0.0669 | 0.0573 | 0.1229 | 0.1338 | 0.1236 | 0.2578 | 0.1404 | 0.0573 |
| 2009 | 0.0638 | 0.0427 | 0.0175 | 0.0079 | 0.0091 | 0.0065 | 0.1032 | 0.0876 | 0.0816 | 0.1376 | 0.1406 | 0.0752 |
| 2010 | 0.0867 | 0.0632 | 0.0313 | 0.0095 | 0.0105 | 0.0092 | 0.0821 | 0.0864 | 0.0820 | 0.2599 | 0.1333 | 0.0339 |
| 2011 | 0.1081 | 0.0566 | 0.0381 | 0.0067 | 0.0132 | 0.0072 | 0.0680 | 0.0812 | 0.0731 | 0.1373 | 0.1038 | 0.0526 |
| 2012 | 0.1011 | 0.0536 | 0.0361 | 0.0116 | 0.0109 | 0.0079 | 0.0601 | 0.0751 | 0.0676 | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2013 | 0.0950 | 0.0508 | 0.0342 | \#VALUE! | \#VALUE! | \#VALUE! | 0.0539 | 0.0698 | 0.0629 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A14 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of Y, $g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 13. Philippines |  |  | 13. Slovenia |  |  | 7. Russia |  |  | 14. Egypt |  |  |
| 1990 | (0.0384) | (0.0317) | (0.0700) |  |  |  |  |  |  | (0.0635) | (0.0775) | (0.1411) |
| 1991 | (0.0227) | (0.0037) | (0.0265) |  |  |  |  |  |  | (0.0105) | (0.0774) | (0.0879) |
| 1992 | (0.0128) | (0.0217) | (0.0345) |  |  |  |  |  |  | (0.0386) | (0.0053) | (0.0439) |
| 1993 | (0.0165) | (0.0509) | (0.0674) |  |  |  |  |  |  | 0.0189 | (0.0797) | (0.0607) |
| 1994 | 0.0119 | (0.0534) | (0.0415) |  |  |  |  |  |  | 0.0037 | (0.0710) | (0.0673) |
| 1995 | 0.0062 | (0.0602) | (0.0540) | (0.0030) | 0.0268 | 0.0237 | (0.0540) | 0.0914 | 0.0373 | 0.0100 | (0.0769) | (0.0670) |
| 1996 | 0.0030 | (0.0520) | (0.0490) | 0.0007 | 0.0244 | 0.0250 | (0.0817) | 0.1282 | 0.0465 | (0.0214) | (0.0439) | (0.0653) |
| 1997 | 0.0006 | (0.0597) | (0.0591) | (0.0150) | 0.0091 | (0.0059) | (0.0713) | 0.0955 | 0.0242 | (0.0224) | (0.0473) | (0.0698) |
| 1998 | (0.0178) | 0.0037 | (0.0141) | (0.0078) | (0.0062) | (0.0140) | (0.0548) | 0.1304 | 0.0756 | (0.0100) | (0.0955) | (0.1055) |
| 1999 | (0.0356) | 0.0879 | 0.0523 | (0.0083) | (0.0355) | (0.0438) | (0.0130) | 0.2026 | 0.1896 | (0.0008) | (0.0910) | (0.0917) |
| 2000 | (0.0382) | 0.1153 | 0.0772 | (0.0129) | (0.0256) | (0.0385) | 0.0386 | 0.1839 | 0.2225 | (0.0136) | (0.0599) | (0.0735) |
| 2001 | (0.0379) | 0.0717 | 0.0338 | (0.0112) | 0.0044 | (0.0069) | 0.0303 | 0.1099 | 0.1402 | (0.0613) | 0.0074 | (0.0539) |
| 2002 | (0.0503) | 0.1062 | 0.0559 | (0.0090) | 0.0160 | 0.0069 | 0.0770 | 0.0434 | 0.1204 | (0.0749) | 0.0266 | (0.0484) |
| 2003 | (0.0432) | 0.0559 | 0.0127 | (0.0144) | 0.0032 | (0.0112) | 0.0209 | 0.1047 | 0.1257 | (0.0646) | 0.0359 | (0.0287) |
| 2004 | (0.0356) | 0.0735 | 0.0378 | (0.0161) | (0.0113) | (0.0274) | 0.0643 | 0.0717 | 0.1360 | (0.0623) | 0.0472 | (0.0151) |
| 2005 | (0.0249) | 0.0624 | 0.0374 | (0.0130) | (0.0012) | (0.0142) | 0.0722 | 0.0799 | 0.1521 | (0.0619) | 0.0367 | (0.0252) |
| 2006 | (0.0099) | 0.0801 | 0.0702 | (0.0068) | (0.0120) | (0.0188) | 0.1007 | 0.0411 | 0.1419 | (0.0853) | 0.0673 | (0.0180) |
| 2007 | (0.0017) | 0.0846 | 0.0829 | 0.0304 | (0.0736) | (0.0432) | 0.0801 | 0.0168 | 0.0969 | (0.0572) | 0.0064 | (0.0509) |
| 2008 | (0.0091) | 0.0994 | 0.0903 | 0.0114 | (0.0694) | (0.0580) | 0.0595 | 0.0417 | 0.1012 | (0.0707) | 0.0085 | (0.0622) |
| 2009 | (0.0114) | 0.1473 | 0.1359 | (0.0378) | 0.0386 | 0.0008 | (0.0507) | 0.1319 | 0.0812 | (0.0729) | (0.0009) | (0.0738) |
| 2010 | (0.0229) | 0.1885 | 0.1656 | (0.0409) | 0.0342 | (0.0068) | (0.0161) | 0.1061 | 0.0900 | (0.0860) | 0.0278 | (0.0582) |
| 2011 | (0.0229) | 0.1885 | 0.1656 | (0.0554) | 0.0534 | (0.0020) | 0.0445 | 0.0444 | 0.0889 | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2012 | (0.0229) | 0.1885 | 0.1656 |  |  |  | 0.0281 | 0.0659 | 0.0941 | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2013 | (0.0229) | 0.1885 | 0.1656 |  |  |  | 0.0000 | 0.0802 | 0.0802 | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 13. Philippines |  |  | 13. Slovenia |  |  | 7. Russia |  |  | 14. Egypt |  |  |
| 1990 | 0.0865 | 0.1073 | 0.0747 |  |  |  |  |  |  | 0.1017 | 0.1356 | 0.1010 |
| 1991 | 0.0677 | 0.0939 | 0.0508 |  |  |  |  |  |  | 0.1008 | 0.0970 | 0.0661 |
| 1992 | 0.0767 | 0.0748 | 0.0427 |  |  |  |  |  |  | 0.0919 | 0.0810 | 0.0531 |
| 1993 | 0.1050 | 0.0705 | 0.0421 |  |  |  |  |  |  | 0.0917 | 0.0874 | 0.0584 |
| 1994 | 0.0904 | 0.0640 | 0.0363 |  |  |  |  |  |  | 0.0990 | 0.0801 | 0.0511 |
| 1995 | 0.0895 | 0.0841 | 0.0641 | 0.0392 | 0.0331 | 0.0247 | 0.0506 | 0.0928 | 0.0907 | 0.0392 | 0.1073 | 0.0251 |
| 1996 | 0.0727 | 0.0946 | 0.0629 | 0.0474 | 0.0368 | 0.0300 | 0.0540 | 0.0908 | 0.0884 | 0.1236 | 0.0639 | 0.0375 |
| 1997 | 0.1248 | 0.1366 | 0.0965 | 0.0596 | 0.0589 | 0.0493 | 0.0355 | 0.0712 | 0.0759 | 0.0972 | 0.0813 | 0.0541 |
| 1998 | 0.0827 | 0.1088 | 0.0613 | 0.0645 | 0.0639 | 0.0548 | 0.0343 | 0.0321 | 0.0337 | 0.0539 | 0.1062 | 0.0253 |
| 1999 | 0.1101 | 0.0783 | 0.0469 | 0.0608 | 0.0724 | 0.0628 | 0.1515 | 0.0360 | 0.0365 | 0.1075 | 0.0777 | 0.0490 |
| 2000 | 0.1544 | 0.0824 | 0.0468 | 0.0618 | 0.0704 | 0.0616 | 0.6171 | 0.0808 | 0.0636 | 0.1048 | 0.0652 | 0.0384 |
| 2001 | 0.1635 | 0.1044 | 0.0623 | 0.0654 | 0.0617 | 0.0529 | 0.4439 | 0.1011 | 0.0846 | 0.0099 | 0.0809 | 0.0047 |
| 2002 | 0.1758 | 0.0984 | 0.0552 | 0.0724 | 0.0608 | 0.0513 | 0.3534 | 0.0814 | 0.0717 | 0.0887 | 0.0526 | 0.0306 |
| 2003 | 0.1867 | 0.1200 | 0.0675 | 0.0711 | 0.0672 | 0.0567 | 0.3536 | 0.0856 | 0.0744 | 0.0796 | 0.0468 | 0.0258 |
| 2004 | 0.2020 | 0.1146 | 0.0598 | 0.0784 | 0.0770 | 0.0636 | 0.3640 | 0.0854 | 0.0731 | 0.0765 | 0.0488 | 0.0279 |
| 2005 | 0.1945 | 0.1119 | 0.0579 | 0.0766 | 0.0711 | 0.0577 | 0.3737 | 0.0799 | 0.0671 | 0.0807 | 0.0553 | 0.0335 |
| 2006 | 0.1715 | 0.0911 | 0.0465 | 0.0834 | 0.0751 | 0.0597 | 0.3588 | 0.0902 | 0.0741 | 0.0767 | 0.0605 | 0.0385 |
| 2007 | 0.1806 | 0.0895 | 0.0437 | 0.1782 | 0.1284 | 0.0971 | 0.3089 | 0.1127 | 0.0921 | 0.0923 | 0.0754 | 0.0512 |
| 2008 | 0.1871 | 0.0886 | 0.0426 | 0.1359 | 0.1202 | 0.0905 | 0.3046 | 0.1163 | 0.0932 | 0.0934 | 0.0855 | 0.0602 |
| 2009 | 0.1497 | 0.0611 | 0.0275 | 0.0620 | 0.0597 | 0.0484 | 0.1716 | 0.0581 | 0.0503 | 0.1362 | 0.0682 | 0.0422 |
| 2010 | (0.0115) | 0.0161 | (0.0014) | 0.0484 | 0.0506 | 0.0412 | 0.3036 | 0.0839 | 0.0641 | 0.1171 | 0.0699 | 0.0452 |
| 2011 | 0.1031 | 0.0101 | 0.0083 | 0.0436 | 0.0349 | 0.0270 | 0.2081 | 0.0610 | 0.0509 | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2012 | 0.1016 | 0.0100 | 0.0082 | 0.0396 | 0.0302 | 0.0229 | 0.3085 | 0.0839 | 0.0632 | \#DIV/0! | \#DIV/0! | \#DIV/0! |
| 2013 | 0.1001 | 0.0099 | 0.0082 | 0.0453 | 0.0278 | 0.0252 | 0.0000 | (1.0000) | 1.5390 | \#DIV/0! | \#DIV/0! | \#DIV/0! |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A15 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\mathrm{PRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{spRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 14. Singapore |  |  | 14. Spain |  |  | 8. Turkey |  |  | 15. Kenya |  |  |
| 1990 | 0.1086 | (0.0012) | 0.1074 | (0.0376) | (0.0105) | (0.0481) | (0.0341) | (0.0137) | (0.0478) | (0.0476) | (0.0682) | (0.1158) |
| 1991 | 0.1140 | 0.0247 | 0.1386 | (0.0360) | (0.0107) | (0.0467) | (0.0565) | 0.0264 | (0.0302) | (0.0561) | (0.0212) | (0.0773) |
| 1992 | 0.1297 | 0.0118 | 0.1415 | (0.0480) | 0.0033 | (0.0447) | (0.0462) | 0.0145 | (0.0318) | (0.0144) | (0.0371) | (0.0516) |
| 1993 | 0.1550 | (0.0635) | 0.0915 | (0.0778) | 0.0613 | (0.0165) | (0.0253) | (0.0352) | (0.0605) | (0.0497) | 0.0217 | (0.0280) |
| 1994 | 0.1363 | 0.0556 | 0.1919 | (0.0872) | 0.0686 | (0.0186) | (0.0317) | 0.0422 | 0.0104 | (0.0649) | 0.0358 | (0.0291) |
| 1995 | 0.1301 | 0.0513 | 0.1814 | (0.0545) | 0.0545 | 0.0000 | (0.0215) | (0.0281) | (0.0495) | (0.0147) | (0.0983) | (0.1130) |
| 1996 | 0.1438 | 0.0166 | 0.1604 | (0.0571) | 0.0631 | 0.0060 | (0.0238) | (0.0461) | (0.0699) | 0.0101 | (0.0776) | (0.0676) |
| 1997 | 0.0924 | 0.0693 | 0.1617 | (0.0256) | 0.0353 | 0.0097 | (0.0477) | (0.0168) | (0.0645) | (0.0196) | (0.0686) | (0.0883) |
| 1998 | 0.1446 | 0.0851 | 0.2297 | (0.0102) | 0.0110 | 0.0008 | (0.0387) | 0.0515 | 0.0129 | (0.0069) | (0.0750) | (0.0819) |
| 1999 | 0.1146 | 0.0727 | 0.1873 | (0.0160) | (0.0034) | (0.0194) | (0.0507) | 0.0524 | 0.0017 | (0.0028) | (0.0694) | (0.0722) |
| 2000 | 0.1006 | 0.0285 | 0.1291 | 0.0082 | (0.0439) | (0.0357) | (0.0292) | (0.0040) | (0.0333) | 0.0086 | (0.1105) | (0.1019) |
| 2001 | (0.0151) | 0.1681 | 0.1530 | 0.0150 | (0.0431) | (0.0281) | (0.0466) | 0.0924 | 0.0458 | 0.0222 | (0.1645) | (0.1422) |
| 2002 | (0.0051) | 0.1545 | 0.1493 | 0.0206 | (0.0454) | (0.0247) | (0.0452) | 0.0634 | 0.0182 | 0.0222 | (0.1102) | (0.0880) |
| 2003 | 0.0685 | 0.1829 | 0.2513 | 0.0182 | (0.0456) | (0.0273) | (0.0854) | 0.0738 | (0.0116) | (0.0244) | (0.0501) | (0.0745) |
| 2004 | 0.0660 | 0.1321 | 0.1981 | 0.0194 | (0.0648) | (0.0454) | (0.0524) | 0.0232 | (0.0293) | (0.0163) | (0.0797) | (0.0960) |
| 2005 | 0.0868 | 0.1545 | 0.2413 | 0.0363 | (0.0956) | (0.0593) | (0.0428) | 0.0040 | (0.0388) | 0.0166 | (0.1241) | (0.1075) |
| 2006 | 0.0760 | 0.1956 | 0.2717 | 0.0494 | (0.1213) | (0.0719) | (0.0264) | (0.0282) | (0.0545) | (0.0220) | (0.1005) | (0.1226) |
| 2007 | 0.1272 | 0.1730 | 0.3001 | 0.0492 | (0.1249) | (0.0757) | (0.0198) | (0.0376) | (0.0573) | (0.0183) | (0.0949) | (0.1132) |
| 2008 | 0.0580 | 0.1171 | 0.1751 | (0.0226) | (0.0425) | (0.0651) | (0.0271) | (0.0220) | (0.0491) | (0.0320) | (0.1112) | (0.1432) |
| 2009 | (0.0157) | 0.2390 | 0.2233 | (0.0938) | 0.0734 | (0.0204) | (0.0467) | 0.0344 | (0.0123) | (0.0452) | (0.0855) | (0.1307) |
| 2010 | 0.0773 | 0.1792 | 0.2565 | (0.0838) | 0.0591 | (0.0246) | (0.0427) | (0.0190) | (0.0617) | (0.0567) | (0.0690) | (0.1257) |
| 2011 | 0.0773 | 0.1792 | 0.2565 | (0.0966) | 0.0882 | (0.0085) | (0.0361) | 0.0360 | (0.0001) | (0.0429) | (0.1212) | (0.1640) |
| 2012 | 0.0773 | 0.1792 | 0.2565 |  |  |  | (0.0331) | 0.0330 | (0.0001) | (0.0453) | (0.1363) | (0.1816) |
| 2013 | 0.0773 | 0.1792 | 0.2565 |  |  |  |  |  |  | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.ate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 14. Singapore |  |  | 14. Spain |  |  | 8. Turkey |  |  | 15. Kenya |  |  |
| 1990 | 0.1781 | 0.1344 | 0.0665 | 0.0524 | 0.0663 | 0.0570 | 0.1478 | 0.0926 | 0.0954 | 0.0977 | 0.0806 | 0.1074 |
| 1991 | 0.1551 | 0.1246 | 0.0525 | 0.0513 | 0.0628 | 0.0545 | 0.1334 | 0.1172 | 0.0844 | 0.0210 | 0.1141 | 0.0302 |
| 1992 | 0.1715 | 0.1221 | 0.0567 | 0.0510 | 0.0547 | 0.0476 | 0.1739 | 0.1374 | 0.1015 | 0.0928 | 0.0555 | 0.0575 |
| 1993 | 0.1620 | 0.1330 | 0.0651 | 0.0491 | 0.0411 | 0.0348 | 0.1821 | 0.1498 | 0.1165 | 0.0195 | 0.1210 | 0.0223 |
| 1994 | 0.1549 | 0.1017 | 0.0424 | 0.0488 | 0.0401 | 0.0336 | 0.2310 | 0.1075 | 0.0801 | 0.0522 | 0.1009 | 0.0507 |
| 1995 | 0.2523 | 0.1536 | 0.0679 | 0.0517 | 0.0481 | 0.0404 | 0.2471 | 0.1333 | 0.1042 | 0.2123 | 0.0550 | 0.1140 |
| 1996 | 0.1941 | 0.1478 | 0.0583 | 0.0520 | 0.0468 | 0.0394 | 0.2381 | 0.1628 | 0.1339 | 0.1086 | 0.0468 | 0.0140 |
| 1997 | 0.1932 | 0.1483 | 0.0556 | 0.0543 | 0.0478 | 0.0406 | 0.2327 | 0.1466 | 0.1194 | 0.1484 | 0.0505 | 0.0169 |
| 1998 | 0.1367 | 0.1060 | 0.0335 | 0.0542 | 0.0519 | 0.0440 | 0.3418 | 0.1291 | 0.0981 | 0.0801 | 0.0411 | 0.0062 |
| 1999 | 0.1258 | 0.0996 | 0.0376 | 0.0427 | 0.0508 | 0.0425 | 0.3430 | 0.0996 | 0.0724 | 0.0513 | 0.0306 | 0.0029 |
| 2000 | 0.1156 | 0.1023 | 0.0448 | 0.0416 | 0.0562 | 0.0460 | 0.2800 | 0.1121 | 0.0857 | 0.1857 | 0.0558 | 0.0207 |
| 2001 | 0.0894 | 0.0718 | 0.0357 | 0.0386 | 0.0586 | 0.0411 | 0.9961 | 0.0191 | 0.0514 | 0.2584 | 0.0643 | 0.0283 |
| 2002 | 0.0820 | 0.0621 | 0.0345 | 0.0384 | 0.0602 | 0.0396 | 0.2880 | 0.0839 | 0.0622 | (0.0119) | 0.0263 | (0.0005) |
| 2003 | 0.0813 | 0.0388 | 0.0205 | 0.0393 | 0.0627 | 0.0401 | 0.3066 | 0.0828 | 0.0604 | (0.0576) | 0.0242 | (0.0023) |
| 2004 | 0.0887 | 0.0596 | 0.0294 | 0.0359 | 0.0648 | 0.0423 | 0.2652 | 0.0953 | 0.0719 | 0.1830 | 0.0537 | 0.0188 |
| 2005 | 0.0895 | 0.0581 | 0.0240 | 0.0363 | 0.0681 | 0.0458 | 0.2297 | 0.0955 | 0.0724 | 0.2050 | 0.0661 | 0.0277 |
| 2006 | 0.1010 | 0.0645 | 0.0229 | 0.0382 | 0.0717 | 0.0500 | 0.1873 | 0.1066 | 0.0828 | 0.2292 | 0.0753 | 0.0346 |
| 2007 | 0.1001 | 0.0701 | 0.0195 | 0.0365 | 0.0711 | 0.0494 | 0.1772 | 0.0938 | 0.0710 | 0.1071 | 0.1301 | 0.0900 |
| 2008 | 0.0884 | 0.0834 | 0.0300 | 0.0313 | 0.0616 | 0.0430 | 0.1408 | 0.0939 | 0.0723 | 0.0900 | 0.1397 | 0.0986 |
| 2009 | 0.0703 | 0.0624 | 0.0207 | 0.0244 | 0.0415 | 0.0270 | 0.1465 | 0.0429 | 0.0258 | 0.0794 | 0.1267 | 0.0872 |
| 2010 | 0.0929 | 0.0637 | 0.0227 | 0.0229 | 0.0362 | 0.0241 | 0.1657 | 0.0756 | 0.0536 | 0.0695 | 0.1149 | 0.0765 |
| 2011 | 0.1297 | 0.0571 | 0.0311 | 0.0232 | 0.0312 | 0.0217 | 0.1239 | 0.0554 | 0.0377 | 0.0651 | 0.1338 | 0.0935 |
| 2012 | 0.1216 | 0.0540 | 0.0294 | 0.0231 | 0.0258 | 0.0186 | 0.1084 | 0.0686 | 0.0498 | 0.0593 | 0.1273 | 0.0873 |
| 2013 | 0.1146 | 0.0513 | 0.0279 | 0.0280 | 0.0240 | 0.0218 | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

Table A16 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{i}_{\text {PRI }}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 15. Sri Lanka |  |  | Taiwan |  |  | 9. Ukraine |  |  | 16. Morocco |  |  |
| 1990 | (0.0850) | (0.0233) | (0.1083) | (0.0171) | 0.0641 | 0.0470 |  |  |  | (0.0249) | 0.0205 | (0.0044) |
| 1991 | (0.1039) | (0.0290) | (0.1329) | (0.0174) | 0.0598 | 0.0424 |  |  |  | (0.0233) | 0.0115 | (0.0118) |
| 1992 | (0.0592) | (0.0628) | (0.1220) | (0.0195) | 0.0372 | 0.0176 |  |  |  | (0.0154) | 0.0030 | (0.0124) |
| 1993 | (0.0706) | (0.0475) | (0.1180) | (0.0195) | 0.0361 | 0.0166 | (0.0111) | 0.0111 | 0.0000 | (0.0290) | 0.0118 | (0.0173) |
| 1994 | (0.0939) | (0.0516) | (0.1455) | (0.0210) | 0.0381 | 0.0170 | (0.0088) | (0.0282) | (0.0370) | (0.0355) | 0.0183 | (0.0171) |
| 1995 | (0.0908) | (0.0353) | (0.1262) | (0.0193) | 0.0358 | 0.0165 | (0.0714) | 0.0204 | (0.0510) | (0.0488) | 0.0106 | (0.0382) |
| 1996 | (0.0857) | (0.0285) | (0.1142) | (0.0205) | 0.0559 | 0.0354 | (0.0545) | 0.0123 | (0.0423) | (0.0330) | 0.0340 | 0.0010 |
| 1997 | (0.0681) | (0.1074) | (0.1755) | (0.0151) | 0.0374 | 0.0223 | (0.0416) | (0.0071) | (0.0488) | (0.0077) | 0.0048 | (0.0029) |
| 1998 | (0.0761) | (0.0004) | (0.0765) | (0.0129) | 0.0242 | 0.0112 | (0.0325) | (0.0152) | (0.0476) | (0.0212) | 0.0172 | (0.0040) |
| 1999 | (0.0653) | (0.0392) | (0.1044) | (0.0134) | 0.0405 | 0.0271 | (0.0225) | 0.0540 | 0.0315 | (0.0243) | 0.0199 | (0.0044) |
| 2000 | (0.0933) | (0.0449) | (0.1382) | (0.0445) | 0.0679 | 0.0235 | (0.0089) | 0.0317 | 0.0229 | (0.0587) | 0.0447 | (0.0140) |
| 2001 | (0.1038) | 0.0157 | (0.0881) | (0.0683) | 0.1272 | 0.0589 | (0.0147) | 0.0131 | (0.0016) | 0.0113 | 0.0364 | 0.0477 |
| 2002 | (0.0819) | (0.0068) | (0.0886) | (0.0306) | 0.1082 | 0.0776 | 0.0049 | 0.0280 | 0.0330 | 0.0124 | 0.0291 | 0.0414 |
| 2003 | (0.0762) | (0.0008) | (0.0771) | (0.0246) | 0.1006 | 0.0760 | (0.0029) | 0.0187 | 0.0158 | 0.0100 | 0.0273 | 0.0372 |
| 2004 | (0.0815) | (0.0275) | (0.1090) | (0.0266) | 0.0664 | 0.0399 | (0.0293) | 0.1037 | 0.0744 | 0.0064 | 0.0147 | 0.0210 |
| 2005 | (0.0775) | (0.0353) | (0.1128) | (0.0032) | 0.0510 | 0.0477 | (0.0191) | 0.0159 | (0.0033) | 0.0001 | 0.0242 | 0.0243 |
| 2006 | (0.0765) | (0.0611) | (0.1376) | (0.0023) | 0.0684 | 0.0661 | (0.0074) | (0.0421) | (0.0494) | (0.0012) | 0.0315 | 0.0303 |
| 2007 | (0.0725) | (0.0550) | (0.1274) | (0.0024) | 0.0884 | 0.0860 | (0.0128) | (0.0558) | (0.0686) | 0.0078 | (0.0093) | (0.0015) |
| 2008 | (0.0730) | (0.1055) | (0.1785) | (0.0091) | 0.0623 | 0.0531 | (0.0115) | (0.0874) | (0.0989) | 0.0104 | (0.0683) | (0.0580) |
| 2009 | (0.1142) | 0.0292 | (0.0850) | (0.0394) | 0.1329 | 0.0935 | (0.0398) | (0.0019) | (0.0417) | 0.0051 | (0.0612) | (0.0561) |
| 2010 | (0.1101) | (0.0057) | (0.1158) | (0.0296) | 0.1060 | 0.0764 | (0.0646) | 0.0285 | (0.0361) | 0.0051 | (0.0562) | (0.0511) |
| 2011 | (0.1101) | (0.0057) | (0.1158) | (0.0296) | 0.1060 | 0.0764 | (0.0159) | (0.0599) | (0.0758) | 0.0031 | (0.1072) | (0.1041) |
| 2012 | (0.1101) | (0.0057) | (0.1158) | (0.0296) | 0.1060 | 0.0764 | (0.0219) | 0.2611 | 0.2392 | 0.0006 | (0.0620) | (0.0614) |
| 2013 | (0.1101) | (0.0057) | (0.1158) | (0.0296) | 0.1060 | 0.0764 | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}$ * | $\begin{array}{\|l\|} \hline \text { Infla.rate, } \mathrm{HA} \quad \mathrm{gy}^{*} \\ \hline \text { 16. Morocco } \end{array}$ |  | $\mathrm{ga}^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 15. Sri Lanka |  |  | Taiwan |  |  | 9. Ukraine |  |  |  |  |  |
| 1990 | 0.4345 | 0.1673 | 0.1372 | 0.0548 | 0.0411 | 0.0244 |  |  |  | 0.0264 | 0.0368 | 0.0138 |
| 1991 | 0.3348 | 0.1520 | 0.1161 | 0.0556 | 0.0443 | 0.0254 |  |  |  | 0.0148 | 0.0255 | 0.0051 |
| 1992 | 0.2024 | 0.1400 | 0.1149 | 0.0598 | 0.0516 | 0.0309 |  |  |  | 0.0023 | 0.0198 | 0.0006 |
| 1993 | 0.1476 | 0.1353 | 0.1085 | 0.0649 | 0.0543 | 0.0326 | 1.1092 | 0.9630 | 0.0164 | 0.0106 | 0.0222 | 0.0033 |
| 1994 | 0.0938 | 0.1634 | 0.0887 | 0.0619 | 0.0532 | 0.0326 | 0.6639 | 0.3185 | 0.1145 | 0.0017 | 0.0196 | 0.0004 |
| 1995 | 0.1168 | 0.1177 | 0.0942 | 0.0640 | 0.0543 | 0.0335 | 0.8742 | 0.3421 | 0.1738 | 0.0250 | 0.0198 | 0.0064 |
| 1996 | 0.1066 | 0.1066 | 0.0845 | 0.0642 | 0.0466 | 0.0324 | 0.5598 | 0.2373 | 0.1510 | (0.0245) | 0.0125 | (0.0035) |
| 1997 | 0.0805 | 0.1499 | 0.1257 | 0.0588 | 0.0513 | 0.0324 | 0.4310 | 0.2076 | 0.1318 | 0.0085 | 0.0203 | 0.0020 |
| 1998 | 0.0776 | 0.0930 | 0.0796 | 0.0591 | 0.0540 | 0.0347 | 0.1247 | 0.0634 | 0.0781 | (0.0691) | 0.1130 | (0.0609) |
| 1999 | 0.0685 | 0.0986 | 0.0842 | 0.0604 | 0.0506 | 0.0317 | 0.1386 | 0.0572 | 0.0602 | 0.0622 | 0.0525 | 0.0327 |
| 2000 | 0.0704 | 0.1010 | 0.0851 | 0.0627 | 0.0522 | 0.0326 | 0.1751 | 0.0773 | 0.0763 | 0.0569 | 0.0483 | 0.0302 |
| 2001 | 0.0768 | 0.0709 | 0.0563 | 0.0459 | 0.0328 | 0.0232 | 0.1411 | 0.0839 | 0.0794 | 0.0707 | 0.0392 | 0.0271 |
| 2002 | 0.0768 | 0.0736 | 0.0583 | 0.0532 | 0.0319 | 0.0217 | 0.1609 | 0.0684 | 0.0677 | 0.0646 | 0.0429 | 0.0272 |
| 2003 | 0.0745 | 0.0684 | 0.0528 | 0.0553 | 0.0331 | 0.0224 | 0.1564 | 0.0780 | 0.0757 | 0.0687 | 0.0472 | 0.0310 |
| 2004 | 0.0731 | 0.0846 | 0.0674 | 0.0614 | 0.0432 | 0.0302 | 0.2812 | 0.0795 | 0.0689 | 0.0691 | 0.0510 | 0.0345 |
| 2005 | 0.0659 | 0.0932 | 0.0756 | 0.0590 | 0.0400 | 0.0283 | 0.1515 | 0.0866 | 0.0831 | 0.0644 | 0.0453 | 0.0301 |
| 2006 | 0.0710 | 0.1002 | 0.0813 | 0.0674 | 0.0403 | 0.0260 | 0.1258 | 0.1015 | 0.0971 | 0.0681 | 0.0470 | 0.0314 |
| 2007 | 0.0692 | 0.0999 | 0.0810 | 0.0794 | 0.0390 | 0.0249 | 0.1289 | 0.1170 | 0.1095 | 0.0687 | 0.0553 | 0.0385 |
| 2008 | 0.0995 | 0.1074 | 0.0838 | 0.0557 | 0.0370 | 0.0259 | 0.1129 | 0.1171 | 0.1104 | 0.0747 | 0.0807 | 0.0585 |
| 2009 | 0.0645 | 0.0810 | 0.0644 | 0.0455 | 0.0246 | 0.0168 | 0.1313 | 0.0525 | 0.0501 | 0.0700 | 0.0779 | 0.0554 |
| 2010 | 0.0628 | 0.0967 | 0.0793 | 0.0764 | 0.0382 | 0.0258 | 0.1387 | 0.0517 | 0.0500 | 0.0516 | 0.0740 | 0.0533 |
| 2011 | 0.0596 | 0.0852 | 0.0771 | 0.0766 | 0.0366 | 0.0259 | 0.1328 | 0.0769 | 0.0735 | 0.0566 | 0.0801 | 0.0553 |
| 2012 | 0.0525 | 0.0785 | 0.0711 | 0.0734 | 0.0353 | 0.0250 | 0.3149 | (0.1692) | (0.1319) | 0.0711 | 0.0935 | 0.0612 |
| 2013 | 0.0470 | 0.0728 | 0.0659 | 0.0704 | 0.0341 | 0.0241 | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! |

# Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous 

Table A17 Deficit \& Balance of Payments to Y and, endogenous inflation rate, $\mathrm{HA}_{r(i)}$, the growth rate of $\mathrm{Y}, g_{Y}^{*}$, and endogenous rate of tech progress, $g_{A}^{*}$. by country, 1990-2013

|  | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}^{\text {d }}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1 \mathrm{ipRI}}$ | bop | $\Delta \mathrm{d}$ | $\mathrm{SPRI}^{-1} \mathrm{ipRI}$ | bop |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 16. Thailand |  |  | 17. Vietnam |  |  | G | PRI | TOTAL | 17. Nigeria |  |  |
| 1990 | 0.0545 | (0.1520) | (0.0975) | (0.0306) | (0.1363) | (0.1669) | 18. South Africa |  |  |  |  |  |
| 1991 | 0.0445 | (0.1336) | (0.0891) | (0.0261) | (0.0900) | (0.1161) | (0.0401) | 0.0636 | 0.0235 |  |  |  |
| 1992 | 0.0276 | (0.0953) | (0.0678) | (0.0198) | (0.0617) | (0.0815) | (0.0468) | 0.0725 | 0.0256 |  |  |  |
| 1993 | 0.0195 | (0.0827) | (0.0632) | (0.0478) | (0.0919) | (0.1398) | (0.0789) | 0.0986 | 0.0197 |  |  |  |
| 1994 | 0.0310 | (0.1019) | (0.0709) | (0.0157) | (0.1173) | (0.1331) | (0.0739) | 0.0921 | 0.0182 |  |  |  |
| 1995 | 0.0370 | (0.1331) | (0.0961) | (0.0054) | (0.0976) | (0.1030) | (0.0892) | 0.0949 | 0.0058 | 0.0006 | (0.0045) | (0.0039) |
| 1996 | 0.0110 | (0.1100) | (0.0990) | (0.0019) | (0.1256) | (0.1275) | (0.0476) | 0.0340 | (0.0136) | 0.0146 | (0.0421) | (0.0275) |
| 1997 | (0.0038) | (0.0103) | (0.0141) | (0.0175) | (0.0838) | (0.1013) | (0.0514) | 0.0443 | (0.0070) | (0.0019) | (0.0351) | (0.0370) |
| 1998 | (0.0289) | 0.1576 | 0.1288 | (0.0013) | (0.0919) | (0.0932) | (0.0342) | 0.0230 | (0.0112) | (0.0514) | (0.1217) | (0.1732) |
| 1999 | (0.0342) | 0.1354 | 0.1012 | (0.0016) | (0.0408) | (0.0424) | (0.0285) | 0.0150 | (0.0135) | (0.0954) | 0.3242 | 0.2288 |
| 2000 | (0.0223) | 0.0941 | 0.0718 | (0.0285) | (0.0110) | (0.0395) | (0.0179) | 0.0199 | 0.0021 | (0.0231) | 0.3897 | 0.3665 |
| 2001 | (0.0244) | 0.0735 | 0.0491 | 0.0132 | (0.0499) | (0.0367) | (0.0224) | 0.0287 | 0.0063 | (0.0425) | 0.0651 | 0.0226 |
| 2002 | (0.0143) | 0.0658 | 0.0515 | (0.0152) | (0.0531) | (0.0684) | (0.0098) | 0.0197 | 0.0099 | (0.0066) | 0.0415 | 0.0349 |
| 2003 | 0.0041 | 0.0458 | 0.0499 | (0.0356) | (0.0656) | (0.1011) | (0.0096) | 0.0244 | 0.0148 | 0.0304 | (0.0362) | (0.0058) |
| 2004 | (0.0063) | 0.0345 | 0.0282 | (0.0367) | (0.0593) | (0.0960) | (0.0285) | 0.0231 | (0.0054) | (0.0727) | 0.1608 | 0.0880 |
| 2005 | (0.0079) | (0.0323) | (0.0403) | (0.0265) | (0.0365) | (0.0631) | (0.0241) | (0.0024) | (0.0265) | (0.1017) | 0.2037 | 0.1019 |
| 2006 | (0.0131) | 0.0075 | (0.0056) | (0.0194) | (0.0493) | (0.0687) | (0.0020) | (0.0254) | (0.0275) | (0.1660) | 0.4088 | 0.2428 |
| 2007 | (0.0146) | 0.0637 | 0.0491 | (0.0164) | (0.1773) | (0.1938) | 0.0058 | (0.0527) | (0.0469) | (0.1999) | 0.2598 | 0.0599 |
| 2008 | (0.0172) | 0.0048 | (0.0124) | (0.0164) | (0.1736) | (0.1901) | 0.0164 | (0.0847) | (0.0683) | (0.2052) | 0.3504 | 0.1451 |
| 2009 | (0.0067) | 0.0758 | 0.0692 | (0.0123) | (0.1251) | (0.1374) | (0.0071) | (0.0628) | (0.0699) | (0.1557) | 0.1382 | (0.0175) |
| 2010 | (0.0124) | 0.0451 | 0.0327 | (0.0156) | (0.1245) | (0.1401) | (0.0549) | 0.0203 | (0.0346) | (0.0962) | 0.2161 | 0.1199 |
| 2011 | (0.0124) | 0.0451 | 0.0327 | (0.0156) | (0.1245) | (0.1401) | (0.0312) | 0.0069 | (0.0243) | (0.1822) | 0.3317 | 0.1496 |
| 2012 | (0.0124) | 0.0451 | 0.0327 | (0.0156) | (0.1245) | (0.1401) | (0.0466) | 0.0149 | (0.0317) | (0.2117) | 0.3613 | 0.1496 |
| 2013 | (0.0124) | 0.0451 | 0.0327 | (0.0156) | (0.1245) | (0.1401) | (0.0352) | (0.0233) | (0.0585) | \#DIV/0! | \#DIV/0! | \#DIV/0! |


|  | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, H.A | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{g}_{\mathrm{A}}{ }^{*}$ | Infla.rate, HA | $\mathrm{gy}^{*}$ | $\mathrm{ga}_{\text {A }}{ }^{\text { }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 16. Thailand |  |  | 17. Vietnam |  |  | 18. South Africa |  |  | 17. Nigeria |  |  |
| 1990 | 0.2608 | 0.2308 | 0.1656 | 0.4717 | 0.1220 | 0.0705 | (0.0107) | 0.0655 | (0.0060) |  |  |  |
| 1991 | 0.2125 | 0.2059 | 0.1437 | 0.4209 | 0.1161 | 0.0722 | 0.0379 | 0.0410 | 0.0122 |  |  |  |
| 1992 | 0.1857 | 0.1795 | 0.1242 | 0.2329 | 0.1300 | 0.0913 | 0.0549 | 0.0377 | 0.0142 |  |  |  |
| 1993 | 0.1509 | 0.1512 | 0.1074 | 0.1668 | 0.1662 | 0.1249 | 0.0681 | 0.0494 | 0.0252 |  |  |  |
| 1994 | 0.1397 | 0.1497 | 0.1033 | 0.1391 | 0.1517 | 0.1150 | 0.0754 | 0.0588 | 0.0330 |  |  |  |
| 1995 | 0.1152 | 0.1430 | 0.0969 | 0.1851 | 0.1812 | 0.1438 | 0.0756 | 0.0794 | 0.0479 | 0.1619 | 0.0619 | 0.0374 |
| 1996 | 0.0947 | 0.1256 | 0.0855 | 0.1236 | 0.1705 | 0.1323 | 0.0772 | 0.0694 | 0.0422 | 0.2226 | 0.0525 | 0.0193 |
| 1997 | 0.0639 | 0.0866 | 0.0468 | 0.1432 | 0.1600 | 0.1179 | 0.0946 | 0.0596 | 0.0427 | 0.1983 | 0.0659 | 0.0243 |
| 1998 | 0.1138 | 0.0665 | 0.0426 | 0.1464 | 0.1523 | 0.1085 | 0.0830 | 0.0647 | 0.0436 | 0.4370 | 0.0446 | 0.0106 |
| 1999 | 0.0978 | 0.0655 | 0.0424 | 0.1372 | 0.1339 | 0.0928 | 0.0779 | 0.0581 | 0.0383 | 0.2998 | 0.0405 | 0.0103 |
| 2000 | 0.0970 | 0.0761 | 0.0483 | 0.1329 | 0.1346 | 0.0910 | 0.0829 | 0.0578 | 0.0408 | 1.2018 | 0.0583 | 0.0112 |
| 2001 | 0.0855 | 0.0759 | 0.0476 | 0.1256 | 0.1314 | 0.0866 | 0.0745 | 0.0588 | 0.0375 | 0.1627 | 0.0600 | 0.0305 |
| 2002 | 0.0813 | 0.0745 | 0.0452 | 0.1135 | 0.1336 | 0.0886 | 0.0819 | 0.0598 | 0.0416 | 0.1663 | 0.0428 | 0.0148 |
| 2003 | 0.0803 | 0.0751 | 0.0450 | 0.1020 | 0.1344 | 0.0905 | 0.0776 | 0.0628 | 0.0414 | 0.2870 | 0.0665 | 0.0344 |
| 2004 | 0.0813 | 0.0805 | 0.0493 | 0.1012 | 0.1322 | 0.0881 | 0.0810 | 0.0724 | 0.0516 | 0.0968 | 0.0342 | 0.0072 |
| 2005 | 0.0779 | 0.0925 | 0.0601 | 0.1157 | 0.1221 | 0.0886 | 0.0829 | 0.0673 | 0.0468 | (0.9440) | 0.0100 | (0.0144) |
| 2006 | 0.0806 | 0.0847 | 0.0552 | 0.1044 | 0.1247 | 0.0826 | 0.0859 | 0.0749 | 0.0539 | 0.4559 | 0.0347 | 0.0056 |
| 2007 | 0.0834 | 0.0727 | 0.0467 | 0.0937 | 0.1522 | 0.1053 | 0.0799 | 0.0915 | 0.0693 | 3.4716 | (0.0225) | (0.0417) |
| 2008 | 0.0758 | 0.0798 | 0.0540 | 0.0892 | 0.1462 | 0.1040 | 0.0740 | 0.0961 | 0.0740 | (0.0016) | 0.0290 | 0.0017 |
| 2009 | 0.0659 | 0.0528 | 0.0352 | 0.0848 | 0.1252 | 0.0875 | 0.0687 | 0.0668 | 0.0486 | 0.3641 | 0.0686 | 0.0371 |
| 2010 | 0.0733 | 0.0672 | 0.0448 | 0.1055 | 0.1461 | 0.0960 | 0.0670 | 0.0674 | 0.0506 | 0.1791 | 0.0776 | 0.0462 |
| 2011 | 0.0740 | 0.0621 | 0.0454 | 0.0962 | 0.1253 | 0.0899 | 0.0613 | 0.0930 | 0.0523 | 1.0344 | 0.1910 | 0.0931 |
| 2012 | 0.0689 | 0.0584 | 0.0428 | 0.0832 | 0.1114 | 0.0799 | 0.0674 | 0.0871 | 0.0502 | 0.6844 | 0.1629 | 0.0769 |
| 2013 | 0.0644 | 0.0552 | 0.0404 | 0.0733 | 0.1002 | 0.0719 | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! | \#DIV/0! |

## Appendix 1, HEU

## 2. Figures

## Geometric measurements clarifying the essence of Phillips unemployment

This section of part 1 of Appendix 1 is composed of the following 15 figures for 68 countries, 1990-2012, consistently marching with the KEWT database series, 8.14 and 9.15 .

Here is the list of these 15 figures at a glance.
Figure A1-1 Endogenous Phillips curve/line that uses endogenous inflation rate and endogenous or external rate of employment (1)
Figure A1-2 Endogenous Phillips curve/line that uses endogenous inflation rate and endogenous or external rate of employment (2)
Figure A1-3 Growth rate of employment in equilibrium and endogenous/external in inflation rate (1)

Figure A1-4 Growth rate of employment in equilibrium and endogenous/external in inflation rate (2)
Figure A1-5 Two basic functions of the growth rate of population/employees by sector: the US, Japan, Germany, and Russia 2007 (1)

Figure A1-6 Two basic functions of the growth rate of population/employees by sector: Sweden, UK, China, and India 2007 (2)
Figure A1-7 Function of $r^{*}(n)$ that suggests the relationship between the rate of unemployment and the inflation rate (1)
Figure A1-8 Function of $r^{*}(n)$ that suggests the relationship between the rate of unemployment and the inflation rate (2)
Figure A1-9 Comparisons of various inflation rates, endogenous and external, by area 1990-2007

Figure A1-10 The rate of change in the relative share of capital by country
Figure A1-11 The of change in the relative share of capital versus the wage growth ratio of external to endogenous
Figure A1-12 The external rate of unemployment and, the inflation rate as 10 year debt yield less the real rate of return, and the real rate of return by sector (1)
Figure A1-13 The external rate of unemployment and, the inflation rate as 10 year debt yield less the real rate of return, and the real rate of return by sector (2)

Figure A1-14 Endogenous rates of (un)employment in equilibrium and the private sector/government sector in the rate of (un)employment (1)
Figure A1-15 Endogenous rates of (un)employment in equilibrium and the private sector/government sector in the rate of (un)employment (2)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Phillips (1)

| Inflation rate (Endo) to the rate of (un)employment (Endo) in equilibrium: 13 Euro currency area | Inflation rate (Endo) to external rate of unemployment: 13 Euro currency area |
| :---: | :---: |
| Inflation rate (Endo) to the rate of unemployment (Endo)in equilibrium: France | Inflation rate (Endo) to the external rate of unemployment: France |
| Inflation rate (Endo) to the rate of unemployment (Endo) in equilibrium: Germany | Inflation rate (Endo) to the external rate of unemployment: Germany |
| Inflation rate (Endo) to the rate of unemployment (Endo) in equilibrium: Italy | Inflation rate (Endo) to the external rate of unemployment: Italy |

Figure A1-1 Endogenous Phillips curve/line that uses endogenous inflation rate and endogenous or external rate of employment (1)

## Appendix 1, $\boldsymbol{H E U}$

Endogenous Phillips (2)


Figure A1-2 Endogenous Phillips curve/line that uses endogenous inflation rate and endogenous or external rate of employment (2)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Phillips (3)



Figure A1-3 Growth rate of employment in equilibrium and endogenous/external in inflation rate (1)

## Appendix 1, HEU

Endogenous Phillips (4)


Figure A1-4 Growth rate of employment in equilibrium and endogenous/external in inflation rate (2)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Phillips (5)



Figure A1-5 Two basic functions of the growth rate of population/employees by sector: the US, Japan, Germany, and Russia 2007 (1)

## Appendix 1, $\boldsymbol{H E U}$

Endogenous Phillips (6)


The speed of convergence function of $n_{G}$ at the governemntisetor: Sweden, UK, China, and


The speed of convergence fucntion of $n_{P R I}$ at the private sector: Sweden, UK, China, and India;


| The rate of return funtion of $\boldsymbol{n}_{P R I}$ at the private sector: Sweeden, UK, China, and India; 2007 |  |  |
| :---: | :---: | :---: |
| $\underline{0.60}$ |  |  |
|  |  |  |
|  |  |  |
| 0.40 ---CHr*PRI |  |  |
| 0.30 - $\mathbb{N} \mathrm{r}$ *PRI |  |  |
|  |  |  |
|  | - - |  |
| $00.015-0.01-0.000_{0.10} 0$ |  | $\begin{array}{llllll}0 & 0.005 & 0.01 & 0.015 & 0.02 & 0.025\end{array}$ |
|  |  | $n_{\text {EQUUI(PRI) }}$ |

Figure A1-6 Two basic functions of the growth rate of population/employees by sector: Sweden, UK, China, and India 2007 (2)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Phillips (7)



Figure A1-7 Function of $r^{*}(n)$ that suggests the relationship between the rate of unemployment and the inflation rate (1)

## Appendix 1, HEU

Endogenous Phillips (8)


Figure A1-8 Function of $r^{*}(n)$ that suggests the relationship between the rate of unemployment and the inflation rate (2)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Inflation (1)



Note: For external inflation rate, the rate of change in consumers' price index, $g_{C P I}$, was taken. For endogenous infltion rates, one is the weighted average of the theoretical wage rate and the rate of return , $g_{P}=\alpha \cdot g_{r}+(1-\alpha) g_{w}$, and the other is 10 year debt yield less the real rate of return at convergence, Inf.rate $=r_{D E B T}-\left(r^{*}-r_{H A}^{*}\right)$.

Data source: KEWT 3.09 of fifty-eight countries by sector, 1990-2007, whose ten original data come from International Financial Statistics Yearbook, IMF.

Figure A1-9 Comparisons of various inflation rates, endogenous and external, by area 1990-2007

## Appendix 1, HEU

Endogenous Inflation (2)


Figure A1-10 The rate of change in the relative share of capital by country

## Algebraic pertinently consistent with Geometric:

Tables and figures for Phillips Curve, exogenous vs. endogenous

## Endogenous Inflation (3)



Figure A1-11 The of change in the relative share of capital versus the wage growth ratio of external to endogenous

## Appendix 1, HEU

## Growth rate of Employment in Equilibrium (1)



Figure A1-12 The external rate of unemployment and, the inflation rate as 10 year debt yield less the real rate of return, and the real rate of return by sector (1)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Growth rate of Employment in Equilibrium (2)



Figure A1-13 The external rate of unemployment and, the inflation rate as 10 year debt yield less the real rate of return, and the real rate of return by sector (2)

## Appendix 1, HEU

## Growth Rate of Employment in Equilibrium (3)



Figure A1-14 Endogenous rates of (un)employment in equilibrium and the private sector/government sector in the rate of (un)employment (1)

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

## Growth Rate of Employment in Equilibrium (4)



Figure A1-15 Endogenous rates of (un)employment in equilibrium and the private sector/government sector in the rate of (un)employment (2)

## Appendix 1, HEU

## 3. Notations

## Equations endogenously connected with inflation rate, returns, and growth

### 3.1 Four basic equations at convergence

The rate of return at convergence:

$$
\begin{equation*}
r^{*}=\alpha\left(\frac{i\left(1-\beta^{*}\right)(1+n)+n(1-\alpha)}{i \cdot \beta^{*}(1-\alpha)}\right) \tag{1}
\end{equation*}
$$

where $r^{*}=\frac{\alpha}{\Omega^{*}}$ and $\Omega^{*}=\left(\frac{i \cdot \beta^{*}(1-\alpha)}{i\left(1-\beta^{*}\right)(1+n)+n(1-\alpha)}\right)$.

The horizontal asymptote (HA) of the rate of returns:

$$
\begin{equation*}
r_{H A}^{*}=\frac{\alpha\left(1-\beta^{*}\right)(1+n)}{\beta^{*}(1-\alpha)} \tag{2}
\end{equation*}
$$

The real rate of return:

$$
\begin{equation*}
r_{R E A L}^{*}=r^{*}-r_{H A}^{*}=n\left(\frac{\alpha}{i \cdot \beta^{*}}\right)=\frac{\alpha \cdot n}{\beta^{*} \cdot i} .1 \tag{3}
\end{equation*}
$$

The HA is used so as to match the fact that the lower limit of the nominal interest rate is zero when an inflation rate is formulated endogenously.

For an endogenous inflation $(+) /$ deflation $(-)$ rate:

$$
\begin{gather*}
\text { Inf.rate }=\text { Nominal rate }-r_{R E A L}^{*} \\
\text { and, } \quad \text { def. rate }=r_{R E A L}^{*}-\text { Nominal rate } \tag{4}
\end{gather*}
$$

where 10 year debt yield, $r_{D E B T}$, is used for the market nominal rate.

### 3.2 The inflation/deflation rate, the rate of return, and the growth rate of output

The growth rate of output at convergence:

$$
\begin{equation*}
g_{Y}^{*}=\frac{i\left(1-\beta^{*}\right)(1+n)}{1-\alpha}+n \tag{5}
\end{equation*}
$$

where $g_{A}^{*}=i\left(1-\beta^{*}\right)$ and $g_{y}^{*}=i\left(1-\beta^{*}\right) /(1-\alpha)$ hold.
The relationship between the growth rate of output and the rate of return each convergence:

$$
\begin{equation*}
g_{Y}^{*}=\left(\frac{i \cdot \beta^{*}}{\alpha}\right) r^{*} \text { or } \quad r^{*}=\left(\frac{\alpha}{i \cdot \beta^{*}}\right) g_{Y}^{*}, \text { or }\left(\frac{\alpha}{i \cdot \beta^{*}}\right)=\frac{r^{*}}{g_{Y}^{*}} \tag{6}
\end{equation*}
$$

Then, using Eq. (3) above, Eq. (4) is expressed as
${ }^{1}$ If $x=r_{H A}^{*} / r^{*}, x=\frac{\alpha \cdot i\left(\left(1-\beta^{*}\right)(1+n)\right)}{\alpha\left(i\left(1-\beta^{*}\right)(1+n)+n(1-\alpha)\right)}$ and $r_{R E A L}^{*}=(1-x) r^{*}$. This equation
is consistent with Eq. 6 , yet is not simplified enough.

$$
\begin{equation*}
\text { Inf.rate }=r_{D E B T}-n\left(\frac{r^{*}}{g_{Y}^{*}}\right) \tag{7}
\end{equation*}
$$

Or, Eq. (4) is expressed as

$$
\begin{equation*}
\text { Def.rate }=n\left(\frac{r^{*}}{g_{Y}^{*}}\right)-r_{D E B T} \tag{8}
\end{equation*}
$$

For Eq. (7), assuming that $r_{D E B T}$ is fixed, the higher $n\left(\frac{r^{*}}{g_{Y}^{*}}\right)$ the lower the inflation rate is. This indicates that the growth rate of population $n$ and the rate of return should be high and the growth rate of output at convergence should be low if the inflation rate should be lowered. And, the lower the $r_{D E B T}$ the lower the inflation rate is.

For Eq. (8), assuming that $r_{D E B T}$ is fixed, the lower $n\left(\frac{r^{*}}{g_{Y}^{*}}\right)$ the lower the deflation rate is. This indicates that the growth rate of population $n$ and the rate of return should be low and the growth rate of output at convergence should be high if the deflation rate should be lowered. And, the higher the $r_{D E B T}$ the lower the deflation rate is.

If a desired inflation/deflation rate is set zero:

$$
\begin{equation*}
r_{D E B T}=n\left(\frac{r^{*}}{g_{Y}^{*}}\right) \text { or, } n \cdot r^{*}=r_{D E B T} \cdot g_{Y}^{*} \tag{9}
\end{equation*}
$$

Eq. (8) does not use expected rates but $r_{D E B T}$ of the financial/market assets and $n, r^{*}$, and $g_{Y}^{*}$ of the real assets, where $r_{D E B T}$ and $n$ are given externally.

## Appendix 1, HEU

## Part 2: The background of Phillips unemployment

Part 2 is composed of the following nine figures/illustrations, which clarify the underlying background of Phillips unemployment, from the aspect of geometrical measurement.

Here is the list of nine figures at a glance.
Figure A2-1 Hyperbola $r^{*}(i)$ and endogenous inflation/deflation expressed by HA
Figure A2-2 Phillips curve is expressed by linear, due to hyperbola $r^{*}(i)$ and $n(i)=i(n)$
Figure A2-3 Explanatories for speed $(i)$ and $\operatorname{speed}(n), i(n)$ and $n(i)$, and $r^{*}(i)$ and $r^{*}(n)$
Figure A2-4 Two fundamental functions of the ratio of investment to output in equilibrium, inherent in the endogenous I-S diagram
Figure A2-5 Two fundamental functions of the ratio of investment to output in equilibrium, inherent in the endogenous Phillips curve
Figure A2-6 Endogenous Phillips' line versus external Phillips' curve: the inflation rate to the rate of unemployment
Figure A2-7 Endogenous Phillips' line versus external Phillips' curve: the inflation rate to the rate of unemployment
Figure A2-8 Effective range of equilibrium versus risky range to close disequilibrium for $i=I / Y$
Figure A2-9 Curvature most useful for policy-makers and decision-makers

The above nine figures/illustrations show hyperbola measurements, which are each short-cut of endogenous equations. The essence of the Phillip's curve and/or line is completely supported and reinforced by these figures. When statistics data are used, the Phillips curve is estimated while when endogenous data are used, the Phillips line is measured accurately.

If statistics data $=$ endogenous data hold, as in the $E E S$, the Phillips curve is always shown by lines. The mechanics is the same regardless of which data are used. We are much obliged to Phillips on this discovery and accordingly, Phillip's tests of practice machine actually manufactured by Langley family, as shown in the literature.

The substance of the machine is now scientifically fulfilled by the method of the $E E S$ and its hyperbola topology in the two-dimensional plane.

Algebraic pertinently consistent with Geometric:
Tables and figures for Phillips Curve, exogenous vs. endogenous


Figure 3-1 r*(i) by country 2010
Source: the EES, p.506, 2013.

Figure A2-1 Hyperbola $r^{*}(i)$ and endogenous inflation/deflation expressed by HA

## Appendix 1, $\boldsymbol{H E U}$








Figure 3-1 r*(n) by country 2010
Source: the EES, p.516, 2013.
Figure A2-2 Phillips curve is expressed by linear, due to hyperbola $r^{*}(i)$ and $n(i)=i(n)$


BOX B-1 Cases when each of elements, $a, b, c, d$, is zero (the EES, 478, 2013)
i) $\mathrm{a}=0$, the linear type: $\mathrm{y}=\frac{\mathrm{cx}+\mathrm{d}}{\mathrm{b}} \quad$ or $\mathrm{y}=\frac{\mathrm{c}}{\mathrm{b}} \mathrm{x}+\frac{\mathrm{d}}{\mathrm{b}} . \quad$ To $r^{*}(n)$.
ii) $\quad \mathrm{b}=0: \mathrm{y}=\frac{\mathrm{cx}+\mathrm{d}}{\mathrm{ax}}$ and $\mathrm{y}=\frac{\mathrm{c}}{\mathrm{a}}+\frac{\mathrm{d}}{\mathrm{ax}} . \quad$ To $r^{*}(i) ; \quad \beta^{*}(i)$.
iii) $\quad c=0$ and $d=1: y=\frac{1}{a x+b} . \quad$ To $\operatorname{speed}(i)$ and $\operatorname{speed}(n)$.
iv) $\quad \mathrm{d}=0: \mathrm{y}=\frac{\mathrm{cx}}{\mathrm{ax}+\mathrm{b}}$ and $\mathrm{y}=\frac{\mathrm{c}}{\mathrm{a}}+\frac{-\frac{\mathrm{b} \cdot \mathrm{c}}{\mathrm{a}}}{\mathrm{ax}+\mathrm{b}} . \quad$ To $n(i)$ or $i(n) ; \quad \Omega^{*}(i) \quad$ and $\Omega^{*}(n) ; \quad \Omega^{*}\left(\beta^{*}\right)$.
v) $\mathrm{c}=0: \mathrm{y}=\frac{\mathrm{d}}{\mathrm{ax}+\mathrm{b}}$. $\quad$ To $\Omega^{*}(n)$.
vi) No zero, the standard type: $\mathrm{y}=\frac{\mathrm{cx}+\mathrm{d}}{\mathrm{ax}+\mathrm{b}}$ and $\mathrm{y}=\frac{\mathrm{c}}{\mathrm{a}}+\frac{\mathrm{d}-\frac{\mathrm{b} \cdot \mathrm{c}}{\mathrm{a}}}{\mathrm{ax}+\mathrm{b}}$. $\quad$ To $\beta^{*}(n) ; \quad \alpha(i)$ and $\alpha(n)$.

Figure A2-3 Explanatories for $\operatorname{speed}(i)$ and $\operatorname{speed}(n), i(n)$ and $n(i)$, and $r^{*}(i)$ and $r^{*}(n)$

## Appendix 1, HEU

$1 . \rightarrow$ The speed of convergence function of the ratio of investment to output: $i=I / Y$


1. $\rightarrow$ On the vertical asymptote (VA), the speed of convergence $\cdot 1 / \lambda^{*}$, is infinite.
$2 . \rightarrow$ The horizontal asymptote (HA) is $1 / \lambda^{*}=0$ and the curvature $=1$.
$3 . \rightarrow$ The curve is reversed if. $\left(1-\beta^{*}\right)\left(1-\delta_{0}\right)<0$, which rarely occurs. *
$2 . \rightarrow$ The rate of return function of the ratio of investment to output: $i=I / Y$

2. $\rightarrow$ The horizontal asymptote•(HA) is:: $\left(\alpha\left(1-\beta^{*}\right)(1+n)\right) /\left(\beta^{*}(1-\alpha)\right)$.
$2 . \rightarrow$ The first quadrant on the LHS shows inflation with diminishing returns.
$3 . \rightarrow$ The second quadrant on the RHS shows real deflation with increasing returns.
3. $\rightarrow$ If the sum of $r^{*}(i)$ and its H.A. are plus, these are normal; if these are minus, it implies that 'falling into the trap of liquidity. $\mathrm{H} . \mathrm{A}=0$ implies a base of inflation/deflation.
$5 . \rightarrow$ The curve is reversed under $a \cdot f=\alpha \cdot n \cdot \beta^{*}(1-\alpha)^{2}<0$; from the first to second quadrant. This occurs often at the government sector, where its relative share of capital turns to minus due to huge deficits or a minus saving.
Note: Two parts of figures above show related equations, where parameters except for $i=I / Y$ or $n$ are fixed. $\cdots$ These figures hold by sector and at the total economy; $\mathrm{T}=\mathrm{G}+\mathrm{PRI}$.

Figure A2-4 Two fundamental functions of the ratio of investment to output in equilibrium, inherent in the endogenous I-S diagram

## Algebraic pertinently consistent with Geometric: Tables and figures for Phillips Curve, exogenous vs. endogenous

$1 \rightarrow$ The speed of convergence function of the growth rate of employees, $n:\left(\frac{1}{\lambda^{*}}\right)(n)$


1. On the vertical asymptote (V.A.), the speed of convergence, $1 / \lambda^{*}$, is infinite.
2. The horizontal asymptote (H.A.) is $1 / \lambda^{*}=0$ and , the curvature $=1$.
3. The curve stays at the first and third quadrants (no reverse). $\cdot$ Its vertical asymptote shifts from the first to fourth quadrant: $n=-\frac{i\left(1-\beta^{*}\right)\left(1-\delta_{0}\right)}{(1-\alpha)}$.
4. "At the V.A. it is mot risky."The milder the curve the more stable the equilibrium is.
5. The rate of return function of the growth rate of employees, $n: r^{*}(n)$

6. The higher the intercept the better to increase employment; $\alpha\left(1-\beta^{*}\right) /\left(\beta^{*}(1-\alpha)\right.$.
7. If the gradient is negative, the rate of unemployment does not improve (as the LHS). $\cdots$ If the gradient is positive, the rate of unemployment improves (as the RHS): $\frac{\alpha\left(i\left(1-\beta^{*}\right)+(1-\alpha)\right)}{i \cdot \beta^{*}(1-\alpha)}=1$
8. Calculate the intercept divided by the V.A. of $\left(\frac{1}{\lambda^{*}}\right)(n)$ and the gradient divided by the V.A. of $\left(\frac{1}{\lambda^{*}}\right)(n) \cdot \cdots$ Then, the relationship between the rate of return and the growth rate of population, $r^{*}(n)$, is clarified structurally. An endogenous rate of (un)employment is related tor ${ }^{*}(n)$

Figure A2-5 Two fundamental functions of the ratio of investment to output in equilibrium, inherent in the endogenous Phillips curve

## Appendix 1, $\boldsymbol{H E U}$



Phillips' line in equilibrium sets a result (inflation rate of the above LHS) on the $y$ axis and a result (rate of employment of the above RHS) on the x axis. Full employment $\cdot n=n_{E}$, is a base by sector, where Phillips' line overlaps the $y$ axis. The rate of unemployment occurs if $n>n_{E}$ holds in equilibrium. The average wage rate is the same by sector, but its marginal values differ forequilibrium, by year.
Note: Illustration here shows all of related equations, where related parameters, except for $i=I / Y$ or $n$, are fixed. Corresponding figures hold by sector and at the total economy.

Figure A2-6 Endogenous Phillips' line versus external Phillips' curve: the inflation rate to the rate of unemployment


For endogenous rate of employment, if equilibrium holds at $n=n_{E}$, it shows full employment. If $n>n_{E}$, the endogenous rate of employment is negative, while if $n<n_{E}$, it is positive. .
At equilibrium, the growth rate of population, $n$, is set full employment under $w=w_{G}=w_{P R I}$. Endogenously, both inflation and deflation are measured. -Inflation rate is' 10 year debt yield less the real rate of retum, which is 'the rate of retum less the horizontal asymptote of $r^{*}(i)$.'
Since $r^{*}(n)$ is not a hyperbolic but a line, endogenous Phillips' shows a line (not a curve). *
Figure A2-7 Endogenous Phillips' line versus external Phillips' curve: the inflation rate to the rate of unemployment

Algebraic pertinently consistent with Geometric:
Tables and figures for Phillips Curve, exogenous vs. endogenous


Note: $r^{*}(i)$ shows the case of $\alpha>0$ so that the effective range of $i=I / Y$ is the first or fourth quadrant. The shadow range of $i=1 / Y$ is close to the vertical asymptote of either of or both of $\left(1 / \lambda^{*}\right)(i)$ and, $r^{*}(i)$. Each risky range of $i=l / Y$ is determined by the shape of the curvature: The shaper the curve, in the case of the right angle hyperbolic, the more close to CRC the DRC becomes under the same curvature of 1.0 ..

Figure A2-8 Effective range of equilibrium versus risky range to close
disequilibrium for $i=I / Y$

## Appendix 1, $\boldsymbol{H E U}$



Note: This figure is important as a preliminary step into an endogenous Phillips' curveline.
Two functions, $\left(1 / \lambda^{*}\right)(i)$ and, $r^{*}(i)$, each constitutes a right angle hyperbolic, whose curvature is $1.0 \ldots$
Nevertheless, each shape differs by 'the length of the arrow, the' The longer the arrow, the more diminishing, The author is grateful to the advice of Yoshiomi Furuta Prof. of mathematics...
$\downarrow$
Case of the hyperbolic; $\left(\frac{1}{\lambda^{*}}\right)(i)$ : The V.A. is $-b / a$, where $b=(1-\alpha) n$ and $a=\left(1-\beta^{*}\right)\left(1-\delta_{0}\right)$. The curvature is the same 1.0 at any point of $i=I / Y$ yet, the shape differs significantly by the magnitude of $\sqrt{c / a}$, where $\frac{c}{a}=\frac{\alpha\left(1-\beta^{*}\right)(1+n)}{\beta^{*}(1-\alpha)}$. Because it is required to shorten the distance between the V.A. and the root square $\sqrt{c / a} \cdot \sqrt{c / a}-b / a$, where $c=\alpha\left(1-\beta^{*}\right)(1+n) \cdots$ When $\sqrt{c / a} \cdots$ is lowered, the shape becomes sharpened approaching CRC.

Figure A2-9 Curvature most useful for policy-makers and decision-makers

